

# Package ‘FPDclustering’

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**Type** Package

**Title** PD-Clustering and Factor PD-Clustering

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**Description** Probabilistic distance clustering (PD-clustering) is an iterative, distribution free, probabilistic clustering method. PD-clustering assigns units to a cluster according to their probability of membership, under the constraint that the product of the probability and the distance of each point to any cluster centre is a constant. PD-clustering is a flexible method that can be used with non-spherical clusters, outliers, or noisy data. PDQ is an extension of the algorithm for clusters of different size. GPDC and TPDC uses a dissimilarity measure based on densities. Factor PD-clustering (FPDC) is a factor clustering method that involves a linear transformation of variables and a cluster optimizing the PD-clustering criterion. It works on high dimensional data sets.

**Depends** ThreeWay ,mvtnorm,R (>= 3.5)

**Imports** ExPosition,cluster,rootSolve, MASS, klaR, GGally, ggplot2

**License** GPL (>= 2)

**NeedsCompilation** no

**Repository** CRAN

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ais	<i>Australian institute of sport data</i>
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---

### Description

Data obtained to study sex, sport and body-size dependency of hematology in highly trained athletes.

### Usage

```
data(ais)
```

### Format

A data frame with 202 observations and 13 variable.

**rcc** red blood cell count, in

**wcc** while blood cell count, in per liter

**hc** hematocrit, percent

**hg** hemaglobin concentration, in g per decaliter

**ferr** plasma ferritins, ng

**bmi** Body mass index, kg

**ssf** sum of skin folds

**pcBfat** percent Body fat

**lbm** lean body mass, kg

**ht** height, cm

**wt** weight, kg

**sex** a factor with levels f m

**sport** a factor with levels B\_Ball Field Gym Netball Row Swim T\_400m T\_Sprnt Tennis W\_Polo

### Source

R package DAAG

**References**

Telford, R.D. and Cunningham, R.B. 1991. Sex, sport and body-size dependency of hematology in highly trained athletes. *Medicine and Science in Sports and Exercise* 23: 788-794.

**Examples**

```
data(ais)
pairs(ais[,1:11],col=ais$sex)
```

---

asymmetric20

*Asymmetric data set shape 20*

---

**Description**

Each cluster has been generated according to a multivariate asymmetric Gaussian distribution, with shape 20, covariance matrix equal to the identity matrix and randomly generated centres.

**Usage**

```
data(asymmetric20)
```

**Format**

A data frame with 800 observations on the following 101 variables. The first variable is the membership.

**Source**

Generated with R using the package *sn* (The skew-normal and skew-t distributions), function `rsn`

**Examples**

```
data(asymmetric20)
plot(asymmetric20[,2:3])
```

---

 asymmetric3

*Asymmetric data set shape 3*


---

### Description

Each cluster has been generated according to a multivariate asymmetric Gaussian distribution, with shape 3, covariance matrix equal to the identity matrix and randomly generated centres.

### Usage

```
data(asymmetric3)
```

### Format

A data frame with 800 observations on 101 variables. The first variable is the membership labels.

### Source

Generated with R using the package `sn` (The skew-normal and skew-t distributions), function `rsn`

### Examples

```
data(asymmetric3)
plot(asymmetric3[,2:3])
```

---

 FPDC

*Factor probabilistic distance clustering*


---

### Description

An implementation of FPDC, a probabilistic factor clustering algorithm that involves a linear transformation of variables and a cluster optimizing the PD-clustering criterion

### Usage

```
FPDC(data = NULL, k = 2, nf = 2, nu = 2)
```

### Arguments

<code>data</code>	A matrix or data frame such that rows correspond to observations and columns correspond to variables.
<code>k</code>	A numerical parameter giving the number of clusters
<code>nf</code>	A numerical parameter giving the number of factors for variables
<code>nu</code>	A numerical parameter giving the number of factors for units

**Value**

A class FPDclustering list with components

label	A vector of integers indicating the cluster membership for each unit
centers	A matrix of cluster centers
probability	A matrix of probability of each point belonging to each cluster
JDF	The value of the Joint distance function
iter	The number of iterations
explained	The explained variability
data	the data set

**Author(s)**

Cristina Tortora and Paul D. McNicholas

**References**

Tortora, C., M. Gettler Summa, M. Marino, and F. Palumbo. *Factor probabilistic distance clustering (fpdc): a new clustering method for high dimensional data sets*. *Advanced in Data Analysis and Classification*, 10(4), 441-464, 2016. doi:10.1007/s11634-015-0219-5.

Tortora C., Gettler Summa M., and Palumbo F.. *Factor pd-clustering*. In Lausen et al., editor, *Algorithms from and for Nature and Life, Studies in Classification, Data Analysis, and Knowledge Organization* DOI 10.1007/978-3-319-00035-011, 115-123, 2013.

Tortora C., *Non-hierarchical clustering methods on factorial subspaces*, 2012.

**See Also**

[PDC](#)

**Examples**

```
## Not run:
# Asymmetric data set clustering example (with shape 3).
data('asymmetric3')
x<-asymmetric3[,-1]

#Clustering
fpdas3=FPDC(x,4,3,3)

#Results
table(asymmetric3[,1],fpdas3$label)
Silh(fpdas3$probability)
summary(fpdas3)
plot(fpdas3)

## End(Not run)

## Not run:
```

```

# Asymmetric data set clustering example (with shape 20).
data('asymmetric20')
x<-asymmetric20[,-1]

#Clustering
fpdas20=FPDC(x,4,3,3)

#Results
table(asymmetric20[,1],fpdas20$label)
Silh(fpdas20$probability)
summary(fpdas20)
plot(fpdas20)

## End(Not run)

## Not run:
# Clustering example with outliers.
data('outliers')
x<-outliers[,-1]

#Clustering
fpdout=FPDC(x,4,5,4)

#Results
table(outliers[,1],fpdout$label)
Silh(fpdout$probability)
summary(fpdout)
plot(fpdout)

## End(Not run)

```

---

GPDC

*Gaussian PD-Clustering*


---

### Description

An implementation of Gaussian PD-Clustering GPDC, an extension of PD-clustering adjusted for cluster size that uses a dissimilarity measure based on the Gaussian density.

### Usage

```
GPDC(data=NULL,k=2,method="kmedoids", nr=5,iter=100)
```

### Arguments

data	A matrix or data frame such that rows correspond to observations and columns correspond to variables.
k	A numerical parameter giving the number of clusters

method	A parameter that selects center starts. Options available are random ("random"), kmedoid ("kmedoid", by default), and PDC ("PDclust").
nr	Number of random starts when method set to "random"
iter	Maximum number of iterations

**Value**

A class FPDclustering list with components

label	A vector of integers indicating the cluster membership for each unit
centers	A matrix of cluster means
sigma	A list of K elements, with the variance-covariance matrix per cluster
probability	A matrix of probability of each point belonging to each cluster
JDF	The value of the Joint distance function
iter	The number of iterations
data	the data set

**Author(s)**

Cristina Tortora and Francesco Palumbo

**References**

Tortora C., McNicholas P.D., and Palumbo F. *A probabilistic distance clustering algorithm using Gaussian and Student-t multivariate density distributions*. SN Computer Science, 1:65, 2020.

C. Rainey, C. Tortora and F.Palumbo. *A parametric version of probabilistic distance clustering*. In: Greselin F., Deldossi L., Bagnato L., Vichi M. (eds) *Statistical Learning of Complex Data. CLADAG 2017. Studies in Classification, Data Analysis, and Knowledge Organization*. Springer, Cham, 33-43 2019. doi.org/10.1007/978-3-030-21140-0\_4

**See Also**

[PDC, PDQ](#)

**Examples**

```
#Load the data
data(ais)
dataSEL=ais[,c(10,3,5,8)]

#Clustering
res=GPDC(dataSEL,k=2,method = "kmedoids")

#Results
table(res$label,ais$sex)
plot(res)
summary(res)
```

---

outliers

*Data set with outliers*

---

### Description

Each cluster has been generated according to a multivariate Gaussian distribution, with centers  $c$  randomly generated. For each cluster, 20% of uniform distributed outliers have been generated at a distance included in  $\max(x-c)$  and  $\max(x-c)+5$  from the center.

### Usage

```
data(outliers)
```

### Format

A data frame with 960 observations on the following 101 variables. The first variable corresponds to the membership

### Source

generated with R

### Examples

```
data(outliers)
plot(outliers[,2:3])
```

---

PDC

*Probabilistic Distance Clustering*

---

### Description

Probabilistic distance clustering (PD-clustering) is an iterative, distribution free, probabilistic clustering method. PD clustering is based on the constraint that the product of the probability and the distance of each point to any cluster centre is a constant.

### Usage

```
PDC(data = NULL, k = 2)
```

### Arguments

data	A matrix or data frame such that rows correspond to observations and columns correspond to variables.
k	A numerical parameter giving the number of clusters



**Value**

A class FPDclustering list with components

label	A vector of integers indicating the cluster membership for each unit
centers	A matrix of cluster centers
probability	A matrix of probability of each point belonging to each cluster
JDF	The value of the Joint distance function
iter	The number of iterations
data	the data set

**Author(s)**

Cristina Tortora and Paul D. McNicholas

**References**

Ben-Israel C. and Iyigun C. Probabilistic D-Clustering. *Journal of Classification*, **25**(1), 5-26, 2008.

**Examples**

```
#Normally generated clusters
c1 = c(+2,+2,2,2)
c2 = c(-2,-2,-2,-2)
c3 = c(-3,3,-3,3)
n=200
x1 = cbind(rnorm(n, c1[1]), rnorm(n, c1[2]), rnorm(n, c1[3]), rnorm(n, c1[4]) )
x2 = cbind(rnorm(n, c2[1]), rnorm(n, c2[2]),rnorm(n, c2[3]), rnorm(n, c2[4]) )
x3 = cbind(rnorm(n, c3[1]), rnorm(n, c3[2]),rnorm(n, c3[3]), rnorm(n, c3[4]) )
x = rbind(x1,x2,x3)

#Clustering
pdn=PDC(x,3)

#Results
plot(pdn)
```

**Description**

An implementation of probabilistic distance clustering adjusted for cluster size (PDQ), a probabilistic distance clustering algorithm that involves optimizing the PD-clustering criterion. The algorithm can be used, on continuous, count, or mixed type data setting Euclidean, Chi square, or Gower as dissimilarity measurements.

**Usage**

```
PDQ(x=NULL,k=2,ini='kmd',dist='euc',cent=NULL,ord=NULL,cat=NULL,bin=NULL,cont=NULL,w=NULL)
```

**Arguments**

x	A matrix or data frame such that rows correspond to observations and columns correspond to variables.
k	A numerical parameter giving the number of clusters.
ini	A parameter that selects center starts. Options available are random ("random"), kmedoid ("kmd", by default), center ("center", the user inputs the center), and kmode ("kmode", for categoriacal data sets).
dist	A parameter that selects the distance measure used. Options available are Euclidean ("euc"), Gower ("gower") and chi square ("chi").
cent	User inputed centers if method selected is "random".
ord	column indices of the x matrix indicating which columns are ordinal variables.
cat	column indices of the x matrix indicating which columns are categorical variables.
bin	column indices of the x matrix indicating which columns are binary variables.
cont	column indices of the x matrix indicating which columns are continuous variables.
w	numerical vector same length as the columns of the data, ccontaining the variable weights when using Gower distance, equal weights by default.

**Value**

A class FPDclustering list with components

label	A vector of integers indicating the cluster membership for each unit
centers	A matrix of cluster centers
probability	A matrix of probability of each point belonging to each cluster
JDF	The value of the Joint distance function
iter	The number of iterations
jdfvector	collection of all jdf calculations at each iteration
data	the data set

**Author(s)**

Cristina Tortora and Noe Vidales

**References**

Iyigun, Cem, and Adi Ben-Israel. *Probabilistic distance clustering adjusted for cluster size*. Probability in the Engineering and Informational Sciences 22.4 (2008): 603-621. doi.org/10.1017/S0269964808000351.

Tortora and Palumbo. *Clustering mixed-type data using a probabilistic distance algorithm*. submitted.

**See Also**[PDC](#)**Examples**

```

#Mixed type data

sig=matrix(0.7,4,4)
diag(sig)=1###creat a correlation matrix
x1=rmvnorm(200,c(0,0,3,3))## cluster 1
x2=rmvnorm(200,c(4,4,6,6),sigma=sig)## cluster 2
x=rbind(x1,x2)# data set with 2 clusters
l=c(rep(1,200),rep(2,200))#creating the labels
x1=cbind(x1,rbinom(200,4,0.2),rbinom(200,4,0.2))#categorical variables
x2=cbind(x2,rbinom(200,4,0.7),rbinom(200,4,0.7))
x=rbind(x1,x2) ##Data set

#### Performing PDQ
pdq_class<-PDQ(x=x,k=2, ini="random", dist="gower", cont= 1:4, cat = 5:6)

###Output
table(1,pdq_class$label)
plot(pdq_class)
summary(pdq_class)

###Continuous data example
# Gaussian Generated Data no overlap
x<-rmvnorm(100, mean=c(1,5,10), sigma=diag(1,3))
y<-rmvnorm(100, mean=c(4,8,13), sigma=diag(1,3))
data<-rbind(x,y)

#### Performing PDQ
pdq1=PDQ(data,2,ini="random",dist="euc")
table(rep(c(2,1),each=100),pdq1$label)
Silh(pdq1$probability)
plot(pdq1)
summary(pdq1)

# Gaussian Generated Data with overlap
x2<-rmvnorm(100, mean=c(1,5,10), sigma=diag(1,3))
y2<-rmvnorm(100, mean=c(2,6,11), sigma=diag(1,3))
data2<-rbind(x2,y2)

#### Performing PDQ
pdq2=PDQ(data2,2,ini="random",dist="euc")
table(rep(c(1,2),each=100),pdq2$label)
plot(pdq2)
summary(pdq2)

```

---

plot.FPDclustering      *Plots for FPDclusteringt Objects*

---

### Description

Probability Silhouette plot, Scatterplot up to 10 variables, and parallel coordinate plot up to 10 variables, for objects of class FPDclustering.

### Usage

```
## S3 method for class 'FPDclustering'
plot(x, maxVar=30, ... )
```

### Arguments

x	an object of class FPDclustering
maxVar	a scalar indicating the maximum number of variables to display on the parallel plot, 30 by default
...	Additional parameters for the function paris

### Author(s)

Cristina Tortora

---

Silh      *Probabilistic silhouette plot*

---

### Description

Graphical tool to evaluate the clustering partition.

### Usage

```
Silh(p)
```

### Arguments

p	A matrix of probabilities such that rows correspond to observations and columns correspond to clusters.
---	---

**Details**

The probabilistic silhouettes are an adaptation of the ones proposed by Menardi(2011) according to the following formula:

$$dbs_i = (\log(p_{im_k}/p_{im_1}))/\max_i|\log(p_{im_k}/p_{im_1})|$$

,  
where  $m_k$  is such that  $x_i$  belongs to cluster  $k$  and  $m_1$  is such that  $p_{im_1}$  is maximum for  $m$  different from  $m_k$ .

**Value**

Probabilistic silhouette plot

**Author(s)**

Cristina Tortora

**References**

Menardi G. Density-based Silhouette diagnostics for clustering methods.*Statistics and Computing*, **21**, 295-308, 2011.

**Examples**

```
## Not run:
# Asymmetric data set silhouette example (with shape=3).
data('asymmetric3')
x<-asymmetric3[,-1]
fpdas3=FPDC(x,4,3,3)
Silh(fpdas3$probability)

## End(Not run)

## Not run:
# Asymmetric data set silhouette example (with shape=20).
data('asymmetric20')
x<-asymmetric20[,-1]
fpdas20=FPDC(x,4,3,3)
Silh(fpdas20$probability)

## End(Not run)

## Not run:
# Silhouette example with outliers.
data('outliers')
x<-outliers[,-1]
fpdout=FPDC(x,4,4,3)
Silh(fpdout$probability)

## End(Not run)
```

---

Star *Star dataset to predict star types*

---

**Description**

A 6 class star dataset for star classification with Deep Learned approaches

**Usage**

```
data(ais)
```

**Format**

A data frame with 202 observations and 13 variable.

**K** Absolute Temperature (in K)

**Lum** Relative Luminosity (L/Lo)

**Rad** Relative Radius (R/Ro)

**Mag** Absolute Magnitude (Mv)

**Col** Star Color (white,Red,Blue, Yellow,yellow-orange etc)

**Spect** Spectral Class (O,B,A,F,G,K,,M)

**Type** Star Type (Red Dwarf, Brown Dwarf, White Dwarf, Main Sequence , SuperGiants, Hyper-Giants)

**Source**

<https://www.kaggle.com/deepu1109/star-dataset>

**Examples**

```
data(Star)
```

---

summary.FPDclustering *Summary for FPDclusteringt Objects*

---

**Description**

Number of elements per cluster.

**Usage**

```
## S3 method for class 'FPDclustering'  
summary(object, ... )
```

**Arguments**

object            an object of class FPDclustering  
 ...              Additional parameters for the function paris

**Author(s)**

Cristina Tortora

---

TPDC                                  *Student-t PD-Clustering*

---

**Description**

An implementation of Student-t PD-Clustering TPDC, an extension of PD-clustering adjusted for cluster size that uses a dissimilarity measure based on the multivariate Student-t density.

**Usage**

```
TPDC(data=NULL,k=2,method="kmedoids", nr=5,iter=100)
```

**Arguments**

data              A matrix or data frame such that rows correspond to observations and columns correspond to variables.

k                  A numerical parameter giving the number of clusters

method            A parameter that selects center starts. Options available are random ("random"), kmedoid ("kmedoid", by default), and PDC ("PDclust").

nr                Number of random starts if method is "random"

iter              Maximum number of iterations

**Value**

A class FPDclustering list with components

label            A vector of integers indicating the cluster membership for each unit

centers          A matrix of cluster means

sigma            A list of K elements, with the variance-covariance matrix per cluster

df                A vector of K degrees of freedom

probability      A matrix of probability of each point belonging to each cluster

JDF              The value of the Joint distance function

iter             The number of iterations

data             the data set

**Author(s)**

Cristina Tortora and Francesco Palumbo

**References**

Tortora C., McNicholas P.D., and Palumbo F. *A probabilistic distance clustering algorithm using Gaussian and Student-t multivariate density distributions*. SN Computer Science, 1:65, 2020.

C. Rainey, C. Tortora and F.Palumbo. *A parametric version of probabilistic distance clustering*. In: Greselin F., Deldossi L., Bagnato L., Vichi M. (eds) *Statistical Learning of Complex Data. CLADAG 2017. Studies in Classification, Data Analysis, and Knowledge Organization*. Springer, Cham, 33-43 2019. doi.org/10.1007/978-3-030-21140-0\_4

**See Also**

[PDC](#), [PDQ](#)

**Examples**

```
#Load the data
data(ais)
dataSEL=ais[,c(10,3,5,8)]

#Clustering
res=TPDC(dataSEL,k=2,method = "kmedoids")

#Results
table(res$label,ais$sex)
summary(res)
plot(res)
```

---

TuckerFactors

*Choice of the number of Tucker 3 factors for FPDC*

---

**Description**

An empirical way of choosing the number of factors for FPDC. The function returns a graph and a table representing the explained variability varying the number of factors.

**Usage**

```
TuckerFactors(data = NULL, nc = 2)
```

**Arguments**

data	A matrix or data frame such that rows correspond to observations and columns correspond to variables.
nc	A numerical parameter giving the number of clusters



**Value**

A table containing the explained variability varying the number of factors for units (column) and for variables (row) and the corresponding plot

**Author(s)**

Cristina Tortora

**References**

Kiers H, Kinderen A. A fast method for choosing the numbers of components in Tucker3 analysis. *British Journal of Mathematical and Statistical Psychology*, **56**(1), 119-125, 2003.

Kroonenberg P. *Applied Multiway Data Analysis*. Ebooks Corporation, Hoboken, New Jersey, 2008.

Tortora C., Gettler Summa M., and Palumbo F.. Factor pd-clustering. In Lausen et al., editor, *Algorithms from and for Nature and Life, Studies in Classification, Data Analysis, and Knowledge Organization* DOI 10.1007/978-3-319-00035-011, 115-123, 2013.

**See Also**

[T3](#)

**Examples**

```
## Not run:  
# Asymmetric data set example (with shape=3).  
data('asymmetric3')  
xp=TuckerFactors(asymmetric3[,-1], nc = 4)
```

```
## End(Not run)
```

```
## Not run:  
# Asymmetric data set example (with shape=20).  
data('asymmetric20')  
xp=TuckerFactors(asymmetric20[,-1], nc = 4)
```

```
## End(Not run)
```

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