

# Package ‘VARshrink’

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**Title** Shrinkage Estimation Methods for Vector Autoregressive Models

**Version** 0.3.1

**Description** Vector autoregressive (VAR) model is a fundamental and effective approach for multivariate time series analysis. Shrinkage estimation methods can be applied to high-dimensional VAR models with dimensionality greater than the number of observations, contrary to the standard ordinary least squares method. This package is an integrative package delivering nonparametric, parametric, and semiparametric methods in a unified and consistent manner, such as the multivariate ridge regression in Golub, Heath, and Wahba (1979) <doi:10.2307/1268518>, a James-Stein type nonparametric shrinkage method in Opgen-Rhein and Strimmer (2007) <doi:10.1186/1471-2105-8-S2-S3>, and Bayesian estimation methods using noninformative and informative priors in Lee, Choi, and S.-H. Kim (2016) <doi:10.1016/j.csda.2016.03.007> and Ni and Sun (2005) <doi:10.1198/073500104000000622>.

**License** GPL-3

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Acoef\_sh

*Coefficient matrices of endogenous variables*

---

### Description

Returns the estimated coefficient matrices of the lagged endogenous variables of a VAR(p) model. This is a modification of vars::Acoef() for the class "varshrinkest".

### Usage

Acoef\_sh(x)

### Arguments

x An object of class "varshrinkest", generated by VARshrink().

**Details**

Consider VAR(p) model:

$$y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + C d_t + e_t.$$

The function returns the K-by-K matrices  $A_1, \dots, A_p$  as a list object.

**Value**

A list object with K-by-K VAR coefficient matrices  $A_1, A_2, \dots, A_p$

**See Also**

[Acoef](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
Acoef_sh(estim)
```

---

arch.test\_sh

*ARCH-LM test*

---

**Description**

Performs univariate and multivariate ARCH-LM tests for a VAR. This is a modification of `vars::arch.test()` for the class "varshrinkest".

**Usage**

```
arch.test_sh(x, lags.single = 16, lags.multi = 5,
  multivariate.only = TRUE)
```

**Arguments**

<code>x</code>	An object of class "varshrinkest" obtained by <code>VARshrink()</code>
<code>lags.single</code>	An integer of the lag order used for univariate ARCH statistics.
<code>lags.multi</code>	An integer of the lag order used for multivariate ARCH statistic.
<code>multivariate.only</code>	If TRUE, only the multivariate statistic is computed.

**See Also**

[arch.test](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
arch.test_sh(estim)
```

Bcoef\_sh

*Coefficient matrix***Description**

Returns the estimated coefficients of a VAR(p) model as a matrix. This is a modification of `vars::Bcoef()` for the class "varshrinkest".

**Usage**

```
Bcoef_sh(x)
```

**Arguments**

`x` An object of class "varshrinkest" generated by `VARshrink()`.

**Details**

Consider VAR(p) model:

$$y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + C d_t + e_t.$$

The function returns the concatenated matrix  $(A_1, \dots, A_p, C)$  as a matrix object.

**Value**

A matrix holding the estimated coefficients of a VAR.

**See Also**

[Bcoef](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
Bcoef_sh(estim)
```

---

BQ\_sh *BQ function for class "varshrinkest"*

---

**Description**

This is a modification of vars::BQ() for the class "varshrinkest".

**Usage**

```
BQ_sh(x)
```

**Arguments**

x An object of class "varshrinkest" obtained by VARshrink().

**See Also**

[BQ](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
BQ_sh(estim)
```

---

calcSSE\_Acoef *Sum of squared errors (SSE) between coefficients of two VARs*

---

**Description**

Compute sum of squared errors of coefficients of lagged endogenous variables (Acoef) of two VAR models.

**Usage**

```
calcSSE_Acoef(Acoef1, Acoef2)
```

**Arguments**

Acoef1, Acoef2 Each one is a list object with K-by-K coefficient matrices of lagged endogenous variables. See help(Acoef\_sh), or, help(Acoef).

**Details**

Consider VAR(p) model:

$$y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + C d_t + e_t.$$

The SSE of two VAR(p) models is expressed as

$$\sum_{k=1}^p \sum_{i=1}^K \sum_{j=1}^K ((A_k)_{ij} - (A'_k)_{ij})^2.$$

**Value**

SSE value.

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim1 <- VARshrink(y, p = 2, type = "const", method = "fbayes")
Acoef1 <- Acoef_sh(estim1)
estim2 <- VARshrink(y, p = 2, type = "const", method = "ridge")
Acoef2 <- Acoef_sh(estim2)
calcSSE_Acoef(Acoef1, Acoef2)
```

---

causality\_sh

*Causality Analysis for class "varshrinkest"*


---

**Description**

A modification of vars::causality() for the class "varshrinkest".

**Usage**

```
causality_sh(x, cause = NULL, vcov. = NULL, boot = FALSE,
             boot.runs = 100)
```

**Arguments**

x                    An object of class "varshrinkest" obtained by VARshrink().  
cause, vcov., boot, boot.runs            Other arguments for causality analysis; see help(causality) for details.

**See Also**

[causality](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
causality_sh(estim, cause = "e")
```

---

convPsi2varresult      *Convert format for VAR coefficients from Psi to varresult*

---

### Description

Convert a matrix of VAR coefficients estimated by a shrinkage method into a list of "shrinklm" object, where the class "shrinklm" inherits the class "lm".

### Usage

```
convPsi2varresult(Psi, Y, X, lambda0, type = c("const", "trend", "both",
      "none"), ybar = NULL, xbar = NULL, Q_values = NULL, callstr = "")
```

### Arguments

Psi	An M-by-K matrix of VAR coefficients
Y	An N-by-K data matrix of dependent variables
X	An N-by-M data matrix of regressors
lambda0	A rescaled shrinkage intensity parameter, based on which the effective number of parameters is computed by $\text{Trace}(X(X'X + \text{lambda0} * I)^{-1}X')$
type	Type of deterministic variables in the VAR estimation problem. Either of "const", "trend", "both", or "none".
ybar, xbar	NULL if Y and X are not centered. Mean vectors if Y and X had been centered. If Y and X had been centered (ybar and xbar are not NULL) and type is "const" or "both", then the coefficients for the constant term is computed and concatenated to the coefficients.
Q_values	Nonnegative weight vector of length N. Default is NULL. Take weights on rows (samples) of Y and X by sqrt(Q).
callstr	The call to VARshrink().

### Details

Consider VAR(p) model:

$$y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + C d_t + e_t.$$

It can be written in the matrix form:

$$Y = X P \psi + E,$$

where Psi is a concatenated M-by-K matrix,  $\Psi = (A_1, \dots, A_p, C)^T$ . It can be written in the multiple linear regression form of a VAR(p) model:

$$y_j = X \psi_j + e_j, \quad j = 1, \dots, K,$$

where  $y_j$ ,  $\psi_j$ , and  $e_j$  are the  $j$ -th column vectors of  $Y$ ,  $\Psi$ , and  $E$ , respectively. This function converts  $\Psi$  into a list of "shrinklm" objects, where each "shrinklm" object contains the length- $M$  vector  $\psi_j$  as coefficients.

Considering that each coefficient vector  $\psi_j$  is estimated by a shrinkage method, the effective number of parameters,  $k_{eff}$ , is computed as:

$$k_{eff} = \text{Trace}(X(X^T X + \lambda_0 * I)^{-1} X^T).$$

Then, the degree of freedom of residuals is computed as:

$$df.residual = N - k_{eff},$$

where  $N$  is the number of rows of data matrices  $Y$  and  $X$ .

### Value

A list object with objects of class `c("shrinklm", "lm")`. Each "shrinklm" object has components: coefficients, residuals, fitted.values, rank, df.residual, lambda0, call, terms, svd

---

```
createVARCoefs_ltriangular
```

*Create coefficients of a VAR model*

---

### Description

Randomly create sparse lower-triangular matrices for VAR coefficients of lagged endogenous variables, and set a constant vector.

### Usage

```
createVARCoefs_ltriangular(p = 1, K = 5, diag_val = 1/p,
  num_nonzero = 0, const_vector = NULL, range_min = 0.2,
  range_max = 1/p)
```

### Arguments

<code>p</code>	lag order
<code>K</code>	Number of time series variables.
<code>diag_val</code>	diagonal values of $A_1, \dots, A_p$
<code>num_nonzero</code>	Number of nonzero entries on the lower-triangular parts of $A_1, \dots, A_p$
<code>const_vector</code>	constant vector $c$ of the VAR model
<code>range_min, range_max</code>	Each nonzero off-diagonal entry of coefficient matrices is drawn uniformly from the interval $[-range\_max, -range\_min] \cup [range\_min, range\_max]$



**Details**

Consider VAR(p) model:

$$y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + c + e_t,$$

with the constant deterministic variable ( $d_t = 1$ ). The function creates the coefficient matrices  $A_1, \dots, A_p$  and constant vector  $c$ .

Diagonal elements of each K-by-K matrix  $A_k$  are all equal to `diag_val`, and off-diagonal elements are all zero except for a few randomly selected nonzero elements. Nonzero off-diagonal elements are selected from lower-triangular parts of  $A_i$  and the values are drawn from a uniform distribution over  $[-\text{range\_max}, -\text{range\_min}] \cup [\text{range\_min}, \text{range\_max}]$ .

**Value**

A list object with components `$A` and `$c`. `$A` is a list of K-by-K matrices  $A_1, \dots, A_p$ , and `$c` is a constant vector of length K.

**Examples**

```
p <- 1; K <- 20;
const_vector <- c(rep(0.2, 5), rep(0.7, 15))
createVARCoefs_ltriangular(p = p, K = K, diag_val = 0.6,
num_nonzero = K, const_vector = const_vector, range_max = 1)
```

---

fevd.varshrinkest      *Forecast Error Variance Decomposition*

---

**Description**

Computes the forecast error variance decomposition of a VAR(p) for `n.ahead` steps. This is a modification of `vars::fevd()` for the class "varshrinkest".

**Usage**

```
## S3 method for class 'varshrinkest'
fevd(x, n.ahead = 10, ...)
```

**Arguments**

<code>x</code>	Object of class 'varshrinkest'; generated by <code>VARshrink()</code> .
<code>n.ahead</code>	Integer specifying the steps.
<code>...</code>	Currently not used.

**See Also**

[fevd](#)

---

irf.varshrinkest      *Impulse response function*

---

### Description

Computes the impulse response coefficients of a VAR(p) (or transformed VECM to VAR(p)) for n.ahead steps. This is a modification of vars::irf() for the class "varshrinkest".

### Usage

```
## S3 method for class 'varshrinkest'
irf(x, impulse = NULL, response = NULL,
     n.ahead = 10, ortho = TRUE, cumulative = FALSE, boot = TRUE,
     ci = 0.95, runs = 100, seed = NULL, ...)
```

### Arguments

x	Object of class 'varshrinkest'; generated by VARshrink()
impulse	A character vector of the impulses, default is all variables.
response	A character vector of the responses, default is all variables.
n.ahead	Integer specifying the steps.
ortho	Logical, if TRUE (the default) the orthogonalised impulse response coefficients are computed (only for objects of class 'varshrinkest').
cumulative	Logical, if TRUE the cumulated impulse response coefficients are computed. The default value is false.
boot	Logical, if TRUE (the default) bootstrapped error bands for the impulse response coefficients are computed.
ci	Numeric, the confidence interval for the bootstrapped errors bands.
runs	An integer, specifying the runs for the bootstrap.
seed	An integer, specifying the seed for the rng of the bootstrap.
...	Currently not used.

### See Also

[irf](#)

---

lm_full_Bayes_SR	<i>Full Bayesian Shrinkage Estimation Method for Multivariate Regression</i>
------------------	--

---

### Description

Estimate regression coefficients and scale matrix for noise by using Gibbs MCMC algorithm. The function assumes 1) multivariate t-distribution for noise as a sampling distribution, and 2) noninformative priors for regression coefficients and scale matrix for noise.

### Usage

```
lm_full_Bayes_SR(Y, X, dof = Inf, burnin cycle = 1000,
  mcmc cycle = 2000)
```

### Arguments

Y	An N x K matrix of dependent variables.
X	An N x M matrix of regressors.
dof	Degree of freedom for multivariate t-distribution. If dof = Inf (default), then multivariate normal distribution is applied and weight vector q is not estimated. If dof = NULL or dof <= 0, then dof and q are estimated automatically. If dof is a positive number, q is estimated.
burnin cycle, mcmc cycle	Number of burnin cycles is the number of initially generated sample values to drop. Number of MCMC cycles is the number of generated sample values to compute estimates.

### Details

Consider the multivariate regression:

$$Y = X\Psi + e, \quad e \sim mvt(0, dof, \Sigma).$$

$\Psi$  is a M-by-K matrix of regression coefficients and  $\Sigma$  is a K-by-K scale matrix for multivariate t-distribution for noise.

Sampling distribution for noise  $e$  is multivariate t-distribution with degree of freedom  $dof$  and scale matrix  $\Sigma$ :  $e \sim mvt(0, dof, \Sigma)$ . The priors are noninformative priors: 1) the shrinkage prior for regression coefficients  $\Psi$ , and 2) the reference prior for scale matrix  $\Sigma$ .

The function implements Gibbs MCMC algorithm for estimating regression coefficients  $\Psi$  and scale matrix  $\Sigma$ .

### Value

A list object with estimated parameters:  $\Psi$ ,  $\Sigma$ ,  $dof$ ,  $\delta$  ( $\delta$  is the reciprocal of  $\lambda$ ), and  $\lambda$ . Additional components are  $se.param$  (standard error of the parameters) and  $LINEXVARmodel$  (estimates under LINEX loss).

## References

S. Ni and D. Sun (2005). Bayesian estimates for vector autoregressive models. *Journal of Business & Economic Statistics* 23(1), 105-117.

---

lm_multiv_ridge	<i>Multivariate Ridge Regression</i>
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---

## Description

Estimate regression coefficients by using ridge regression.

## Usage

```
lm_multiv_ridge(Y, X, lambda = 0, do_scale = FALSE)
```

## Arguments

Y	An N x K matrix of dependent variables.
X	An N x M matrix of regressors.
lambda	Numeric vector of lambda values
do_scale	If true, X is centered and scaled, and Y is centered.

## Details

Consider the multivariate regression:

$$Y = X\text{Psi} + e.$$

Psi is a M-by-K matrix of regression coefficients. The ridge regression estimate for the coefficients is

$$\text{Psi} = (X'X + \text{lambda} * I)^{-1}X'Y.$$

## Value

A list object with the components: 1) Psi - A list of estimated Psi matrices, 2) lambda - A vector of lambda values, 3) GCV - A vector of GCV values

## References

G. H. Golub, M. Heath, G. Wahba (1979). Generalized cross-validation as a method for choosing a good ridge parameter. *Technometrics* 21(2), 215-223. doi: 10.2307/1268518

---

lm_semi_Bayes_PCV	<i>Semiparametric Bayesian Shrinkage Estimation Method for Multivariate Regression</i>
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---

### Description

Estimate regression coefficients and scale matrix for noise by using a parameterized cross validation (PCV). The function assumes 1) multivariate t-distribution for noise as a sampling distribution, and 2) informative priors for regression coefficients and scale matrix for noise.

### Usage

```
lm_semi_Bayes_PCV(Y, X, dof = Inf, lambda = NULL, lambda_var = NULL,
  prior_type = c("NCJ", "CJ"), num_folds = 5, m0 = ncol(Y))
```

### Arguments

Y	An N x K matrix of dependent variables.
X	An N x M matrix of regressors.
dof	Degree of freedom for multivariate t-distribution. If dof = Inf (default), then multivariate normal distribution is applied and weight vector q is not estimated. If dof = NULL or a numeric vector, then dof is selected by K-fold CV automatically and q is estimated.
lambda	If NULL or a vector of length >=2, it is selected by PCV.
lambda_var	If NULL, it is selected by a Stein-type shrinkage method.
prior_type	"NCJ" for non-conjugate prior and "CJ" for conjugate prior for scale matrix Sigma.
num_folds	Number of folds for PCV.
m0	A hyperparameter for inverse Wishart distribution for Sigma

### Details

Consider the multivariate regression:

$$Y = X\Psi + e, \quad e \sim mvt(0, dof, Sigma).$$

Psi is a M-by-K matrix of regression coefficients and Sigma is a K-by-K scale matrix for multivariate t-distribution for noise.

Sampling distribution for noise e is the multivariate t-distribution with degree of freedom dof and scale matrix Sigma:  $e \sim mvt(0, dof, Sigma)$ . The priors are informative priors: 1) a shrinkage prior for regression coefficients Psi, and 2) inverse Wishart prior for scale matrix Sigma, which can be either non-conjugate ("NCJ") or conjugate ("CJ") to the shrinkage prior for coefficients Psi.

The function implements parameterized cross validation (PCV) for selecting a shrinkage parameter lambda for estimating regression coefficients ( $0 < \lambda \leq 1$ ). In addition, the function uses a Stein-type shrinkage method for selecting a shrinkage parameter lambda\_var for estimating variances of time series variables.

## References

N. Lee, H. Choi, and S.-H. Kim (2016). Bayes shrinkage estimation for high-dimensional VAR models with scale mixture of normal distributions for noise. *Computational Statistics & Data Analysis* 101, 250-276. doi: 10.1016/j.csda.2016.03.007

---

lm_ShVAR_KCV	<i>K-fold Cross Validation for Selection of Shrinkage Parameters of Semiparametric Bayesian Shrinkage Estimator for Multivariate Regression</i>
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---

## Description

Estimate regression coefficients and scale matrix for noise by using semiparametric Bayesian shrinkage estimator, whose shrinkage parameters are selected by K-fold cross validation (KCV).

## Usage

```
lm_ShVAR_KCV(Y, X, dof = Inf, lambda = NULL, lambda_var = NULL,
  prior_type = c("NCJ", "CJ"), num_folds = 5, m0 = ncol(Y))
```

## Arguments

Y	An N x K matrix of dependent variables.
X	An N x M matrix of regressors.
dof	Degree of freedom for multivariate t-distribution. If dof = Inf (default), then multivariate normal distribution is applied and weight vector q is not estimated. If dof = NULL or a numeric vector, then dof is selected by K-fold CV automatically and q is estimated.
lambda	If NULL or a vector of length $\geq 2$ , it is selected by KCV.
lambda_var	If NULL or a vector of length $\geq 2$ , it is selected by KCV.
prior_type	"NCJ" for non-conjugate prior and "CJ" for conjugate prior for scale matrix Sigma.
num_folds	Number of folds for KCV.
m0	A hyperparameter for inverse Wishart distribution for Sigma

## Details

The shrinkage parameters, lambda and lambda\_var, for the semiparametric Bayesian shrinkage estimator are selected by KCV. See `help(lm_semi_Bayes_PCV)` for details about semiparametric Bayesian estimator.

## References

N. Lee, H. Choi, and S.-H. Kim (2016). Bayes shrinkage estimation for high-dimensional VAR models with scale mixture of normal distributions for noise. *Computational Statistics & Data Analysis* 101, 250-276. doi: 10.1016/j.csda.2016.03.007

---

logLik.varshrinkest     *Log-likelihood method for class "varshrinkest"*

---

### Description

Returns the log-likelihood of a VAR model estimated by VARshrink(). It extends vars::logLik.varest() to incorporate 1) multivariate t-distribution for residuals, 2) scale matrix Sigma provided by shrinkage methods, and 3) effective number of parameters provided by shrinkage methods.

### Usage

```
## S3 method for class 'varshrinkest'
logLik(object, ...)
```

### Arguments

object	An object of class "varshrinkest"
...	Currently not used.

### Details

Acknowledgement: This code was contributed by Sung-Hoon Han & Dong-Han Lee @ Kangwon National University (2018.11.29.)

### Examples

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
logLik(estim)
```

---

normality.test\_sh     *Normality, multivariate skewness and kurtosis test*

---

### Description

This function computes univariate and multivariate Jarque-Bera tests and multivariate skewness and kurtosis tests for the residuals of a VAR(p) or of a VECM in levels. This is a modification of vars::normality.test() for the class "varshrinkest".

### Usage

```
normality.test_sh(x, multivariate.only = TRUE)
```

**Arguments**

`x` An object of class "varshrinkest" obtained by VARshrink().

`multivariate.only` If TRUE, only the multivariate statistics is computed.

**See Also**

[normality.test](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
normality.test_sh(estim)
```

---

Phi.varshrinkest	<i>Coefficient matrices of the MA representation</i>
------------------	--

---

**Description**

Returns the estimated coefficient matrices of the moving average representation of a stable VAR(p), of an SVAR as an array or a converted VECM to VAR. This is a modification of vars::Phi() for the class "varshrinkest".

**Usage**

```
## S3 method for class 'varshrinkest'
Phi(x, nstep = 10, ...)
```

**Arguments**

`x` An object of class 'varshrinkest', generated by VARshrink().

`nstep` An integer specifying the number of moving error coefficient matrices to be calculated.

`...` Currently not used.

**See Also**

[Phi](#)



---

predict.varshrinkest *Predict method for objects of class varshrinkest*

---

### Description

Forecasting a VAR object of class 'varshrinkest' with confidence bands. This is a modification of vars::predict.varest() for the class "varshrinkest".

### Usage

```
## S3 method for class 'varshrinkest'
predict(object, ..., n.ahead = 10, ci = 0.95,
        dumvar = NULL)
```

### Arguments

object	An object of class 'varshrinkest'; generated by VARshrink()
...	currently not used.
n.ahead	An integer specifying the number of forecast steps.
ci	The forecast confidence interval
dumvar	Matrix for objects of class 'vec2var' or 'varest', if the dumvar argument in ca.jo() has been used or if the exogen argument in VARshrink() has been used, respectively. The matrix should have the same column dimension as in the call to ca.jo() or to VARshrink() and row dimension equal to n.ahead.

---

print.varshrinkest *Print method for class "varshrinkest"*

---

### Description

Print method for an object of class "varshrinkest"

### Usage

```
## S3 method for class 'varshrinkest'
print(x, digits = max(3, getOption("digits") - 3),
      ...)
```

### Arguments

x	An object of class "varshrinkest"
digits, ...	Other arguments for print() method

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
print(estim)
```

---

```
print.varshsum          Print method for class "varshsum"
```

---

**Description**

Print method for an object obtained by `summary.varshrinkest()`.

**Usage**

```
## S3 method for class 'varshsum'
print(x, digits = max(3, getOption("digits") - 3),
      signif.stars = getOption("show.signif.stars"), ...)
```

**Arguments**

`x` An object of class "varshsum"  
`digits`, `signif.stars`, ... Other arguments for `print()`, `printCoefmat()`, `format()` method

**Details**

This function extends `print.varsum()` for VAR models estimated by shrinkage methods. The output includes scale matrix  $\Sigma$  and degree of freedom `dof` for multivariate t-distribution for residuals.

---

```
restrict_sh          Restricted VAR
```

---

**Description**

This is a modification of `vars::restrict()` for the class "varshrinkest". Warning: THIS CODE IS NOT COMPLETE: this function may raise an error because it ignores shrinkage estimation.

**Usage**

```
restrict_sh(x, ...)
```

**Arguments**

`x` An object of class "varshrinkest"  
 ... Other arguments to `vars::restrict()`

**See Also**[restrict](#)**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
restrict_sh(estim)
```

---

`roots_sh`*Eigenvalues of the companion coefficient matrix of a VAR(p)-process*

---

**Description**

This is a variant of `vars::roots()` for an object of class 'varshrinkest', VAR parameters estimated by `VARshrink()`.

**Usage**

```
roots_sh(x, modulus = TRUE)
```

**Arguments**

<code>x</code>	An object of class "varshrinkest"
<code>modulus</code>	TRUE for modulus of the roots.

**See Also**[roots](#)**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
roots_sh(estim)
```

---

serial.test_sh	<i>Test for serially correlated errors for VAR shrinkage estimate</i>
----------------	---

---

**Description**

An extension of vars::serial.test() to the class "varshrinkest".

**Usage**

```
serial.test_sh(x, lags.pt = 16, lags.bg = 5,
  type = c("PT.asymptotic", "PT.adjusted", "BG", "ES"))
```

**Arguments**

x                    An object of class "varshrinkest" obtained by VARshrink().  
lags.pt, lags.bg, type                    Other arguments for vars::serial.test(). see help(serial.test) for details.

**See Also**

[serial.test](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
serial.test_sh(estim)
```

---

shrinkVARcoef	<i>Semiparametric Bayesian Shrinkage Estimator for Multivariate Regression</i>
---------------	--

---

**Description**

Compute the semiparametric Bayesian shrinkage estimator of Psi and Sigma for a given shrinkage parameter lambda. The function is a private function for lm\_semi\_Bayes\_PCV() and lm\_ShVAR\_KCV().

**Usage**

```
shrinkVARcoef(Y, X, lambda, dof = Inf, prior_type = "NCJ",
  TolDRes = 1e-04, m0 = ncol(Y))
```

**Arguments**

Y	An N x K matrix of dependent variables.
X	An N x M matrix of regressors.
lambda	A shrinkage intensity parameter value between 0~1.
dof	Degree of freedom for multivariate t-distribution. If NULL or Inf, then use multivariate normal distribution.
prior_type	"NCJ" for non-conjugate prior and "CJ" for conjugate prior for scale matrix Sigma.
TolDRes	Tolerance parameter for stopping criterion.
m0	A hyperparameter for inverse Wishart distribution for Sigma

**References**

N. Lee, H. Choi, and S.-H. Kim (2016). Bayes shrinkage estimation for high-dimensional VAR models with scale mixture of normal distributions for noise. *Computational Statistics & Data Analysis* 101, 250-276. doi: 10.1016/j.csda.2016.03.007

---

 simVARmodel

---

*Generate multivariate time series data using the given VAR model*


---

**Description**

Generate a multivariate time series data set using the given VAR model.

**Usage**

```
simVARmodel(numT, model, burnin = 0)
```

**Arguments**

numT	Number of observed time points, T.
model	A list object with Coef, Sigma, dof; Coef is a list with A and c; A is a list object of K-by-K coefficient matrices and c is a length-K vector. Sigma is a K-by-K scale matrix and dof is a degree of freedom for multivariate t-distribution for noise.
burnin	Number of initial points which are not included in the final values.

**Details**

First, it creates (p+burnin+numT x K) data, then it remove the first (p+burnin) vectors. Finally, it returns (numT x K) data.

**Value**

A numT-by-K matrix

**Examples**

```
myCoef <- list(A = list(matrix(c(0.5, 0, 0, 0.5), 2, 2)), c = c(0.2, 0.7))
myModel <- list(Coef = myCoef, Sigma = diag(0.1^2, 2), dof = Inf)
simVARmodel(numT = 100, model = myModel, burnin = 10)
```

---

stability_sh	<i>Stability function</i>
--------------	---------------------------

---

**Description**

A variant of vars::stability(). Warning: this function has not been tested for small sample sizes yet.

**Usage**

```
stability_sh(x, type = c("OLS-CUSUM", "Rec-CUSUM", "Rec-MOSUM",
  "OLS-MOSUM", "RE", "ME", "Score-CUSUM", "Score-MOSUM", "fluctuation"),
  h = 0.15, dynamic = FALSE, rescale = TRUE, ...)
```

**Arguments**

x                    An object of class "varshrinkest"  
 type, h, dynamic, rescale, ...  
                     Other arguments to strucchange::efp()

**See Also**

[stability](#)

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
stability_sh(estim)
```

---

summary.shrinklm	<i>Summary method for class "shrinklm"</i>
------------------	--

---

**Description**

Class "shrinklm" inherits the class "lm", and it extends the "lm" class to incorporate shrinkage estimates with effective number of parameter.

**Usage**

```
## S3 method for class 'shrinklm'
summary(object, correlation = FALSE,
        symbolic.cor = FALSE, ...)
```

**Arguments**

object	An object of class "shrinklm"
correlation	If TRUE, the correlation matrix of the the estimated coefficients is returned and printed.
symbolic.cor	If TRUE, print the correlations in a symbolic form rather than as numbers
...	Currently not used.

---

summary.varshrinkest    *Summary method for an object of class 'varshrinkest', VAR parameters estimated by VARshrink()*

---

**Description**

Extend summary.varest() to class 'varshrinest' to incorporate adapted methods for new classes: summary.shrinklm(), logLik.varshrinkest(), roots.varshrinkest().

**Usage**

```
## S3 method for class 'varshrinkest'
summary(object, equations = NULL, ...)
```

**Arguments**

object	An object of class "varshrinkest", usually a result of call to "VARshrink()".
equations	Subset of names of endogenous time series variables to summarize.
...	Currently not used.

**Details**

Code is modified to avoid call to data matrices (\$y, \$datamat) and to use effective numbers of parameters of shrinkage estimates.

Output includes the scale matrix, Sigma, and degree-of-freedom, dof, for multivariate t-distribution for residuals.

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
estim <- VARshrink(y, p = 2, type = "const", method = "ridge")
summary(estim)
```

**Description**

Shrinkage estimation methods for high-dimensional VAR models. Consider VAR(p) model:  $y_t = A_1 y_{t-1} + \dots + A_p y_{t-p} + C d_t + e_t$ , where  $y_t$  is K-dimensional time series,  $d_t$  is deterministic regressors,  $e_t$  is a noise process, and  $A_1, \dots, A_p$ , and  $C$  are coefficient matrices. Exogenous variables can be included additionally as regressors.

**Usage**

```
VARshrink(y, p = 1, type = c("const", "trend", "both", "none"),
  season = NULL, exogen = NULL, method = c("ridge", "ns", "fbayes",
  "sbayes", "kcv"), lambda = NULL, lambda_var = NULL, dof = Inf, ...)
```

**Arguments**

<code>y</code>	A T-by-K matrix of endogenous variables
<code>p</code>	Integer for the lag order
<code>type</code>	Type of deterministic regressors to include. #' 1) "const" - the constant. 2) "trend" - the trend. 3) "both" - both the constant and the trend. 4) "none" - no deterministic regressors. ***Note: In the package version $\leq 0.3$ , <code>method='ns'</code> does not accept <code>type="const"</code> and <code>type="both"</code> to avoid constant term.
<code>season</code>	An integer value of frequency for inclusion of centered seasonal dummy variables. $\text{abs}(\text{season}) \geq 3$ .
<code>exogen</code>	A T-by-L matrix of exogenous variables. Default is NULL.
<code>method</code>	1) "ridge" - multivariate ridge regression. 2) "ns" - a Stein-type nonparametric shrinkage method. 3) "fbayes" - a full Bayesian shrinkage method using noninformative priors. 4) "sbayes" - a semiparametric Bayesian shrinkage method using parameterized cross validation. 5) "kcv" - a semiparametric Bayesian shrinkage method using K-fold cross validation
<code>lambda, lambda_var</code>	Shrinkage parameter value(s). Use of this parameter is slightly different for each method: the same value does not imply the same shrinkage estimates.
<code>dof</code>	Degree of freedom of multivariate t-distribution for noise. Valid only for <code>method = "fbayes"</code> and <code>method = "sbayes"</code> . <code>dof=Inf</code> means multivariate normal distribution.
<code>...</code>	Extra arguments to pass to a specific function of the estimation method. For example, <code>burnincycle</code> and <code>mcmccycle</code> are for "fbayes".

**Details**

Shrinkage estimation methods can estimate the coefficients even when the dimensionality  $K$  is larger than the number of observations.



**Value**

An object of class "varshrinkest" with the components: varresult, datamat, y, type, p, K, obs, totobs, restrictions, method, lambda, call. The class "varshrinkest" inherits the class "varest" in the package vars.

**Examples**

```
data(Canada, package = "vars")
y <- diff(Canada)
VARshrink(y, p = 2, type = "const", method = "ridge")
```

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