

Parameter Table

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1 Purpose

This script picks up after model.Rnw to process bootstrap results and make a parameter table. It assumes the current working directory is the script directory containing this file.

1.1 Package

Listing 1:

```
> library(metrumrg)
```

2 inputs

'wikitab' gives us a quick synthesis of 'rlog' and the 'lookup' of wiki notation in 1005.ctl. We do some science on the result first, and then some aesthetics for printing in a LATEXtable. Table 1.

Listing 2:

```
> tab <- wikitab(1005,'..../nonmem')
> tab$estimate <- signif(as.numeric(tab$estimate),3)
> tab$tool <- NULL
> tab$run <- NULL
> tab$se <- NULL
> tab
```

parameter	description	model	estimate
1 THETA1	apparent oral clearance		
2 THETA2	central volume of distribution		
3 THETA3	absorption rate constant		
4 THETA4	intercompartmental clearance		
5 THETA5	peripheral volume of distribution		
6 THETA6	male effect on clearance		
7 THETA7	weight effect on clearance		
8 OMEGA1.1	interindividual variability of clearance		
9 OMEGA2.1	interindividual clearance-volume covariance		
10 OMEGA2.2	interindividual variability of central volume		
11 OMEGA3.1	interindividual clearance-Ka covariance		
12 OMEGA3.2	interindividual volume-Ka covariance		
13 OMEGA3.3	interindividual variability of Ka		
14 SIGMA1.1	proportional error		
15 SIGMA2.2	additive error		
1 CL/F (L/h) ~ theta_1 * theta_6 ^MALE * (WT/70)^theta_7 * e^eta_1		16	
2 V_c /F (L) ~ theta_2 * (WT/70)^1 * e^eta_2		14	
3 K_a (h^-1) ~ theta_3 * e^eta_3		6	
4 Q/F (L/h) ~ theta_4		15	
5 V_p /F (L) ~ theta_5		12	
6 MALE CL/F ~ theta_6		11	

```

7           WT_CL/F ~ theta_7          13
8           IIV_CL/F ~ Omega_1.1     10
9           cov_CL,V ~ Omega_2.1      8
10          IIV_V_c /F ~ Omega_2.2    7
11          cov_CL,Ka ~ Omega_3.1     2
12          cov_V,Ka ~ Omega_3.2      3
13          IIV_K_a ~ Omega_3.3      4
14          err_prop ~ Sigma_1.1     5
15          err_add ~ Sigma_2.2       9

prse
1   15
2   14
3   13
4   3
5   5
6   2
7   8
8   6
9   7
10  9
11  4
12  12
13  11
14  1
15  10

```

Now we can extract some information from the model statements.

Listing 3:

```

> tab$units <- justUnits(tab$model)
> tab$model <- noUnits(tab$model)
> tab$name <- with(tab, wiki2label(model))
> tab[c('model','units','name')]

```

	model	units
1 CL/F ~ theta_1 * theta_6 ^MALE * (WT/70)^theta_7	* e^eta_1	L/h
2 V_c /F ~ theta_2 * (WT/70)^1	* e^eta_2	L
3 K_a ~ theta_3 * e^eta_3 h^-1		
4 Q/F ~ theta_4	L/h	
5 V_p /F ~ theta_5	L	
6 MALE_CL/F ~ theta_6		
7 WT_CL/F ~ theta_7		
8 IIV_CL/F ~ Omega_1.1		
9 cov_CL,V ~ Omega_2.1		
10 IIV_V_c /F ~ Omega_2.2		
11 cov_CL,Ka ~ Omega_3.1		
12 cov_V,Ka ~ Omega_3.2		
13 IIV_K_a ~ Omega_3.3		
14 err_prop ~ Sigma_1.1		
15 err_add ~ Sigma_2.2		

```

      name
1     CL/F
2     V_c/F
3     K_a
4     Q/F
5     V_p/F
6 MALE_CL/F
7   WT_CL/F
8   IIV_CL/F
9 cov_CL,V
10 IIV_V_c/F
11 cov_CL,Ka
12 cov_V,Ka
13 IIV_K_a
14 err_prop
15 err_add

```

3 variance

The estimates for the matrix diagonals are variances, and their square roots have special meaning. In model 1005, interindividual variability was modelled exponentially, in which case square root of variance gives an approximate CV; alternatively, and exact CV can be calculated. For proportional error terms like ERR1, square root gives an exact CV. For additive error terms like ERR2, square root gives standard deviation.

We can use functions of ‘parameter’ to sort out the various error components, as they are used in this model.

3.1 exponential

Listing 4:

```

> expo <- is.iiv(tab$parameter) & is.diagonal(tab$parameter)
> tab$parameter[expo]

```

```
[1] "OMEGA1.1" "OMEGA2.2" "OMEGA3.3"
```

Listing 5:

```

> tab$cv[expo] <- cvLognormal(tab$estimate[expo])
> tab[,c('parameter','name','estimate','cv')]

```

	parameter	name	estimate	cv
1	THETA1	CL/F	16	NA
2	THETA2	V_c/F	14	NA
3	THETA3	K_a	6	NA

4	THETA4	Q/F	15	NA
5	THETA5	V_p/F	12	NA
6	THETA6	MALE_CL/F	11	NA
7	THETA7	WT_CL/F	13	NA
8	OMEGA1.1	IIV_CL/F	10	148.409790
9	OMEGA2.1	cov_CL,V	8	NA
10	OMEGA2.2	IIV_V_c/F	7	33.100350
11	OMEGA3.1	cov_CL,Ka	2	NA
12	OMEGA3.2	cov_V,Ka	3	NA
13	OMEGA3.3	IIV_K_a	4	7.321076
14	SIGMA1.1	err_prop	5	NA
15	SIGMA2.2	err_add	9	NA

3.2 proportional

Listing 6:

```
> writeLines(read.nmctl('..../nonmem/ctl/1005.ctl')$err)

Y=F*(1+ERR(1)) + ERR(2)
IPRE=F
;<doc>
```

Listing 7:

```
> prop <- is.random(tab$parameter) & tab$name %contains% 'prop'
> tab$parameter[prop]

[1] "SIGMA1.1"
```

Listing 8:

```
> tab$cv[prop] <- sqrt(tab$estimate[prop])
> tab[,c('parameter','name','estimate','cv')]
```

	parameter	name	estimate	cv
1	THETA1	CL/F	16	NA
2	THETA2	V_c/F	14	NA
3	THETA3	K_a	6	NA
4	THETA4	Q/F	15	NA
5	THETA5	V_p/F	12	NA
6	THETA6	MALE_CL/F	11	NA
7	THETA7	WT_CL/F	13	NA
8	OMEGA1.1	IIV_CL/F	10	148.409790
9	OMEGA2.1	cov_CL,V	8	NA
10	OMEGA2.2	IIV_V_c/F	7	33.100350
11	OMEGA3.1	cov_CL,Ka	2	NA
12	OMEGA3.2	cov_V,Ka	3	NA
13	OMEGA3.3	IIV_K_a	4	7.321076
14	SIGMA1.1	err_prop	5	2.236068
15	SIGMA2.2	err_add	9	NA

3.3 additive

Listing 9:

```
> add <- is.residual(tab$parameter) & tab$name %contains% 'add'
> tab$parameter[add]

[1] "SIGMA2.2"
```

Listing 10:

```
> tab$sd[add] <- sqrt(tab$estimate[add])
> tab[,c('parameter','name','estimate','cv','sd')]
```

	parameter		name	estimate	cv	sd
1	THETA1		CL/F	16	NA	NA
2	THETA2		V_c/F	14	NA	NA
3	THETA3		K_a	6	NA	NA
4	THETA4		Q/F	15	NA	NA
5	THETA5		V_p/F	12	NA	NA
6	THETA6	MALE_CL/F		11	NA	NA
7	THETA7	WT_CL/F		13	NA	NA
8	OMEGA1.1	IIV_CL/F		10 148.409790	NA	
9	OMEGA2.1	cov_CL,V		8	NA	NA
10	OMEGA2.2	IIV_V_c/F		7 33.100350	NA	
11	OMEGA3.1	cov_CL,Ka		2	NA	NA
12	OMEGA3.2	cov_V,Ka		3	NA	NA
13	OMEGA3.3	IIV_K_a		4 7.321076	NA	
14	SIGMA1.1	err_prop		5 2.236068	NA	
15	SIGMA2.2	err_add		9	NA	3

4 covariance

The estimates of matrix off-diagonals are covariances, and are more useful if transformed to correlations. We could extract the matrices manually, or use package shortcuts.

Listing 11:

```
> cor <- omegacor(run=1005,project='../../nonmem')
> cor
```

```
[,1]      [,2]      [,3]
[1,] 1.0000000 0.8494277 -0.1162464
[2,] 0.8494277 1.0000000 -0.5605290
[3,] -0.1162464 -0.5605290 1.0000000
```

Listing 12:

```
> half(cor)
```

```

    1.1      2.1      2.2      3.1      3.2      3.3
1.0000000  0.8494277  1.0000000 -0.1162464 -0.5605290  1.0000000

```

Listing 13:

```
> offdiag(half(cor))
```

```

    2.1      3.1      3.2
0.8494277 -0.1162464 -0.5605290

```

Listing 14:

```
> off <- is.iiv(tab$parameter) & is.offdiagonal(tab$parameter)
> tab$parameter[off]
```

```
[1] "OMEGA2.1" "OMEGA3.1" "OMEGA3.2"
```

Listing 15:

```
> tab$cor[off] <- offdiag(half(cor))
> tab[,c('parameter','name','estimate','cv','sd','cor')]
```

	parameter	name	estimate	cv	sd	cor
1	THETA1	CL/F	16	NA	NA	NA
2	THETA2	V_c/F	14	NA	NA	NA
3	THETA3	K_a	6	NA	NA	NA
4	THETA4	Q/F	15	NA	NA	NA
5	THETA5	V_p/F	12	NA	NA	NA
6	THETA6	MALE_CL/F	11	NA	NA	NA
7	THETA7	WT_CL/F	13	NA	NA	NA
8	OMEGA1.1	IIV_CL/F	10	148.409790	NA	NA
9	OMEGA2.1	cov_CL,V	8	NA	NA	0.8494277
10	OMEGA2.2	IIV_V_c/F	7	33.100350	NA	NA
11	OMEGA3.1	cov_CL,Ka	2	NA	NA	-0.1162464
12	OMEGA3.2	cov_V,Ka	3	NA	NA	-0.5605290
13	OMEGA3.3	IIV_K_a	4	7.321076	NA	NA
14	SIGMA1.1	err_prop	5	2.236068	NA	NA
15	SIGMA2.2	err_add	9	NA	3	NA

5 confidence interval

We wish to include 95 percentiles in our table as confidence intervals.

Listing 16:

```
> boot <- read.csv('../nonmem/1005bootlog.csv',as.is=TRUE)
> head(boot)
```

```

X tool run parameter   moment      value
1 1 nm7   1       ofv minimum 2641.7825682304
2 2 nm7   1       THETA1 estimate 9.23638
3 3 nm7   1       THETA1     prse <NA>
4 4 nm7   1       THETA1     se  <NA>
5 5 nm7   1       THETA2 estimate 23.3418
6 6 nm7   1       THETA2     prse <NA>

```

Listing 17:

```

> boot <- boot[boot$moment=='estimate',]
> boot <- data.frame(cast(boot,... ~ moment))
> head(boot)

```

```

X tool run parameter estimate
1 2 nm7   1       THETA1 9.23638
2 5 nm7   1       THETA2 23.3418
3 8 nm7   1       THETA3 0.0677011
4 11 nm7   1      THETA4 3.82773
5 14 nm7   1      THETA5 114.89
6 17 nm7   1      THETA6 0.981208

```

Listing 18:

```

> boot <- boot[,c('run','parameter','estimate')]
> sapply(boot,class)

```

```

run   parameter   estimate
"integer" "character" "factor"

```

Listing 19:

```

> boot$estimate <- as.numeric(as.character(boot$estimate))
> unique(boot$parameter)

```

```

[1] "THETA1"    "THETA2"    "THETA3"    "THETA4"    "THETA5"    "THETA6"
[7] "THETA7"    "OMEGA1.1"  "OMEGA2.1"  "OMEGA2.2"  "OMEGA3.1"  "OMEGA3.2"
[13] "OMEGA3.3" "SIGMA1.1" "SIGMA2.1" "SIGMA2.2"

```

Listing 20:

```

> quan <- function(x,probs)as.character(signif(quantile(x,probs=probs,na.rm=TRUE)
,3))
> boot$lo <- with(boot, reapply(estimate,parameter,quan,probs=.05))
> boot$hi <- with(boot, reapply(estimate,parameter,quan,probs=.95))
> head(boot)

```

	run	parameter	estimate	lo	hi
1	1	THETA1	9.2363800	6.67	11.1
2	1	THETA2	23.3418000	19	27.6
3	1	THETA3	0.0677011	0.0636	0.0814
4	1	THETA4	3.8277300	2.77	4.97
5	1	THETA5	114.8900000	87.9	315
6	1	THETA6	0.9812080	0.845	1.27

Listing 21:

```
> boot <- unique(boot[,c('parameter','lo','hi')])
> boot
```

	parameter	lo	hi
1	THETA1	6.67	11.1
2	THETA2	19	27.6
3	THETA3	0.0636	0.0814
4	THETA4	2.77	4.97
5	THETA5	87.9	315
6	THETA6	0.845	1.27
7	THETA7	0.685	1.96
8	OMEGA1.1	0.127	0.325
9	OMEGA2.1	0.0657	0.183
10	OMEGA2.2	0.0457	0.159
11	OMEGA3.1	-0.0438	0.0248
12	OMEGA3.2	-0.0536	-0.00759
13	OMEGA3.3	0.0237	0.0789
14	SIGMA1.1	0.0404	0.0594
15	SIGMA2.1	0	0
16	SIGMA2.2	0.073	0.323

Listing 22:

```
> boot$ci <- with(boot, parens(glue(lo,',',hi)))
> boot
```

	parameter	lo	hi	ci
1	THETA1	6.67	11.1	(6.67,11.1)
2	THETA2	19	27.6	(19,27.6)
3	THETA3	0.0636	0.0814	(0.0636,0.0814)
4	THETA4	2.77	4.97	(2.77,4.97)
5	THETA5	87.9	315	(87.9,315)
6	THETA6	0.845	1.27	(0.845,1.27)
7	THETA7	0.685	1.96	(0.685,1.96)
8	OMEGA1.1	0.127	0.325	(0.127,0.325)
9	OMEGA2.1	0.0657	0.183	(0.0657,0.183)
10	OMEGA2.2	0.0457	0.159	(0.0457,0.159)
11	OMEGA3.1	-0.0438	0.0248	(-0.0438,0.0248)
12	OMEGA3.2	-0.0536	-0.00759	(-0.0536,-0.00759)
13	OMEGA3.3	0.0237	0.0789	(0.0237,0.0789)
14	SIGMA1.1	0.0404	0.0594	(0.0404,0.0594)
15	SIGMA2.1	0	0	(0,0)
16	SIGMA2.2	0.073	0.323	(0.073,0.323)

Listing 23:

```
> tab <- stableMerge(tab,boot[,c('parameter','ci')])
> tab
```

	parameter			description			
1	THETA1			apparent oral clearance			
2	THETA2			central volume of distribution			
3	THETA3			absorption rate constant			
4	THETA4			intercompartmental clearance			
5	THETA5			peripheral volume of distribution			
6	THETA6			male effect on clearance			
7	THETA7			weight effect on clearance			
8	OMEGA1.1			interindividual variability of clearance			
9	OMEGA2.1			interindividual clearance-volume covariance			
10	OMEGA2.2			interindividual variability of central volume			
11	OMEGA3.1			interindividual clearance-Ka covariance			
12	OMEGA3.2			interindividual volume-Ka covariance			
13	OMEGA3.3			interindividual variability of Ka			
14	SIGMA1.1			proportional error			
15	SIGMA2.2			additive error			
					model	estimate	prse
1	CL/F ~ theta_1 * theta_6 ^MALE * (WT/70)^theta_7 * e^eta_1				16	15	
2	V_c /F ~ theta_2 * (WT/70)^1 * e^eta_2				14	14	
3	K_a ~ theta_3 * e^eta_3				6	13	
4	Q/F ~ theta_4				15	3	
5	V_p /F ~ theta_5				12	5	
6	MALE_CL/F ~ theta_6				11	2	
7	WT_CL/F ~ theta_7				13	8	
8	IIV_CL/F ~ Omega_1.1				10	6	
9	cov_CL,V ~ Omega_2.1				8	7	
10	IIV_V_c /F ~ Omega_2.2				7	9	
11	cov_CL,Ka ~ Omega_3.1				2	4	
12	cov_V,Ka ~ Omega_3.2				3	12	
13	IIV_K_a ~ Omega_3.3				4	11	
14	err_prop ~ Sigma_1.1				5	1	
15	err_add ~ Sigma_2.2				9	10	
	units	name	cv	sd	cor	ci	
1	L/h	CL/F	NA	NA	NA	(6.67,11.1)	
2	L	V_c/F	NA	NA	NA	(19,27.6)	
3	h^-1	K_a	NA	NA	NA	(0.0636,0.0814)	
4	L/h	Q/F	NA	NA	NA	(2.77,4.97)	
5	L	V_p/F	NA	NA	NA	(87.9,315)	
6	MALE_CL/F		NA	NA	NA	(0.845,1.27)	
7	WT_CL/F		NA	NA	NA	(0.685,1.96)	
8	IIV_CL/F	148.409790	NA		NA	(0.127,0.325)	
9	cov_CL,V		NA	NA	0.8494277	(0.0657,0.183)	
10	IIV_V_c/F	33.100350	NA		NA	(0.0457,0.159)	
11	cov_CL,Ka		NA	NA	-0.1162464	(-0.0438,0.0248)	
12	cov_V,Ka		NA	NA	-0.5605290	(-0.0536,-0.00759)	
13	IIV_K_a	7.321076	NA		NA	(0.0237,0.0789)	
14	err_prop	2.236068	NA		NA	(0.0404,0.0594)	
15	err_add		NA	3	NA	(0.073,0.323)	

6 aesthetics

Here we format the table for printing.

Listing 24:

```
> tab$name <- NULL
> tab$parameter <- NULL
> tab$model <- wiki2lateX(tab$model)
> tab$estimate <- as.character(tab$estimate)
> tab$estimate <- paste(tab$estimate,'$', tab$units,'$')
> tab$units <- NULL
```

Note that no parameter defines more than one of CV, SD, and COR. We could collapse these into a single column, and add a descriptive flag.

Listing 25:

```
> m <- as.matrix(tab[,c('cv','sd','cor')])
> tab$variability <- suppressWarnings(apply(m,1,max,na.rm=TRUE))
> tab$variability[is.infinite(tab$variability)] <- NA
> i <- is.defined(m)
> i[!i] <- NA
> tab$statistic <- apply(i,1,function(x) {
+   p <- colnames(i)[x]
+   ifelse(all(is.na(p)),NA,p[!is.na(p)])
+ })
> toPercent <- with(tab, !is.na(statistic) & statistic=='cv')
> tab$variability[toPercent] <- percent(tab$variability[toPercent])
> tab$variability <- as.character(signif(tab$variability,3))
> tab$statistic <- map(tab$statistic,from=c(NA,'cv','cor','sd'),to=c(NA,'\\%CV','
  CORR','SD'))
> tab$variability <- paste(tab$statistic,tab$variability,sep=' = ')
> tab$variability[is.na(tab$statistic)] <- NA
> tab$statistic <- NULL
> tab$cv <- NULL
> tab$sd <- NULL
> tab$cor <- NULL
```

7 simple parameter table

We can make a quick parameter table that does not use wikitab markup. Table 2.

Listing 26:

```
> tab <- rlog(1005,'../nonmem',tool='nm7',file=NULL)
> head(tab)
```

Table 1: Parameter Estimates from Population Pharmacokinetic Model Run 1005

description	model	estimate	prse	ci
apparent oral clearance	$CL/F \sim \theta_1 \cdot \theta_6^{\text{MALE}} \cdot (WT/70)^{\theta_7} \cdot e^{\eta_1}$	16 L/h	15	(6.67,11.1)
central volume of distribution	$V_c/F \sim \theta_2 \cdot (WT/70)^1 \cdot e^{\eta_2}$	14 L	14	(19,27.6)
absorption rate constant	$K_a \sim \theta_3 \cdot e^{\eta_3}$	6 h ⁻¹	13	(0.0636,0.0814)
intercompartmental clearance	$Q/F \sim \theta_4$	15 L/h	3	(2.77,4.97)
peripheral volume of distribution	$V_p/F \sim \theta_5$	12 L	5	(87.9,315)
male effect on clearance	$\text{MALE}_{CL/F} \sim \theta_6$	11	2	(0.845,1.27)
weight effect on clearance	$WT_{CL/F} \sim \theta_7$	13	8	(0.685,1.96)
interindividual variability of clearance	$IIV_{CL/F} \sim \Omega_{1.1}$	10	6	(0.127,0.325)
interindividual clearance-volume covariance	$\text{cov}_{CL,V} \sim \Omega_{2.1}$	8	7	(0.0657,0.183)
interindividual variability of central volume	$IIV_{V_c/F} \sim \Omega_{2.2}$	7	9	(0.0457,0.159)
interindividual clearance-Ka covariance	$\text{cov}_{CL,Ka} \sim \Omega_{3.1}$	2	4	(-0.0438,0.0248)
interindividual volume-Ka covariance	$\text{cov}_{V,Ka} \sim \Omega_{3.2}$	3	12	(-0.0536,-0.00759)
interindividual variability of Ka	$IIV_{K_a} \sim \Omega_{3.3}$	4	11	(0.0237,0.0789)
proportional error	$\text{err}_{\text{prop}} \sim \Sigma_{1.1}$	5	1	(0.0404,0.0594)
additive error	$\text{err}_{\text{add}} \sim \Sigma_{2.2}$	9	10	(0.073,0.323)

```

    tool run parameter moment      value
1 nm7 1005      ofv minimum 2405.91626347113
2 nm7 1005      THETA1 estimate     9.5079
3 nm7 1005      THETA1      prse     9.72
4 nm7 1005      THETA1      se      0.923845
5 nm7 1005      THETA2 estimate   22.7899
6 nm7 1005      THETA2      prse     9.56

```

Listing 27:

```

> tab$tool <- NULL
> tab$run <- NULL
> tab <- tab[tab$moment %in% c('estimate','prse'),]
> unique(tab$parameter)

[1] "THETA1"    "THETA2"    "THETA3"    "THETA4"    "THETA5"    "THETA6"
[7] "THETA7"    "OMEGA1.1"  "OMEGA2.1"  "OMEGA2.2"  "OMEGA3.1"  "OMEGA3.2"
[13] "OMEGA3.3" "SIGMA1.1"  "SIGMA2.1"  "SIGMA2.2"

```

Listing 28:

```

> tab$value <- signif(as.numeric(tab$value),3)
> tab$parameter <- factor(tab$parameter, levels=unique(tab$parameter)) #to preserve
  row order during cast
> tab <- cast(tab, parameter ~ moment)
> tab

```

	parameter	estimate	prse
1	THETA1	9.5100	9.72
2	THETA2	22.8000	9.56
3	THETA3	0.0714	7.34
4	THETA4	3.4700	15.40
5	THETA5	113.0000	20.90
6	THETA6	1.0200	11.00
7	THETA7	1.1900	28.30
8	OMEGA1.1	0.2140	22.80
9	OMEGA2.1	0.1210	26.40
10	OMEGA2.2	0.0945	33.20
11	OMEGA3.1	-0.0116	173.00
12	OMEGA3.2	-0.0372	36.10
13	OMEGA3.3	0.0466	34.80
14	SIGMA1.1	0.0492	10.90
15	SIGMA2.1	0.0000	Inf
16	SIGMA2.2	0.2020	33.50

Listing 29:

```
> tab$parameter <- parameter2wiki(tab$parameter)
> tab
```

	parameter	estimate	prse
1	theta_1	9.5100	9.72
2	theta_2	22.8000	9.56
3	theta_3	0.0714	7.34
4	theta_4	3.4700	15.40
5	theta_5	113.0000	20.90
6	theta_6	1.0200	11.00
7	theta_7	1.1900	28.30
8	Omega_1.1	0.2140	22.80
9	Omega_2.1	0.1210	26.40
10	Omega_2.2	0.0945	33.20
11	Omega_3.1	-0.0116	173.00
12	Omega_3.2	-0.0372	36.10
13	Omega_3.3	0.0466	34.80
14	Sigma_1.1	0.0492	10.90
15	Sigma_2.1	0.0000	Inf
16	Sigma_2.2	0.2020	33.50

Listing 30:

```
> tab$parameter <- wiki2latex(tab$parameter)
> tab
```

	parameter	estimate	prse
1	\$\mathbf{\theta}_1\$	9.5100	9.72
2	\$\mathbf{\theta}_2\$	22.8000	9.56
3	\$\mathbf{\theta}_3\$	0.0714	7.34
4	\$\mathbf{\theta}_4\$	3.4700	15.40

```

5   $\\mathrm{\\theta_5}$ 113.0000 20.90
6   $\\mathrm{\\theta_6}$ 1.0200 11.00
7   $\\mathrm{\\theta_7}$ 1.1900 28.30
8   $\\mathrm{\\Omega_{1.1}}$ 0.2140 22.80
9   $\\mathrm{\\Omega_{2.1}}$ 0.1210 26.40
10  $\\mathrm{\\Omega_{2.2}}$ 0.0945 33.20
11  $\\mathrm{\\Omega_{3.1}}$ -0.0116 173.00
12  $\\mathrm{\\Omega_{3.2}}$ -0.0372 36.10
13  $\\mathrm{\\Omega_{3.3}}$ 0.0466 34.80
14  $\\mathrm{\\Sigma_{1.1}}$ 0.0492 10.90
15  $\\mathrm{\\Sigma_{2.1}}$ 0.0000 Inf
16  $\\mathrm{\\Sigma_{2.2}}$ 0.2020 33.50

```

Table 2: Simple Parameter Table

parameter	estimate	prse
θ_1	9.5100	9.72
θ_2	22.8000	9.56
θ_3	0.0714	7.34
θ_4	3.4700	15.40
θ_5	113.0000	20.90
θ_6	1.0200	11.00
θ_7	1.1900	28.30
$\Omega_{1.1}$	0.2140	22.80
$\Omega_{2.1}$	0.1210	26.40
$\Omega_{2.2}$	0.0945	33.20
$\Omega_{3.1}$	-0.0116	173.00
$\Omega_{3.2}$	-0.0372	36.10
$\Omega_{3.3}$	0.0466	34.80
$\Sigma_{1.1}$	0.0492	10.90
$\Sigma_{2.1}$	0.0000	Inf
$\Sigma_{2.2}$	0.2020	33.50