## Package 'fBasics'

November 3, 2023
Title Rmetrics - Markets and Basic Statistics
Version 4032.96
Description Provides a collection of functions to
explore and to investigate basic properties of financial returns and related quantities.
The covered fields include techniques of explorative data analysis and the investigation of distributional properties, including parameter estimation and hypothesis testing. Even more there are several utility functions for data handling and management.

Depends R (>=2.15.1)
Imports timeDate, timeSeries (>= 4021.105), stats, grDevices, graphics, methods, utils, MASS, spatial, gss, stabledist
Suggests interp, RUnit, tcltk
LazyData yes
License GPL (>=2)

## Encoding UTF-8

URL https://geobosh.github.io/fBasicsDoc/(doc),
https://r-forge.r-project.org/scm/viewvc.php/pkg/fBasics/?root=rmetrics (devel), https://www.rmetrics.org

BugReports https://r-forge.r-project.org/projects/rmetrics
NeedsCompilation yes
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Repository CRAN
Date/Publication 2023-11-03 16:10:02 UTC

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fBasics-package Portfolio modelling, optimization and backtesting

## Description

The Rmetrics fBasics package is a collection of functions to explore and to investigate basic properties of financial returns and related quantities.
The covered fields include techniques of explorative data analysis and the investigation of distributional properties, including parameter estimation and hypothesis testing. Evenmore there are several utility functions for data handling and managemnet.

## 1 Introduction

The fBasics package contains basics tools often required in computational finance and financial engineering. The topics are: basic statistics functions, financial return distributions, hypothesis testing, plotting routines, matrix computations and linear algebra, and some usefule utility functions.

## 2 Basic Statistics Functions

Financial Return Statistics

```
basicStats Returns a basic statistics summary
```

Distribution Function of Maximum Drawdowns

| dmaxdd | Density function of mean Max-Drawdowns |
| :--- | :--- |
| pmaxdd | Probability function of mean Max-Drawdowns |
| rmaxdd | Random Variates of mean Max-Drawdowns |
| maxddStats | Expectation of Drawdowns for BM with drift |

## Calculation of Sample Moments

```
sampleLmoments Computes sample L-moments
sampleMED Returns sample median
sampleIQR returns sample inter quartal range
sampleSKEW returns robust sample skewness
sampleKURT returns robust sample kurtosis
```


## Bivariate Interpolation:

```
akimaInterp Interpolates irregularly spaced points
akimaInterpp Interpolates and smoothes pointwise
krigeInterp Kriges irregularly spaced data points
linearInterp Interpolates irregularly spaced points
linearInterpp Interpolates linearly pointwise
```

Utility Statistics Functions:

```
colSds
colVars
colSkewness
colKurtosis
colMaxs
colMins
colProds
colQuantiles
```

colStats Computes sample statistics by col
colSums Computes sums of values in each col
colMeans Computes means of values in each col
Computes standard deviation of each col
Computes sample variance by col
Computes sample skewness by col
Computes sample kurtosis by col
Computes maximum values in each col
Computes minimum values in each col
Computes product of values in each col
Computes product of values in each col

| rowStats | Computes sample statistics by row |
| :--- | :--- |
| rowSums | Computes sums of values in each row |
| rowMeans | Computes means of values in each row |
| rowSds | Computes standard deviation of each row |
| rowVars | Computes sample variance by row |
| rowSkewness | Computes sample skewness by row |
| rowKurtosis | Computes sample kurtosis by row |
| rowMaxs | Computes maximum values in each row |
| rowMins | Computes minimum values in each row |
| rowProds | Computes product of values in each row |
| rowQuantiles | Computes product of values in each row |

## 3 Financial Return Distributions

Generalized Hyperbolic Distribution:

| dghReturns | Density for the GH distribution |
| :--- | :--- |
| pghreturns | Probability for the GH distribution |
| qghreturns | Quantiles for the GH distribution |
| rghreturns | Random variates for the GH distribution |
| ghFitFits | Fits parameters of the GH distribution |
| ghMode | Computes mode of the GH distribution. |
| ghMean | Returns true mean of the GH distribution |
| ghVar | Returns true variance of the GH distribution |
| ghSkew | Returns true skewness of the GH distribution |

```
ghKurt Returns true kurtosis of the GH distribution
ghMoments
ghMED
ghIQR
ghSKEW
ghKURT
Returns true kurtosis of the GH distribution Returns true n-th moment of the GH distribution Returns true median of te GH distribution Returns true inter quartal range of te GH Returns true robust skewness of te GH Returns true robust kurtosis of te GH
```


## Hyperbolic Distribution:

| dhyp | Returns density for the HYP distribution |
| :--- | :--- |
| phyp | Returns probability for the HYP distribution |
| qhyp | Returns quantiles for the HYP distribution |
| rhyp | Returns random variates for the HYP distribution |
| hypFit | Fits parameters of the HYP distribution |
| hypMode | Computes mode of the HYP distribution |
| hypMean | Returns true mean of the HYP distribution |
| hypVar R | Returns true variance of the HYP distribution |
| hypSkew | Returns true skewness of the HYP distribution |
| hypKurt | Returns true kurtosis of the HYP distribution |
| hypMoments | Returns true n-th moment of the HYP distribution |
| hypMED | Returns true median of the HYP distribution |
| hypIQR | Returns true inter quartal range of the HYP |
| hypSKEW | Returns true robust skewness of the HYP |
| hypKURT | Returns true robust kurtosis of the HYP |

## Normal Inverse Gaussian:

| dnig | Returns density for the NIG distribution |
| :--- | :--- |
| pnig | Returns probability for the NIG distribution |
| qnig | Returns quantiles for the NIG distribution |
| rnig | Returns random variates for the NIG distribution |
| .pnigC | fast C Implementation of function pnig() |
| nigFit | fast CImplementation of function qnig() |
| .nigFit.mle | Fits parameters of a NIG distribution |
| .nigFit.gmm | Uses max Log-likelihood estimation |
| .nigFit.mps | Uses generalized method of moments |
| .nigFit.vmps | Maximum product spacings estimation |
| nigMode | Minimum variance mps estimation |
| nigMean | Computes mode of the NIG distribution |
| nigVar | Returns true mean of the NIG distribution |
| nigSkew | Returns true variance of the NIG distribution |
| nigKurt | Returns true skewness of the NIG distribution |
| nigMoments | Returns true kurtosis of the NIG distribution |
| nigMED | Returns true n-th moment of the NIG distribution |
| nigIQR | Returns true median of the NIG distribution |

```
nigSKEW Returns true robust skewness of the NIG
nigKURT Returns true robust kurtosis of the NIG
```

Generalized Hyperbolic Student-t Distribution:

| dght | Returns density for the GHT distribution |
| :--- | :--- |
| pght | Returns probability for the GHT distribution |
| qght | Returns quantiles for the GHT distribution |
| rght | Returns random variates for the GHT distribution |
| ghtFit | Fits parameters of the GHT distribution |
| ghtMode | Computes mode of the GHT distribution |
| ghtMean | Returns true mean of the NIG distribution |
| ghtVar | Returns true variance of the GHT distribution |
| ghtSkew | Returns true skewness of the GHT distribution |
| ghtKurt | Returns true kurtosis of the GHT distribution |
| ghtMoments | Returns true n-th moment of the GHT distribution |
| ghtMED | Returns true median of the GHT distribution |
| ghtIQR | Returns true inter quartal range of the GHT |
| ghtSKEW | Returns true robust skewness of the GHT |
| ghtKURT | Returns true robust kurtosis of the GHT |

## Stable Distribution:

```
dstable
pstable
qstable
rstable
stableFit
    .phiStable
    .PhiStable
    .qStableFit
    .mleStableFit
    .stablePlot
stableMode
```

Returns density for the stable distribution Returns probability for the stable distribution Returns quantiles for the stable distribution Returns random variates for the dtsble distribution Fits parameters of a the stable distribution Creates contour table for McCulloch estimators Contour table created by function .phiStable() Estimates parameters by McCulloch's approach Estimates stable parameters by MLE approach Plots results of stable parameter estimates Computes mode of the stable distribution

Generalized Lambda Distribution:

| dgld | Returns density for the GLD distribution |
| :--- | :--- |
| pgld | Returns probability for the GLD distribution |
| qgld | Returns quantiles for the GLD distribution |
| rgld | Returns random variates for the GLD distribution |
| gldFit | Fits parameters of the GLD distribution |
| .gldFit.mle | fits GLD using maximum log-likelihood |
| .gldFit.mps | fits GLD using maximum product spacings |
| .gldFit.gof | fits GLD using Goodness of Fit statistics |

```
    .gldFit.hist
    .gldFit.rob
gldMode
gldMED
gldIQR
gldSKEW
gldKURT
```

fits GLD using a histogram fit
fits GLD using robust moments fit
Computes mode of the GLD distribution.
Returns true median of the GLD distribution
Returns true inter quartal range of the GLD
Returns true robust skewness of the GLD
Returns true robust kurtosis of the GLD

Spline Smoothed Distribution:

```
dssd Returns spline smoothed density function
pssd Returns spline smoothed probability function
qssd Returns spline smoothed quantile function
rssd Returns spline smoothed random variates.
ssdFit Fits parameters for a spline smoothed distribution
```


## 4 Hypthesis Testing

One Sample Nornality Tests:

| ksnormTest | One sample Kolmogorov-Smirnov normality test |
| :--- | :--- |
| shapiroTest | Shapiro-Wilk normality test |
| jarqueberaTest | Jarque-Bera normality test |
| normalTest | Normality tests S-Plus compatible call |
| dagoTest | D'Agostino normality test |
| adTest | Anderson-Darling normality test |
| cvmTest | Cramer-von Mises normality test |
| lillieTest | Lilliefors (KS) normality test |
| pchiTest | Pearson chi-square normality test |
| sfTest | Shapiro-Francia normality test |
| jbTest | Finite sample adjusted JB LM and ALM test |

One Sample Location, Scale and variance Tests:

```
locationTest Performs locations tests on two samples
    .tTest
    .kw2Test
scaleTest
    .ansariTest
    .moodTest
varianceTest
    .varfTest
    Unpaired t test for differences in mean
    Kruskal-Wallis test for differences in locations
    Performs scale tests on two samples
    Ansari-Bradley test for differences in scale
    Mood test for differences in scale
    Performs variance tests on two samples
    F test for differences in variances
```

```
.bartlett2Test Bartlett's test for differences in variances
.fligner2Test Fligner-Killeen test for differences in variances
```

Two Sample Tests:

| ks2Test | Performs a two sample Kolmogorov-Smirnov test |
| :--- | :--- |
| correlationTest | Performs correlation tests on two samples |
| pearsonTest | Pearson product moment correlation coefficient |
| kendallTest | Kendall's tau correlation test |
| spearmanTest | Spearman's rho correlation test |

Test Utilities:

| 'fHTEST' | S4 Class Representation |
| :--- | :--- |
| show.fHTEST | S4 Print Method |
| .jbALM | Jarque Bera Augmented Lagrange Multiplier Data |
| .jbLM | Jarque-Bera Lagrange Multiplier Data |
| .jbTable | Finite sample p values for the Jarque Bera test |
| .jbPlot | Plots probabilities |
| .pjb | Returns probabilities for JB given quantiles |
| .qjb | Returns quantiles for JB given probabilities |

## 5 Plotting Routines

Financial Time Series Plots:

```
seriesPlot Dispalys a time series plot
cumulatedPlot Displays cumulated series give returns
returnPlot
drawdownPlot
Displays returns given cumulated series
Displays drawdown series from returns
```

Correlation Plots:

```
acfPlot Displays tailored ACF plot
pacfPlot
teffectPlot
lacfPlot
```


## Distribution Plots:

| histPlot | Returns tailored histogram plot |
| :--- | :--- |
| densityPlot | Returns tailored density plot |
| logDensityPlot | Returns tailored log density plot |


| boxPlot | Returns side-by-side standard box plot |
| :--- | :--- |
| boxPercentile | Plotreturns box-percentile plot |
| qqnormPlot | Returns normal quantile-quantile plot |
| qqnigPlot | Returns NIG quantile-quantile plot |
| qqghtPlot | Rreturns GHT quantile-quantile plot |
| qqgldPlot | Returns GLD quantile-quantile plot |

Time Series Aggregation Plots:

```
scalinglawPlot Displays scaling law behavior
```


## 5. Matrix Computations and Linear Algebra

Elementar Matrix Operation Addons:

```
kron Returns the Kronecker product
vec Stacks a matrix as column vector
vech Stacks a lower triangle matrix
pdl
tslag
Returns regressor matrix for polynomial lags
Returns Lagged/leading vector/matrix
```


## Linear Algebra Addons:

| inv | Returns the inverse of a matrix |
| :--- | :--- |
| norm | Returns the norm of a matrix |
| rk | Returns the rank of a matrix |
| tr | Returns the trace of a matrix |

General Matrix Utility Addons:

```
isPositiveDefinite Checks if a matrix is positive definite
makePositiveDefinite Forces a matrix to be positive definite
colVec Creates a column vector from a data vector
rowVec Creates a row vector from a data vector
gridVector Creates from two vectors rectangular grid
triang Extracs lower tridiagonal part from a matrix
Triang Extracs upper tridiagonal part from a matrix
```


## Selected Matrix Examples:

| hilbert | Creates a Hilbert matrix |
| :--- | :--- |
| pascal | Creates a Pascal matrix |

## 6 Utility Functions

Color Utilities:

```
colorLocator
colorMatrix
colorTable
rainbowPalette
heatPalette
terrainPalette
topoPalette
cmPalette
greyPalette
timPalette
rampPalette
seqPalette
divPalette
qualiPalette
focusPalette
monoPalette
```


## Graphics Utilities:

```
symbolTable
characterTable
decor
hgrid
vgrid
boxL
box
    .xrug
        .yrug
copyright
interactivePlot
```

```
```

Shows a table of plot symbols

```
```

Shows a table of plot symbols
Shows a table of character codes
Shows a table of character codes
Adds horizontal grid and L shaped box
Adds horizontal grid and L shaped box
Adds horizontal grid lines
Adds horizontal grid lines
Adds vertical grid lines
Adds vertical grid lines
Adds L-shaped box
Adds L-shaped box
Adds unterlined box
Adds unterlined box
Adds rugs on x axis
Adds rugs on x axis
Adds rugs on y axis
Adds rugs on y axis
Adds copyright notice
Adds copyright notice
Plots several graphs interactively

```
```

Plots several graphs interactively

```
```

Special Function Utilities:

| Heaviside | Computes Heaviside unit step function |
| :--- | :--- |
| Sign | Another signum function |
| Delta | Computes delta function |
| Boxcar | Computes boxcar function |
| Ramp | Computes ramp function |
| tsHessian | Computes Two Sided Hessian matrix |

Other Utilities:

```
Plots Rs 657 named colors for selection
Returns matrix of R's color names.
Table of Color Codes and Plot Colors itself
Contiguous rainbow color palette
Contiguous heat color palette
Contiguous terrain color palette
Contiguous topo color palette
Contiguous cm color palette
R's gamma-corrected gray palette
Tim's Matlab like color palette
Color ramp palettes
Sequential color brewer palettes
Diverging color brewer palettes
Qualified color brewer palettes
Red, green blue focus palettes
Red, green blue mono palettes
```

```
.unirootNA Computes zero of a function without error exit
getModel Extracts the model slot from a S4 object
getTitle Extracts the title slot from a S4 object
getDescription Extracts the description slot
getSlot Extracts a specified slot from a S4 object
```


## About Builtin Functions

Builtin functions are borrowed from contributed R packages and other sources. There are several reasons why we have modified and copied code from other sources and included in this package.

* The builtin code is not available on Debian, so that Linux users have no easy acces to this code.
* The original code conflicts with other code from this package or conflicts with Rmetrics design objectives.
* We only need a very small piece of functionality from the original package which may depend on other packages which are not needed.
* The package from which we builtin the code is under current development, so that the functions often change and thus leads to unexpectect behavior in the Rmetrics packages.
* The package may be incompatible since it uses other time date and time series classes than the 'timeDate' and 'timeSeries' objects and methods from Rmetrics.
We put the code in script files named builtin-funPackage. $R$ where "fun" denotes the (optional) major function name, and "Package" the name of the contributed package from which we copied the original code.

Builtin functions include:

| gelGmm | gll function from gmm package |
| :--- | :--- |
| gmmGMM | gmm function from gmm package |
| kweightsSandwhich | kweights from sandwhich package |
| glGld | gl functions from gld package |
| ssdenGss | ssden from the gss package |
| hypHyperbolicDist | hyp from HyperbolicDist package |

## Compiled Fortran and C Code:

```
gld.c
nig.c
gss.f
```

```
source code from gld package
```

source code from gld package
source code from Kersti Aas
source code from Kersti Aas
source code fromsandwhich package

```
source code fromsandwhich package
```


## About Rmetrics:

The fBasics Rmetrics package is written for educational support in teaching "Computational Finance and Financial Engineering" and licensed under the GPL.

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```
acfPlot Autocorrelation function plots
```


## Description

Returns plots of autocorrelations including the autocorrelation function ACF, the partial ACF, the lagged ACF, and the Taylor effect plot.

The functions to display stylized facts are:

| acfPlot | autocorrelation function plot, |
| :--- | :--- |
| pacfPlot | partial autocorrelation function plot, |
| lacfPlot | lagged autocorrelation function plot, |
| teffectPlot | Taylor effect plot. |

## Usage

```
acfPlot (x, labels = TRUE, ...)
pacfPlot (x, labels = TRUE, ....)
    lacfPlot(x, n = 12, lag.max = 20, type = c("returns", "values"),
        labels = TRUE, ...)
    teffectPlot(x, deltas \(=\) seq(from \(=0.2\), to \(=3\), by \(=0.2\) ), lag.max = 10,
        ymax = NA, standardize = TRUE, labels = TRUE, ...)
```


## Arguments

labels a logical value. Whether or not $x$ - and $y$-axes should be automatically labeled
x
n
lag.max
type
an uni- or multivariate return series of class timeSeries or any other object which can be transformed by the function as.timeSeries() into an object of class timeSeries. and a default main title should be added to the plot. By default TRUE.
$\mathrm{n} \quad$ an integer value, the number of lags.
maximum lag for which the autocorrelation should be calculated, an integer.
a character string which specifies the type of the input series, either "returns" or series "values". In the case of a return series as input, the required value series is computed by cumulating the financial returns: $\exp (\operatorname{colCumsums}(x))$

```
deltas the exponents, a numeric vector, by default ranging from 0.2 to 3.0 in steps of
    0.2.
ymax maximum y-axis value on plot. If NA, then the value is selected automatically.
standardize a logical value. Should the vector x be standardized?
... arguments to be passed.
```


## Details

## Autocorrelation Functions:

The functions acfPlot and pacfPlot, plot and estimate autocorrelation and partial autocorrelation function. The functions allow to get a first view on correlations within the time series. The functions are synonym function calls for R's acf and pacf from the the ts package.

## Taylor Effect:

The "Taylor Effect" describes the fact that absolute returns of speculative assets have significant serial correlation over long lags. Even more, autocorrelations of absolute returns are typically greater than those of squared returns. From these observations the Taylor effect states, that that the autocorrelations of absolute returns to the the power of delta, abs $(x-m e a n(x))^{\wedge}$ delta reach their maximum at delta=1. The function teffect explores this behaviour. A plot is created which shows for each lag (from 1 to max. lag) the autocorrelations as a function of the exponent delta. In the case that the above formulated hypothesis is supported, all the curves should peak at the same value around delta=1.

## Value

for acfPlot and pacfplot, an object of class "acf", see acf;
for teffectPlot, a numeric matrix of order deltas by max. lag with the values of the autocorrelations;
for lacfPlot, a list with the following two elements:
Rho the autocorrelation function,
lagged the lagged correlations.

## References

Taylor S.J. (1986); Modeling Financial Time Series, John Wiley and Sons, Chichester.
Ding Z., Granger C.W.J., Engle R.F. (1993); A long memory property of stock market returns and a new model, Journal of Empirical Finance 1, 83.

## Examples

```
## data -
    data(LPP2005REC, package = "timeSeries")
    SPI <- LPP2005REC[, "SPI"]
    plot(SPI, type = "l", col = "steelblue", main = "SP500")
```

```
    abline(h = 0, col = "grey")
## teffectPlot -
    # Taylor Effect:
    teffectPlot(SPI)
```

akimaInterp Bivariate Spline Interpolation

## Description

Interpolates bivariate data sets using Akima spline interpolation.

## Usage

akimaInterp(x, y = NULL, $z=$ NULL, gridPoints = 21,
$x_{0}=\operatorname{seq}(\min (x), \max (x)$, length $=$ gridPoints),
yo $=\operatorname{seq}(\min (y), \max (y)$, length $=$ gridPoints), extrap $=$ FALSE)
akimaInterpp(x, y = NULL, z = NULL, xo, yo, extrap = FALSE)

## Arguments

$x, y, z \quad$ for akimaInterp the arguments $x$ and $y$ are two numeric vectors of grid pounts, and $z$ is a numeric matrix or any other rectangular object which can be transformed by the function as.matrix into a matrix object. For akimaInterpp we consider either three numeric vectors of equal length or if $y$ and $z$ are NULL, a list with entries $x, y, z$, or named data frame with $x$ in the first, $y$ in the second, and $z$ in the third column.
gridPoints an integer value specifying the number of grid points in $x$ and $y$ direction.
xo, yo for akimaInterp two numeric vectors of data points spanning the grid, and for akimaInterpp two numeric vectors of data points building pairs for pointwise interpolation.
extrap a logical, if TRUE then the data points are extrapolated.

## Details

Two options are available: gridded and pointwise interpolation.
akimaInterp is a wrapper to interp provided by the contributed R package akima. The Fortran code of the Akima spline interpolation routine was written by H. Akima.
Linear surface fitting and krige surface fitting are provided by the functions linearInterp and krigeInterp.

## Value

akimaInterp returns a list with at least three entries, $x, y$ and $z$. Note, that the returned values, can be directly used by the persp and contour 3D plotting methods.
akimaInterpp returns a data.frame with columns " $x$ ", " $y$ ", and " $z$ ".

## Note

Package akima is no longer needed. Equivalent functions from package interp are now called instead.

## References

Akima H., 1978, A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points, ACM Transactions on Mathematical Software 4, 149-164.

Akima H., 1996, Algorithm 761: Scattered-Data Surface Fitting that has the Accuracy of a Cubic Polynomial, ACM Transactions on Mathematical Software 22, 362-371.

## See Also

linearInterp, krigeInterp.

## Examples

```
## Does not run for r-solaris-x86
## akimaInterp -- Akima Interpolation:
if (requireNamespace("interp")) {
    set.seed(1953)
    x <- runif(999) - 0.5
    y <- runif(999) - 0.5
    z<- cos(2*pi*(x^2+y^2))
    ans <- akimaInterp(x, y, z, gridPoints = 41, extrap = FALSE)
    persp(ans, theta = -40, phi = 30, col = "steelblue",
                xlab = "x", ylab = "y", zlab = "z")
    contour(ans)
}
## Use spatial as alternative on r-solaris-x86
## spatialInterp - Generate Kriged Grid Data:
if (requireNamespace("spatial")) {
    RNGkind(kind = "Marsaglia-Multicarry", normal.kind = "Inversion")
    set.seed(4711, kind = "Marsaglia-Multicarry")
    x <- runif(999)-0.5
    y <- runif(999)-0.5
    z <- cos(2*pi*(x^2+y^2))
    ans <- krigeInterp(x, y, z, extrap = FALSE)
    persp(ans)
    title(main = "Kriging")
    contour(ans)
    title(main = "Kriging")
}
```


## Description

Basic extensions which add and/or modify additional functionality which is not available in R's basic packages.

## Usage

\#\# Default S3 method:
stdev(x, na.rm = FALSE)
\#\# Default S3 method:
termPlot(model, ...)

## Arguments

| model | a fitted model object. |
| :--- | :--- |
| x | an object for which to compute the standard deviation. |
| na.rm | a logical value - should the NA values be removed. |
| $\ldots$. | arguments to be passed. |

## Details

stdev and termPlot are generic functions with default methods stats: :sd and stats: : termplot, respectively.

## See Also

sd, termplot

| BasicStatistics $\quad$ Basic time series statistics |
| :--- | :--- |

## Description

Computes basic financial time series statistics.

## Usage

```
basicStats(x, ci = 0.95)
```


## Arguments

x
an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class "timeSeries". The latter case, other than "timeSeries" objects, is more or less untested.
ci confidence interval, a numeric value, by default 0.95 , i.e. $95 \%$.

## Details

Computes a number of sample statistics for each column of $x$. The statistics should be clear from the row names of the returned data frame.
"LCL" and "UCL" stand for lower/upper confidence limits, computed under the null hypothesis of i.i.d.
"Kurtosis" represents the excess kurtosis, so its theoretical value for the normal distribution is zero, not 3.
These statistics are often computed as a first step in the study of returns on financial assets. In that case any inference on these statistics (including the confidence intervals for the mean) should be considered exploratory, since returns are virtually never i.i.d.

## Value

a data frame with one column for each column of $x$ and the following rows:
"nobs" number of observations,
"NAs" number of NAs
"Minimum" minimum,
"Maximum" maximum,
"1. Quartile" lower quartile,
"3. Quartile" upper quartile,
"Mean" mean,
"Median" median,
"Sum" sum of the values,
"SE Mean" standard error of the mean,
"LCL Mean" lower limit of the CI for the mean,
"UCL Mean" upper limit of the CI for the mean,
"Variance" variance,
"Stdev" standard deviation,
"Skewness" skewness coefficient,
"Kurtosis" excess kurtosis.

## Examples

```
## basicStats -
    # Simulated Monthly Return Data:
    tS = timeSeries(matrix(rnorm(12)), timeDate::timeCalendar())
    basicStats(tS)
```

BoxPlot Time series box plots

## Description

Produce a box plot or a box percentile plot.

## Usage

```
boxPlot(x, col = "steelblue", title = TRUE, ...)
boxPercentilePlot(x, col = "steelblue", title = TRUE, ...)
```


## Arguments

$x \quad$ an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other then timeSeries objects, is more or less untested.
col the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat. colors (ncol(x)).
title a logical flag, by default TRUE. Should a default title added to the plot?
... optional arguments to be passed.

## Details

boxPlot produces a side-by-side standard box plot, boxPercentilePlot produces a side-by-side box-percentile plot.

## Value

NULL, displays a time series plot

## Examples

```
## data -
    data(LPP2005REC, package = "timeSeries")
    LPP <- LPP2005REC[, 1:6]
    plot(LPP, type = "l", col = "steelblue", main = "SP500")
    abline(h = 0, col = "grey")
## boxPlot -
    boxPlot(LPP)
```

```
characterTable Table of characters
```


## Description

Displays a table of numerical equivalents to Latin characters.

## Usage

characterTable(font $=1$, cex $=0.7$ )

## Arguments

cex a numeric value, determines the character size, the default size is 0.7.
font an integer value, the number of the font, by default font number 1.

## Value

displays a table with the characters of the requested font. The character on line "xy" and column " $z$ " of the table has code " $\backslash x y z$ ", e.g cat (" $\backslash 126$ ") prints: V for font number 1. These codes can be used as any other characters.

Note
What happens with non-ASCII characters in plots is system dependent and depends on the graphics device, as well. Use of such characters is not recommended for portable code.

## See Also

colorTable, symbolTable
points for use of characters in plotting

## Examples

```
## Character Table for Font 1:
# characterTable(font = 1)
```

colorLocator $\quad$ Named colors in $R$

## Description

Displays R's 657 named colors for selection and returns optionally R's color names.

## Usage

colorLocator(locator $=$ FALSE, cex.axis $=0.7$ )
colorMatrix()

## Arguments

locator logical, if true, locator is used for interactive selection of color names, default is FALSE.
cex.axis size of axis labels.

## Details

Color Locator:
The colorLocator function plots R's 657 named colors. If locator=TRUE then you can interactively point and click to select the colors for which you want names. To end selection, right click on the mouse and select 'Stop', then R returns the selected color names.

The functions used here are wrappers to the functions provided by Tomas Aragon in the contributed R package epitools.

## Value

## Color Locator:

colorsLocator() generates a plot with R colors and, when locator is true, returns matrix with graph coordinates and names of colors selected. colorsMatrix() quietly returns the matrix of names.

## See Also

colorPalette, colorTable.

## Examples

colorLocator()

```
colorPalette Color palettes
```


## Description

Functions to create color palettes.

The functions are:

| rainbowPalette |  |
| :--- | :--- |
| heatPalette | Contiguous rainbow color palette, |
| terrainPalette | Contiguous heat color palette, |
| topoPalette | Contiguous terrain color palette, |
| cmPalette color palette, |  |
| greyPalette | Contiguous cm color palette, |
| timPalette | R's gamma-corrected gray palette, |
| rampPalette | Color Matlab like color palette, |
| seqPalette | Sequential color brewer palettes, |
| divPalette | Diverging color brewer palettes, |
| qualiPalette | Qualified color brewer palettes, |
| focusPalette | Red, green blue focus palettes, <br> monoPalette |
|  | Red, green blue mono palettes. |

## Usage

```
rainbowPalette(n = 64, ...)
heatPalette(n = 64, ...)
terrainPalette(n = 64, ...)
topoPalette(n = 64, ...)
cmPalette(n = 64, ...)
greyPalette(n = 64, ...)
timPalette(n = 64)
rampPalette(n, name = c("blue2red", "green2red", "blue2green",
    "purple2green", "blue2yellow", "cyan2magenta"))
seqPalette(n, name = c(
    "Blues", "BuGn", "BuPu", "GnBu", "Greens", "Greys", "Oranges",
    "OrRd", "PuBu", "PuBuGn", "PuRd", "Purples", "RdPu", "Reds",
    "YlGn", "YlGnBu", "YlOrBr", "YlOrRd"))
divPalette(n, name = c(
    "BrBG", "PiYG", "PRGn", "PuOr", "RdBu", "RdGy", "RdYlBu", "RdYlGn",
    "Spectral"))
qualiPalette(n, name = c(
```

```
    "Accent", "Dark2", "Paired", "Pastel1", "Pastel2", "Set1", "Set2",
    "Set3"))
focusPalette(n, name = c("redfocus", "greenfocus", "bluefocus"))
monoPalette(n, name = c("redmono", "greenmono", "bluemono"))
```


## Arguments

n
an integer, giving the number of greys or colors to be constructed.
name
a character string, the name of the color set.
arguments to be passed, see the details section

## Details

All Rmetrics' color sets are named as fooPalette, where the prefix foo denotes the name of the underlying color set.

## R's Contiguous Color Palettes::

Palettes for n contiguous colors are implemented in the grDevices package. To conform with Rmetrics' naming convention for color palettes we have build wrappers around the underlying functions. These are the rainbowPalette, heatPalette, terrainPalette, topoPalette, and the cmPalette.
Conceptually, all of these functions actually use (parts of) a line cut out of the 3-dimensional color space, parametrized by the function $h s v(h, s, v$, gamma), where gamma=1 for the fooPalette function, and hence, equispaced hues in RGB space tend to cluster at the red, green and blue primaries.
Some applications, such as contouring, require a palette of colors which do not wrap around to give a final color close to the starting one. To pass additional arguments to the underlying functions see help(rainbow). With rainbow, the parameters start and end can be used to specify particular subranges of hues. Synonym function calls are rainbow, heat.colors, terrain.colors, topo.colors, and cm.colors.

## R's Gamma-Corrected Gray Palette::

grayPalette chooses a series of $n$ gamma-corrected gray levels. The range of the gray levels can be optionally monitored through the . . . arguments, for details see help(gray.colors), which is a synonym function call in the grDevices package.

## Tim's Matlab like Color Palette::

timPalette creates a color set ranging from blue to red, and passes through the colors cyan, yellow, and orange. It comes from the Matlab software, originally used in fluid dynamics simulations. The function here is a copy from R's contributed package fields doing a spline interpolation on $\mathrm{n}=64$ color points.

## Color Ramp Palettes::

rampPalette creates several color ramps. The function is implemented from Tim Keitt's contributed R package colorRamps. Supported through the argument name are the following color ramps: "blue2red", "green2red", "blue2green", "purple2green", "blue2yellow", "cyan2magenta".

## Color Brewer Palettes::

The functions seqPalette, divPalette, and qualiPalette create color sets according to R's contributed RColorBrewer package. The first letter in the function name denotes the type of the color set: " s " for sequential palettes, " d " for diverging palettes, and " q " for qualitative palettes.
Sequential palettes are suited to ordered data that progress from low to high. Lightness steps dominate the look of these schemes, with light colors for low data values to dark colors for high data values. The sequential palettes names are: Blues, BuGn, BuPu, GnBu, Greens, Greys, Oranges, OrRd, PuBu, PuBuGn, PuRd, Purples, RdPu, Reds, YlGn, YlGnBu, YlOrBr, YlOrRd.
Diverging palettes put equal emphasis on mid-range critical values and extremes at both ends of the data range. The critical class or break in the middle of the legend is emphasized with light colors and low and high extremes are emphasized with dark colors that have contrasting hues. The diverging palettes names are: BrBG, PiYG, PRGn, PuOr, RdBu, RdGy, RdYlBu, RdYlGn, Spectral.
Qualitative palettes do not imply magnitude differences between legend classes, and hues are used to create the primary visual differences between classes. Qualitative schemes are best suited to representing nominal or categorical data. The qualitative palettes names are: Accent, Dark2, Paired, Pastel1, Pastel2, Set1, Set2, Set3.
In contrast to the original color brewer palettes, the palettes here are created by spline interpolation from the color variation with the most different values, i.e for the sequential palettes these are 9 values, for the diverging palettes these are 11 values, and for the qualitative palettes these are between 8 and 12 values dependeing on the color set.

## Graph Color Palettes:

The function perfanPalette creates color sets inspired by R's contributed package Performance Analytics. These color palettes have been designed to create readable, comparable line and bar graphs with specific objectives.
Focused Color Palettes Color sets designed to provide focus to the data graphed as the first element. This palette is best used when there is clearly an important data set for the viewer to focus on, with the remaining data being secondary, tertiary, etc. Later elements graphed in diminishing values of gray.
Monochrome Color Palettes These include color sets for monochrome color displays.

## Value

a character string of color strings

## Note

The palettes are wrapper functions provided in several contributed R packages. These include:
Cynthia Brewer and Mark Harrower for the brewer palettes,
Peter Carl and Brian G. Peterson for the "PerformanceAnalytics" package,
Tim Keitt for the "colorRamps" package, Ross Ihaka for the "colorspace" package, Tomas Aragon for the "epitools" package, Doug Nychka for the "fields" package, Erich Neuwirth for the "RColorBrewer" package.

Additional undocumented hidden functions:

$$
\begin{array}{ll}
\text {.asRGB } & \text { Converts any R color to RGB (red/green/blue), } \\
\text {.chcode } & \text { Changes from one to another number system, } \\
\text {.hex.to.dec } & \text { Converts heximal numbers do decimal numbers, } \\
\text {.dec.to.hex } & \text { Converts decimal numbers do heximal numbers. }
\end{array}
$$

## Examples

> \#\# GreyPalette:
greyPalette()

```
    colorTable Table of colors
```


## Description

Displays a table of color codes and plots the colors themselves.

## Usage

colorTable(cex = 0.7)

## Arguments

cex a numeric value, determines the character size in the color plot, the default is 0.7 .

## Value

a table of plot colors with the associated color numbers

## See Also

```
characterTable, symbolTable
```


## Examples

```
## Color Table:
    colorTable()
```


## colVec Column and row vectors

## Description

Creates a column or row vector from a numeric vector.

## Usage

colVec (x)
rowVec(x)

## Arguments

x
a numeric vector.

## Details

colVec and rowVec transform a vector into a column and row vector, respectively. A column vector is a matrix object with one column, and a row vector is a matrix object with one row.

## Examples

```
## Create a numeric Vector:
    x = rnorm(5)
## Column and Row Vectors:
    colVec(x)
    rowVec(x)
```

correlationTest Correlation tests

## Description

Tests if two series are correlated.

## Usage

```
correlationTest(x, y, method = c("pearson", "kendall", "spearman"),
    title = NULL, description = NULL)
pearsonTest(x, y, title = NULL, description = NULL)
kendallTest(x, y, title = NULL, description = NULL)
spearmanTest(x, y, title = NULL, description = NULL)
```


## Arguments

$x, y \quad$ numeric vectors of data values.
method a character string naming which test should be applied.
title an optional title string, if not specified the input's data name is deparsed.
description optional description string, or a vector of character strings.

## Details

These functions test for association/correlation between paired samples based on the Pearson's product moment correlation coefficient (a.k.a. sample correlation), Kendall's tau, and Spearman's rho coefficients.
pearsonTest, kendallTest, and spearmanTest are wrappers of base R's cor.test with simplified interface. They provide 'exact' and approximate p-values for all three alternatives (two-sided, less, and greater), as well as $95 \%$ confidence intervals. This is particularly convenient in interactive use.

Instead of calling the individual functions, one can use correlationTest and specify the required test with argument method.

## Value

an object from class fHTEST

## References

Conover, W. J. (1971); Practical nonparametric statistics, New York: John Wiley \& Sons.
Lehmann E.L. (1986); Testing Statistical Hypotheses, John Wiley and Sons, New York.

## See Also

locationTest, scaleTest, varianceTest.

## Examples

```
## x, y -
    x = rnorm(50)
    y = rnorm(50)
## correlationTest -
    correlationTest(x, y, "pearson")
    correlationTest(x, y, "kendall")
    spearmanTest(x, y)
```


## Description

Functions for decorating plots.

## Usage

decor ()
hgrid(ny = NULL, ...)
$\operatorname{vgrid}(n x=N U L L, . .$.
boxL(col = "white")
box_(col = c("white", "black"))
copyright()

## Arguments

col the color of the background, "black" and foreground "white" lines of the box.
$n x$, ny number of cells of the grid in $x$ or $y$ direction. When NULL, as per default, the grid aligns with the tick marks on the corresponding default axis (i.e., tick marks as computed by axTicks).
... additional arguments passed to the $\operatorname{grid}()$ function.

## Details

decor is equivalent to hgrid() followed by boxL().
hgrid creates horizontal grid lines.
vgrid creates vertical grid lines.
boxL creates an L-shaped box
box_ creates a bottom line box.
copyright adds Rmetrics copyright to a plot.

## Examples

```
plot(x = rnorm(100), type = "l", col = "red",
    xlab = "", ylab = "Variates", las = 1)
title("Normal Deviates", adj = 0)
hgrid()
boxL()
copyright()
```


## distCheck Distribution check

## Description

Tests properties of an $R$ implementation of a distribution, i.e., of all four of its "dpqr" functions.

## Usage

```
distCheck(fun = "norm", n = 1000, robust = TRUE, subdivisions = 100, ...)
```


## Arguments

| fun | a character string, the name of the distribution. |
| :--- | :--- |
| n | an integer specifying the number of random variates to be generated. |
| robust | logical flag, should robust estimates be used? By default TRUE. |
| subdivisions | integer specifying the numbers of subdivisions in integration. |
| $\ldots$ | the distributional parameters. |

## Examples

```
distCheck("norm", mean = 1, sd = 1)
distCheck("lnorm", meanlog = 0.5, sdlog = 2, robust=FALSE)
## here, true E(X) = exp(mu + 1/2 sigma^2) = exp(.5 + 2) = exp(2.5) = 12.182
## and Var (X) = exp(2*mu + sigma^2)*(exp(sigma^2) - 1) = 7954.67
```

DistributionFits Parametric fit of a distribution

## Description

A collection and description of moment and maximum likelihood estimators to fit the parameters of a distribution.

The functions are:

$$
\begin{array}{ll}
\text { nFit } & \text { MLE parameter fit for a normal distribution, } \\
\text { tFit } & \text { MLE parameter fit for a Student t-distribution, } \\
\text { stableFit } & \text { MLE and Quantile Method stable parameter fit. }
\end{array}
$$

## Usage

nFit(x, doplot = TRUE, span = "auto", title = NULL, description = NULL, ...)

```
tFit(x, df = 4, doplot = TRUE, span = "auto", trace = FALSE, title = NULL,
    description = NULL, ...)
stableFit(x, alpha = 1.75, beta = 0, gamma = 1, delta = 0,
    type = c("q", "mle"), doplot = TRUE, control = list(),
    trace = FALSE, title = NULL, description = NULL)
```


## Arguments

| x | a numeric vector. |
| :---: | :---: |
| doplot | a logical flag. Should a plot be displayed? |
| span | x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001 , and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times $=n$ ), where, min and max are the left and right endpoints of the range, and $n$ gives the number of the intermediate points. |
| control | a list of control parameters, see function nlminb. |
| alpha, beta, gamma, delta |  |
|  | The parameters are alpha, beta, gamma, and delta: value of the index parameter alpha with alpha $=(0,2]$; skewness parameter beta, in the range $[-1,1]$; scale parameter gamma; and shift parameter delta. |
| description | a character string which allows for a brief description. |
| df | the number of degrees of freedom for the Student distribution, $d f>2$, maybe non-integer. By default a value of 4 is assumed. |
| title | a character string which allows for a project title. |
| trace | a logical flag. Should the parameter estimation process be traced? |
| type | a character string which allows to select the method for parameter estimation: "mle", the maximum log likelihood approach, or "qm", McCulloch's quantile method. |
|  | parameters to be parsed. |

## Details

## Stable Parameter Estimation:

Estimation techniques based on the quantiles of an empirical sample were first suggested by Fama and Roll [1971]. However their technique was limited to symmetric distributions and suffered from a small asymptotic bias. McCulloch [1986] developed a technique that uses five quantiles from a sample to estimate alpha and beta without asymptotic bias. Unfortunately, the estimators provided by McCulloch have restriction alpha>0.6.
Remark: The parameter estimation for the stable distribution via the maximum Log-Likelihood approach may take a quite long time.

## Value

an object from class "fDISTFIT"

## Examples

```
## nFit -
    # Simulate random normal variates N(0.5, 2.0):
    set.seed(1953)
    s = rnorm(n = 1000, 0.5, 2)
## nigFit -
    # Fit Parameters:
    nFit(s, doplot = TRUE)
```

fBasics-deprecated Deprecated functions in package fBasics

## Description

These functions are provided for compatibility with older versions of the package only, and may be defunct as soon as of the next release.

## Details

There are none currently.
dstable, etc., now are defunct, as they have been available from stabledist since early 2011.

## See Also

Deprecated, Defunct
fBasicsData fBasics data sets

## Description

The following data sets are part of this package:

| Capitalization | Market capitalization of domestic companies, |
| :--- | :--- |
| cars2 | Data for various car models, |
| DowJones30 | Down Jones 30 stocks, |
| HedgeFund | Hennessee Hedge Fund Indices, |
| msft. dat | Daily Microsoft OHLC prices and volume, |
| nyse | NYSE composite Index, |
| PensionFund | Swiss Pension Fund LPP-2005, |
| swissEconomy | Swiss Economic Data, |
| SWXLP | Swiss Pension Fund LPP-2000, |
| usdthb | Tick data of USD to THB. |

## Details

All datasets are data frames. A brief description is given below.

## Capitalization:

Capitalization contains market capitalization of 13 domestic companies for 6 years (from 2003 to 2008) in USD millions. Each row contains the data for one company/stock exchange.

## cars2:

cars2 contains columns rowNames (model), Price, Country, Reliability, Mileage, (Type), (Weight), Disp. (engine displacement) and HP (net horsepower) reprsenting the indicated properties of 60 car models.

## DowJones30:

DowJones 30 contains 2529 daily observations from the 'Dow Jones 30' Index series. The first row contains the dates (from 1990-12-31 to 2001-01-02). Each of the remaining thirty columns represents the closing price of a stock in the Index.

## HedgeFund:

HedgeFund contains monthly percentage returns of 16 hedge fund strategies from Hennessee Group LLC for year 2005.

## msft.dat:

msft. dat contains daily prices (open, high, low and close) and volumes for the Microsoft stocks. It is a data frame with column names "\%Y-\%m-\%d", "Open", "High", "Low", "Close", "Volume".

Note: there is a dataset, MSFT, in package timeSeries which contains the same data but is of class "timeSeries".

## nyse:

nyse contains daily records of the NYSE Composite Index from 1966-01-04 to 2002-12-31 (9311 observations). The data is in column "NYSE" (second column). The first column contains the dates.

## PensionFund:

PensionFund is a daily data set of the Swiss pension fund benchmark LPP-2005. The data set ranges from 2005-11-01 to 2007-04-11. The columns are named: SBI, SPI, SII, LMI, MPI, ALT, LPP25, LPP40, LPP60.

## swissEconomy:

swissEconomy contains the GDP per capita (GDPR), exports (EXPO), imports (IMPO), interest rates (INTR), inflation (INFL), unemployment (UNEM) and population (POPU) foryears 1964 to 1999 for Switzerland.

## SWXLP:

SWXLP is a daily data set of the Swiss pension fund benchmark LPP-2000. The data set ranges from 2000-01-03 to 2007-05-08 (1917 observations). The first column contains the dates. The remaining columns are named: SBI, SPI, SII, LP25, LP40, LP60.

## usdthb:

usdthb Tick data of US Dollar (USD) in Thailand Bhat (THB) collected from Reuters. The date is in the first column in YYYYMMDDhhmm format. The remaining columns contain: delay time (DELAY), contributor (CONTRIBUTOR), bid (BID) and ask (ASK) prices, and quality flag (FLAG). It covers the Asia FX crisis in June 1997.

## References

## Capitalization:

World Federation of Stock Exchanges, http://www.world-exchanges.org/statistics.
cars2:
Derived from the car90 dataset within the rpart package. The car90 dataset is based on the car.all dataset in S-PLUS. Original data comes from: April 1990, Consumer Reports Magazine, pages 235-255, 281-285 and 287-288.

## DowJones30

https://www.yahoo.com.

## HedgeFund:

http://www.hennesseegroup.com/indices/returns/year/2005.html.

## msft.dat:

https://www.yahoo.com.
nyse:
https://www.nyse.com.

## PensionFund:

SBI, SPI, SII: SIX (Swiss Exchange Zurich); LPP25, LPP40, LPP60: Banque Pictet Geneva; LMI, MPI, ALT: Recalculated from the indices and benchmarks.

## swissEconomy:

https://www.oecd.org/ and https://www.imf.org/.
SWXLP:
SBI, SPI, SII: SIX (Swiss Exchange Zurich); LPP25, LPP40, LPP60: Banque Pictet Geneva.
usdthb:
Reuters Select Feed Terminal (1997).

## Examples

```
## Plot DowJones30 Example Data Set
    series <- timeSeries::as.timeSeries(DowJones30)
    head(series)
    plot(series[,1:6], type = "l")
## msft.dat contains (almost?) the same data as MSFT in package timeSeries
data(MSFT, package = "timeSeries")
m1 <- as.matrix(msft.dat[, -1]) # drop date stamps in column 1
m2 <- as.matrix(MSFT)
all.equal(m1, m2, check.attributes = FALSE) # TRUE
## compare the dates:
all.equal(format(msft.dat[ , 1]), format(time(MSFT))) # TRUE
```

```
fDISTFIT-class Class "fDISTFIT"
```


## Description

S4 class representing fitted distributions.

## Objects from the Class

Objects can be created by calls of the form new("fDISTFIT", ...) but are typically created by functions fitting distributions.

## Slots

```
    call: Object of class "call" ~~
```

    model: Object of class "character" ~~
    data: Object of class "data.frame" ~~
    fit: Object of class "list" ~~
    title: Object of class "character" ~~
    description: Object of class "character" ~~
    Slot fit is a list with components:
estimate the point at which the maximum value of the log liklihood function is obtained.
minimum the value of the estimated maximum, i.e. the value of the log liklihood function.
code an integer indicating why the optimization process terminated.
gradient the gradient at the estimated maximum.

The above description of slot fit is taken from the documentation for $t F i t$, $n F i t$ and stableFit. TODO: needs checking and also is it the same for other distribution fitting functions.

## Methods

show signature(object = "fDISTFIT"):

## Examples

showClass("fDISTFIT")

```
fHTEST-class Class "fHTEST"
```


## Description

An S4 class representing the outcome of a statistical test.

## Objects from the Class

Objects are created by some statistical test functions.

## Slots

call: the function call.
data: the data as specified by the input argument(s).
test: a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class "htest".
title: a character string with the name of the test. This can be overwritten specifying a user defined input argument.
description: a character string with an optional user defined description. By default just the current date when the test was applied will be returned.
Slot @test is an object of class "list" containing at least the following elements:
statistic the value(s) of the test statistic.
p.value the p-value(s) of the test.
parameters a numeric value or vector of parameters.
estimate a numeric value or vector of sample estimates.
conf.int a numeric two row vector or matrix of $95 \%$ confidence levels.
method a character string indicating what type of test was performed.
data.name a character string giving the name(s) of the data.

## Methods

show signature(object = "fHTEST"): ...

## See Also

for functions returning objects from class "fHTEST", see scaleTest, correlationTest, ks2Test, locationTest, NormalityTests, varianceTest

## Examples

showClass("fHTEST")

```
    getS4
```


## Description

A collection and description of functions to extract slots from S 4 class objects.

The extractor functions are:

| getModel | Extracts the model slot from a S4 object, |
| :--- | :--- |
| getTitle | Extracts the title slot from a S4 object, |
| getDescription | Extracts the description slot from a S4 object, |
| getSlot | Extracts a specified slot from a S4 object, |
| getArgs | Shows the arguments of a S4 function. |

Since $R$ version 2.14.0, a generic getCall() is part of $R$; for earlier versions, we had provided a simple version for S 4 objects.

## Usage

```
getModel(object)
getTitle(object)
getDescription(object)
getSlot(object, slotName)
getArgs(f, signature)
```


## Arguments

| $f$ | a generic function or the character-string name of one. |
| :--- | :--- |
| object | an object of class $S 4$. |
| signature | the signature of classes to match to the arguments of $f$ |
| slotName | a character string, the name of the slot to be extracted from the S4 object. |

## Value

for getModel, getTitle, getDescription, and getSlot - the content of the corresponding slot.
for getArgs the names of the arguments.

## Examples

```
## Example S4 Representation:
    # Hyothesis Testing with Control Settings
    setClass("hypTest",
```

```
        representation(
            call = "call",
            data = "numeric",
            test = "list",
            description = "character")
    )
## Shapiro Wilk Normaility Test
    swTest = function(x, description = "") {
        ans = shapiro.test(x)
        class(ans) = "list"
        new("hypTest",
            call = match.call(),
            data = x,
            test = ans,
            description = description)
    }
    test = swTest(x = rnorm(500), description = "500 RVs")
## Extractor Functions:
    isS4(test)
    getCall(test)
    getDescription(test)
## get arguments
args(returns)
getArgs(returns)
getArgs("returns")
getArgs(returns, "timeSeries")
getArgs("returns", "timeSeries")
```


## Description

Density, distribution function, quantile function and random generation for the generalized hyperbolic distribution.

## Usage

$\operatorname{dgh}(x$, alpha $=1$, beta $=0$, delta $=1, m u=0, \operatorname{lambda}=-1 / 2, \log =$ FALSE $)$
$\operatorname{pgh}(q$, alpha $=1$, beta $=0$, delta $=1, m u=0$, lambda $=-1 / 2$ )
$\operatorname{qgh}(\mathrm{p}$, alpha $=1$, beta $=0$, delta $=1, \operatorname{mu}=0$, lambda $=-1 / 2$ )
$\operatorname{rgh}(\mathrm{n}, \mathrm{alpha}=1$, beta $=0$, delta $=1$, mu $=0$, lambda $=-1 / 2$ )

## Arguments

$x, q \quad a \quad$ numeric vector of quantiles.
$p \quad a \quad$ numeric vector of probabilities.
n number of observations.
alpha first shape parameter.
beta second shape parameter, should in the range ( 0 , alpha).
delta scale parameter, must be zero or positive.
$\mathrm{mu} \quad$ location parameter, by default 0.
lambda defines the sublclass, by default $-1 / 2$.
$\log \quad$ a logical flag by default FALSE. Should labels and a main title drawn to the plot?

## Details

dgh gives the density, pgh gives the distribution function, qgh gives the quantile function, and rgh generates random deviates.
The meanings of the parameters correspond to the first parameterization, $\mathrm{pm}=1$, which is the default parameterization for this distribution.

In the second parameterization, $\mathrm{pm}=2$, alpha and beta take the meaning of the shape parameters (usually named) zeta and rho.

In the third parameterization, $\mathrm{pm}=3$, alpha and beta take the meaning of the shape parameters (usually named) xi and chi.

In the fourth parameterization, $\mathrm{pm}=4$, alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.
The generator rgh is based on the GH algorithm given by Scott (2004).

## Value

numeric vector

## Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.

Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.
Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
    ## rgh -
    set.seed(1953)
    r = rgh(5000, alpha = 1, beta = 0.3, delta = 1)
    plot(r, type = "l", col = "steelblue",
        main = "gh: alpha=1 beta=0.3 delta=1")
## dgh -
    # Plot empirical density and compare with true density:
    hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
    x = seq(-5, 5, 0.25)
    lines(x, dgh(x, alpha = 1, beta = 0.3, delta = 1))
## pgh -
    # Plot df and compare with true df:
    plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
    lines(x, pgh(x, alpha = 1, beta = 0.3, delta = 1))
## qgh -
    # Compute Quantiles:
    qgh(pgh(seq(-5, 5, 1), alpha = 1, beta = 0.3, delta = 1),
        alpha = 1, beta = 0.3, delta = 1)
```

ghFit

GH Distribution Fit

## Description

Estimates the distrinbutional parameters for a generalized hyperbolic distribution.

## Usage

ghFit(x, alpha $=1$, beta $=0$, delta $=1$, mu = 0, lambda $=-1 / 2$, scale $=$ TRUE, doplot $=$ TRUE, span = "auto", trace = TRUE, title $=$ NULL, description $=$ NULL, ...)

## Arguments

x
alpha first shape parameter.
beta second shape parameter, should in the range ( 0, alpha).
delta scale parameter, must be zero or positive.
mu location parameter, by default 0 .
lambda defines the sublclass, by default $-1 / 2$.
scale a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?

| doplot | a logical flag. Should a plot be displayed? <br> span <br> x-coordinates for the plot, by default 100 values automatically selected and rang- <br> ing between the 0.001, and 0.999 quantiles. Alternatively, you can specify the <br> range by an expression like span=seq ( min, , max, times $=\mathrm{n}$ ), where, min and <br> max are the left and right endpoints of the range, and $n$ gives the number of the <br> intermediate points. |
| :--- | :--- |
| trace | a logical flag. Should the parameter estimation process be traced? |
| title | a character string which allows for a project title. |
| description | a character string which allows for a brief description. |
| $\ldots$ | parameters to be parsed. |

## Details

The meanings of the parameters correspond to the first parameterization, see gh for further details.
The function nlm is used to minimize the "negative" maximum log-likelihood function. nlm carries out a minimization using a Newton-type algorithm.

## Value

a list with the following components:
estimate
the point at which the maximum value of the log liklihood function is obtained.
minimum
the value of the estimated maximum, i.e. the value of the log liklihood function.
an integer indicating why the optimization process terminated.
1: relative gradient is close to zero, current iterate is probably solution;
2: successive iterates within tolerance, current iterate is probably solution;
3: last global step failed to locate a point lower than estimate. Either estimate
is an approximate local minimum of the function or steptol is too small;
4: iteration limit exceeded;
5: maximum step size stepmax exceeded five consecutive times. Either the
function is unbounded below, becomes asymptotic to a finite value from above
in some direction or stepmax is too small.
gradient

steps $\quad$| the gradient at the estimated maximum. |
| :--- | :--- |

## Examples

```
## ghFit -
    # Simulate Random Variates:
    set.seed(1953)
    s = rgh(n = 1000, alpha = 1.5, beta = 0.3, delta = 0.5, mu = -1.0)
## ghFit -
    # Fit Parameters:
    ghFit(s, alpha = 1, beta = 0, delta = 1, mu = mean(s), doplot = TRUE)
```

ghMode Generalized Hyperbolic Mode

## Description

Computes the mode of the generalized hyperbolic function.

## Usage

ghMode(alpha $=1$, beta $=0$, delta $=1$, mu $=0$, lambda $=-1 / 2$ )

## Arguments

| alpha | first shape parameter. |
| :--- | :--- |
| beta | second shape parameter, should in the range ( 0, alpha). |
| delta | scale parameter, must be zero or positive. |
| mu | location parameter, by default 0. |
| lambda | defines the sublclass, by default $-1 / 2$. |

## Details

The meanings of the parameters correspond to the first parameterization, see gh for further details.

## Value

a numeric value, the mode of the generalized hyperbolic distribution

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.
Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.

Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
## ghMode -
    ghMode()
```


## Description

Calculates moments of the generalized hyperbolic distribution.

## Usage

ghMean(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)
$\operatorname{ghVar}(a l p h a=1$, beta=0, delta=1, mu=0, lambda=-1/2)
ghSkew(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)
ghKurt(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)
ghMoments(order, type = c("raw", "central", "mu"),
alpha $=1$, beta=0, delta=1, mu=0, lambda=-1/2)

## Arguments

alpha numeric value, the first shape parameter.
beta numeric value, the second shape parameter in the range (0, alpha).
delta numeric value, the scale parameter, must be zero or positive.
mu numeric value, the location parameter, by default 0 .
lambda numeric value, defines the sublclass, by default $-1 / 2$.
order an integer value, the order of the moment.
type a character value, "raw" gives the moments about zero, "central" gives the central moments about the mean, and "mu" gives the moments about the location parameter mu.

## Value

a named numerical value. The name is one of mean, var, skew, or kurt, obtained by dropping the nig prefix from the name of the corresponding function and lowercasing it.
for ghMoments, the name is obtained by paste0("m", order, type).

## Author(s)

Diethelm Wuertz

## References

Scott, D. J., Wuertz, D. and Tran, T. T. (2008) Moments of the Generalized Hyperbolic Distribution. Preprint.

## Examples

```
## ghMean -
    ghMean(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)
## ghKurt -
    ghKurt(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)
## ghMoments -
    ghMoments(4,
        alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)
    ghMoments(4, "central",
        alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)
```

    ghRobMoments
    Robust Moments for the GH
    
## Description

Computes the first four robust moments for the generalized hyperbolic distribution.

## Usage

```
ghMED(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
ghIQR(alpha= 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
ghSKEW(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
ghKURT(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
```


## Arguments

| alpha | first shape parameter. |
| :--- | :--- |
| beta | second shape parameter, should in the range ( 0, alpha) . |
| delta | scale parameter, must be zero or positive. |
| mu | location parameter, by default 0. |
| lambda | defines the sublclass, by default $-1 / 2$. |

## Details

The meanings of the parameters correspond to the first parameterization, see gh for further details.

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the gh prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz.

## Examples

```
## ghMED -
    # Median:
    ghMED(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
## ghIQR -
    # Inter-quartile Range:
    ghIQR(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
## ghSKEW -
    # Robust Skewness:
    ghSKEW(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
## ghKURT -
    # Robust Kurtosis:
    ghKURT(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
```

    ghSlider Generalized Hyperbolic Distribution Slider
    
## Description

Displays interactively the dependence of the generalized hyperbolic distribution on its parameters.

## Usage

ghSlider()

## Value

a tcl/tk based graphical user interface.
This is a nice display for educational purposes to investigate the densities and probabilities of the generalized hyperbolic distribution.

## Examples

```
## ghSlider -
    # ghSlider()
```


## ght Generalized Hyperbolic Student-t distribution

## Description

Density, distribution function, quantile function and random generation for the generalized hyperbolic Student-t distribution.

## Usage

$\operatorname{dght}(x$, beta $=0.1$, delta $=1, m u=0, n u=10, \log =$ FALSE $)$
pght ( $q$, beta $=0.1$, delta $=1$, mu $=0$, nu $=10$ )
$\operatorname{qght}(\mathrm{p}$, beta $=0.1$, delta $=1, \mathrm{mu}=0, \mathrm{nu}=10)$
$\operatorname{rght}(\mathrm{n}$, beta $=0.1$, delta $=1, \mathrm{mu}=0, \mathrm{nu}=10)$

## Arguments

| $\mathrm{x}, \mathrm{q}$ | a numeric vector of quantiles. |
| :--- | :--- |
| p | a numeric vector of probabilities. |
| n | number of observations. |
| beta | numeric value, the skewness parameter in the range ( 0, alpha). |
| delta | numeric value, the scale parameter, must be zero or positive. |
| mu | numeric value, the location parameter, by default 0. |, | a numeric value, the number of degrees of freedom. Note, alpha takes the limit |
| :--- |
| of abs (beta), and lambda=-nu/2. |
| a logical, if TRUE, probabilities $p$ are given as $\log (p)$. |

## Details

dght gives the density, pght gives the distribution function, qght gives the quantile function, and rght generates random deviates.
The parameters are as in the first parameterization.

## Value

numeric vector

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.
Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.

Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
## ght -
    #
```

ghtFit GHT distribution fit

## Description

Estimates the distributional parameters for a generalized hyperbolic Student-t distribution.

## Usage

```
ghtFit(x, beta = 0.1, delta = 1, mu = 0, nu = 10,
        scale = TRUE, doplot = TRUE, span = "auto", trace = TRUE,
        title = NULL, description = NULL, ...)
```


## Arguments

beta, delta, mu numeric values. beta is the skewness parameter in the range ( 0 , alpha) ; delta is the scale parameter, must be zero or positive; mu is the location parameter, by default 0 . These are the parameters in the first parameterization.
nu
defines the number of degrees of freedom. Note, alpha takes the limit of abs(beta), and lambda=-nu/2.

X
a numeric vector.
scale a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
doplot a logical flag. Should a plot be displayed?
span $\quad x$-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001 , and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times $=n$ ), where, min and max are the left and right endpoints of the range, and $n$ gives the number of the intermediate points.
trace a logical flag. Should the parameter estimation process be traced?
title a character string which allows for a project title.
description a character string which allows for a brief description.
... parameters to be parsed.

## Details

The function nlm is used to minimize the "negative" maximum log-likelihood function. nlm carries out a minimization using a Newton-type algorithm.

## Value

an object from class "fDISTFIT".
Slot fit is a list with the following components:

| estimate | the point at which the maximum value of the log liklihood function is obtained. |
| :--- | :--- |
| minimum | the value of the estimated maximum, i.e. the value of the log liklihood function. |
| code | an integer indicating why the optimization process terminated. |
| 1: relative gradient is close to zero, current iterate is probably solution; |  |
| 2: successive iterates within tolerance, current iterate is probably solution; |  |
| 3: last global step failed to locate a point lower than estimate. Either estimate |  |
| is an approximate local minimum of the function or steptol is too small; |  |
| 4: iteration limit exceeded; |  |
| 5: maximum step size stepmax exceeded five consecutive times. Either the |  |
| function is unbounded below, becomes asymptotic to a finite value from above |  |
| in some direction or stepmax is too small. |  |
| gradient | the gradient at the estimated maximum. |
| steps | number of function calls. |

## Examples

```
## ghtFit -
    # Simulate Random Variates:
    set.seed(1953)
## ghtFit -
    # Fit Parameters:
```

ghtMode Generalized Hyperbolic Student-t Mode

## Description

Computes the mode of the generalized hyperbolic Student-t distribution.

## Usage

```
ghtMode(beta \(=0.1\), delta \(=1, \mathrm{mu}=0, \mathrm{nu}=10\) )
```


## Arguments

| beta | the skewness parameter in the range (0, alpha). |
| :--- | :--- |
| delta | the scale parameter, must be zero or positive. |
| mu | the location parameter, by default 0. | | a numeric value, the number of degrees of freedom. Note, alpha takes the limit |
| :--- |
| of abs(beta), and lambda=-nu/2. |

## Details

These are the parameters in the first parameterization.

## Value

a numeric value, the mode for the generalized hyperbolic Student-t distribution.

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.
Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.
Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
## ghtMode -
    ghtMode()
```

ghtMoments Generalized Hyperbolic Student-t Moments

## Description

Calculates moments of the generalized hyperbolic Student-t distribution.

## Usage

ghtMean(beta=0.1, delta=1, mu=0, nu=10)
ghtVar(beta=0.1, delta=1, mu=0, nu=10)
ghtSkew(beta=0.1, delta=1, mu=0, nu=10)
ghtKurt (beta=0.1, delta=1, mu=0, nu=10)
ghtMoments(order, type = c("raw", "central", "mu"), beta=0.1, delta=1, mu=0, nu=10)

## Arguments

\(\left.\begin{array}{ll}beta \& numeric value, the skewness parameter in the range ( 0, alpha). <br>
delta \& numeric value, the scale parameter, must be zero or positive. <br>

mu \& numeric value, the location parameter, by default 0 .\end{array}\right\}\)| a numeric value, the number of degrees of freedom. Note, alpha takes the limit |
| :--- |
| of abs (beta), and lambda=-nu/2. |
| order |
| type | | an integer value, the order of the moment. |
| :--- |
| a character string, "raw" returns the moments about zero, "central" returns |
| the central moments about the mean, and "mu" returns the moments about the |
| location parameter mu. |

## Value

a named numerical value. The name is one of mean, var, skew, or kurt, obtained by dropping the nig prefix from the name of the corresponding function and lowercasing it.
for ghtMoments, the name is obtained by paste0("m", order, type).

## Author(s)

Diethelm Wuertz

## References

Scott, D.J., Wuertz, D. and Tran, T.T. (2008) Moments of the Generalized Hyperbolic Distribution. Preprint.

## Examples

```
## ghtMean -
    ghtMean(beta=0.2, delta=1.2, mu=-0.5, nu=4)
## ghtKurt -
    ghtKurt(beta=0.2, delta=1.2, mu=-0.5, nu=4)
## ghtMoments -
    ghtMoments(4,
        beta=0.2, delta=1.2, mu=-0.5, nu=4)
    ghtMoments(4, "central",
        beta=0.2, delta=1.2, mu=-0.5, nu=4)
```

ghtRobMoments Robust Moments for the GHT

## Description

Computes the first four robust moments for the generalized hyperbolic Student-t.

## Usage

```
ghtMED(beta = 0.1, delta = 1, mu = 0, nu = 10)
ghtIQR(beta = 0.1, delta = 1, mu = 0, nu = 10)
ghtSKEW(beta = 0.1, delta = 1, mu = 0, nu = 10)
ghtKURT(beta = 0.1, delta = 1, mu = 0, nu = 10)
```


## Arguments

beta skewness parameter in the range ( 0 , alpha).
delta scale parameter, must be zero or positive.
mu location parameter, by default 0.
nu a numeric value, the number of degrees of freedom. Note, alpha takes the limit of abs(beta), and lambda=-nu/2.

## Details

The parameters are those of the first parameterization.

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the ght prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz.

## Examples

```
## ghtMED -
    # Median:
    ghtMED(beta = 0.1, delta = 1, mu = 0, nu = 10)
## ghtIQR -
    # Inter-quartile Range:
    ghtIQR(beta = 0.1, delta = 1, mu = 0, nu = 10)
## ghtSKEW -
    # Robust Skewness:
    ghtSKEW(beta = 0.1, delta = 1, mu = 0, nu = 10)
```

```
    ## ghtKURT -
    # Robust Kurtosis:
    ghtKURT(beta = 0.1, delta = 1, mu = 0, nu = 10)
```

    gld Generalized Lambda Distribution
    
## Description

Density, distribution function, quantile function and random generation for the generalized lambda distribution.

## Usage

dgld(x, lambda1 = 0, lambda2 $=-1$, lambda3 $=-1 / 8$, lambda4 $=-1 / 8, \log =$ FALSE)
pgld(q, lambda1 $=0$, lambda2 $=-1$, lambda3 $=-1 / 8$, lambda4 $=-1 / 8$ )
qgld(p, lambda1 $=0$, lambda2 $=-1$, lambda3 $=-1 / 8$, lambda4 $=-1 / 8$ )
$\operatorname{rgld}(\mathrm{n}, \operatorname{lambda1}=0, \operatorname{lambda2}=-1, \operatorname{lambda3}=-1 / 8$, lambda4 $=-1 / 8$ )

## Arguments

| lambda1 | location parameter. |
| :--- | :--- |
| lambda2 | scale parameter. |
| lambda3 | first shape parameter. |
| lambda4 | second shape parameter. |
| n | number of observations. |
| p | a numeric vector of probabilities. |
| $\mathrm{x}, \mathrm{q}$ | a numeric vector of quantiles. |
| $\log$ | a logical, if TRUE, probabilities p are given as $\log (\mathrm{p})$. |

## Details

dgld gives the density, pgld gives the distribution function, qgld gives the quantile function, and rgld generates random deviates.

## Value

numeric vector

## Author(s)

Chong Gu for code implemented from R's contributed package gld.

## Examples

```
    ## rgld -
    set.seed(1953)
    r = rgld(500,
        lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8)
    plot(r, type = "l", col = "steelblue",
        main = "gld: lambda1=0 lambda2=-1 lambda3/4=-1/8")
## dgld -
    # Plot empirical density and compare with true density:
    hist(r, n = 25, probability = TRUE, border = "white",
        col = "steelblue")
    x = seq(-5, 5, 0.25)
    lines(x, dgld(x,
        lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8))
## pgld -
    # Plot df and compare with true df:
    plot(sort(r), ((1:500)-0.5)/500, main = "Probability",
        col = "steelblue")
    lines(x, pgld(x,
        lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8))
## qgld -
    # Compute Quantiles:
    qgld(pgld(seq(-5, 5, 1),
        lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8),
        lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8)
```

    gldFit GH Distribution Fit
    
## Description

Estimates the distrinbutional parameters for a generalized lambda distribution.

## Usage

```
gldFit(x, lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8,
    method = c("mle", "mps", "gof", "hist", "rob"),
    scale = NA, doplot = TRUE, add = FALSE, span = "auto", trace = TRUE,
    title \(=\) NULL, description \(=\) NULL, ...)
```


## Arguments

a numeric vector.
lambda1, lambda2, lambda3, lambda4
are numeric values where lambda1 is the location parameter, lambda2 is the
location parameter, lambda3 is the first shape parameter, and lambda4 is the
second shape parameter.
method
a character string, the estimation approach to fit the distributional parameters,
see details.
scale
doplot used.
add

span $\quad$| a logical flag. Should a plot be displayed? |
| :--- |
| a logical flag. Should a new fit added to an existing plot? |
| x-coordinates for the plot, by default 100 values automatically selected and rang- |
| ing between the 0.001, and 0.999 quantiles. Alternatively, you can specify the |
| range by an expression like span=seq(min, max, times = $n$ ), where, min and |
| max are the left and rigldt endpoints of the range, and $n$ gives the number of the |
| intermediate points. |

## Details

The function nlminb is used to minimize the objective function. The following approaches have been implemented:
"mle", maximimum log likelihoo estimation.
"mps", maximum product spacing estimation.
"gof", goodness of fit approaches, type="ad" Anderson-Darling, type="cvm" Cramer-vonMise, type="ks" Kolmogorov-Smirnov.
"hist", histogram binning approaches, "fd" Freedman-Diaconis binning, "scott", Scott histogram binning, "sturges", Sturges histogram binning.
"rob", robust moment matching.

## Value

an object from class "fDISTFIT".
Slot fit is a list with the following components:
estimate the point at which the maximum value of the log liklihood function is obtained.
minimum the value of the estimated maximum, i.e. the value of the $\log$ liklihood function.
code an integer indicating why the optimization process terminated.
1: relative gradient is close to zero, current iterate is probably solution;
2: successive iterates within tolerance, current iterate is probably solution;
3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small;
4: iteration limit exceeded;

5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient the gradient at the estimated maximum.
steps number of function calls.

## Examples

```
## gldFit -
    # Simulate Random Variates:
    set.seed(1953)
    s = rgld(n = 1000, lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8)
## gldFit -
    # Fit Parameters:
    gldFit(s, lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8,
        doplot = TRUE, trace = TRUE)
```

    gldMode Generalized Lambda Distribution Mode
    
## Description

Computes the mode of the generalized lambda distribution.

## Usage

gldMode(lambda1 $=0, \operatorname{lambda} 2=-1$, lambda3 $=-1 / 8, \operatorname{lambda4}=-1 / 8)$

## Arguments

| lambda1 | location parameter. |
| :--- | :--- |
| lambda2 | scale parameter. |
| lambda3 | first shape parameter. |
| lambda4 | second shape parameter. |

## Author(s)

Implemented by Diethelm Wuertz

## gldRobMoments Robust Moments for the GLD

## Description

Computes the first four robust moments for the Generalized Lambda Distribution.

## Usage

```
gldMED(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
gldIQR(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
gldSKEW(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
gldKURT(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
```


## Arguments

| lambda1 | location parameter |
| :--- | :--- |
| lambda2 | scale parameter |
| lambda3 | first shape parameter |
| lambda4 | second shape parameter |

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the gld prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz.

## Examples

```
## gldMED -
    # Median:
    gldMED(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
## gldIQR -
    # Inter-quartile Range:
    gldIQR(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
## gldSKEW -
    # Robust Skewness:
    gldSKEW(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
## gldKURT -
    # Robust Kurtosis:
    gldKURT(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
```

```
gridVector Grid vector coordinates
```


## Description

Creates rectangular grid coordinates from two vectors.

## Usage

gridVector $(x, y=N U L L)$

## Arguments

$\mathrm{x}, \mathrm{y} \quad$ numeric vectors

## Details

The grid is obtained by pairing each element of $y$ with all elements of $x$. The $X$ and $Y$ coordinates of the points are stored in separate vectors. This is convenient, for example, for plotting. It can be useful also for brute force optimisation or simulation.

If y is NULL, the default, then $\mathrm{y}=\mathrm{x}$.

## Value

a list with two components, X and Y , giving the coordinates which span the bivariate grid.

## See Also

expand.grid

## Examples

```
## a small grid vector with row and col transformations
gridVector(0:2)
data.frame(gridVector(0:2))
do.call("rbind", gridVector(0:2))
gridVector(0:2, 0:3)
## grid over a unit square
gridVector((0:10)/10) # equivalently: gridVector((0:10)/10, (0:10)/10)
```

Heaviside Heaviside and related functions

## Description

Functions which compute the Heaviside and related functions. These include the Heaviside function, the sign function, the delta function, the boxcar function, and the ramp function.

## Usage

Heaviside(x, a = 0)
Sign $(x, a=0)$
Delta(x, a = 0)
Boxcar (x, a = 0.5)
$\operatorname{Ramp}(x, a=0)$

## Arguments

$x \quad$ a numeric vector.
a a numeric value, the location of the break.

## Details

Heaviside computes the Heaviside unit step function. Heaviside is 1 for $x>a, 1 / 2$ for $x=a$, and 0 for $\mathrm{x}<\mathrm{a}$.
Sign computes the sign function. Sign is 1 for $x>a, 0$ for $x=a$, and -1 for $x<a$.
Delta computes the delta function. Delta is defined as: Delta $(x)=d / d x H(x-a)$.
Boxcar computes the boxcar function. Boxcar is defined as: Boxcar $(x)=H(x+a)-H(x-a)$.
Ramp computes ramp function. The ramp function is defined as: $\operatorname{Ramp}(x)=(x-a) * H(x-a)$.

## Value

numeric vector

## Note

The Heaviside function is used in the implementation of the skew Normal, Student-t, and Generalized Error distributions, distributions functions which play an important role in modelling GARCH processes.

## References

Weisstein W. (2004); http://mathworld.wolfram.com/HeavisideStepFunction.html, Mathworld.

See Also
GarchDistribution, GarchDistributionFits

## Examples

```
## Heaviside -
    x = sort(round(c(-1, -0.5, 0, 0.5, 1, 5*rnorm(5)), 2))
    h = Heaviside(x)
## Sign -
    s = Sign(x)
## Delta -
    d = Delta(x)
## Boxcar -
    Pi = Boxcar(x)
## Ramp -
    r = Ramp(x)
    cbind(x = x, Step = h, Signum = s, Delta = d, Pi = Pi, R = r)
```

    hilbert Hilbert matrix
    
## Description

Creates a Hilbert matrix.

## Usage

hilbert(n)

## Arguments

n
an integer value, the dimension of the square matrix.

## Details

An $n, n$ matrix with $(i, j)$ th element equal to $1 /(i+j-1)$ is said to be a Hilbert matrix of order $n$. Hilbert matrices are symmetric and positive definite.
They are canonical examples of ill-conditioned matrices, making them notoriously difficult to use in numerical computation. For example, the 2-norm condition number of a $5 \times 5$ Hilbert matrix above is about 4.8e5.

## Value

a matrix

## References

Hilbert D., Collected papers, vol. II, article 21.
Beckermann B, (2000); The condition number of real Vandermonde, Krylov and positive definite Hankel matrices, Numerische Mathematik 85, 553-577, 2000.

Choi, M.D., (1983); Tricks or Treats with the Hilbert Matrix, American Mathematical Monthly 90, 301-312, 1983.
Todd, J., (1954); The Condition Number of the Finite Segment of the Hilbert Matrix, National Bureau of Standards, Applied Mathematics Series 39, 109-116.

Wilf, H.S., (1970); Finite Sections of Some Classical Inequalities, Heidelberg, Springer.

## Examples

```
## Create a Hilbert Matrix:
    H = hilbert(5)
    H
```

HistogramPlot Histogram and density plots

## Description

Produce tailored histogram plots and kernel density/log-density estimate plots.

## Usage

```
histPlot(x, labels = TRUE, col = "steelblue", fit = TRUE,
    title = TRUE, grid = TRUE, rug = TRUE, skip = FALSE, ...)
densityPlot(x, labels = TRUE, col = "steelblue", fit = TRUE, hist = TRUE,
    title = TRUE, grid = TRUE, rug = TRUE, skip = FALSE, ...)
logDensityPlot(x, labels = TRUE, col = "steelblue", robust = TRUE,
    title = TRUE, grid = TRUE, rug = TRUE, skip = FALSE, ...)
```


## Arguments

X
labels a logical flag, should the plot be returned with default labels and decorated in an automated way? By default TRUE.
col the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat.colors (ncol(x)).
fit
hist
title a logical flag, should a fit be added to the plot?
a logical flag, by default TRUE. Should a histogram be laid under the plot?
a logical flag, by default TRUE. Should a default title be added to the plot?

| grid | a logical flag, should a grid be added to the plot? By default TRUE. To plot a <br> horizontal lines only use grid=" $h "$ and for vertical lines use grid=" $\mathrm{h} "$, respec- <br> tively. |
| :--- | :--- |
| rug | a logical flag, by default TRUE. Should a rug representation of the data be added <br> to the plot? |
| skip | a logical flag, should zeros be skipped in the return Series? |
| robust | a logical flag, by default TRUE. Should a robust fit be added to the plot? |
| $\ldots$ | optional arguments to be passed on. |

## Details

histPlot produces a tailored histogram plot.
densityPlot produces a tailored kernel density estimate plot.
logDensityPlot produces a tailored log kernel density estimate plot.

## Value

NULL, invisibly. The functions are used for the side effect of producing a plot.

## Examples

```
## data -
    data(LPP2005REC, package = "timeSeries")
    SPI <- LPP2005REC[, "SPI"]
    plot(SPI, type = "l", col = "steelblue", main = "SP500")
    abline(h = 0, col = "grey")
## histPlot -
    histPlot(SPI)
## densityPlot -
    densityPlot(SPI)
```

hyp
Hyperbolic distribution

## Description

Density, distribution function, quantile function and random generation for the hyperbolic distribution.

## Usage

```
dhyp(x, alpha = 1, beta = 0, delta = 1, mu = 0, pm = 1, log = FALSE)
phyp(q, alpha = 1, beta = 0, delta = 1, mu = 0, pm = 1, ...)
qhyp(p, alpha = 1, beta = 0, delta = 1, mu = 0, pm = 1, ...)
rhyp(n, alpha = 1, beta = 0, delta = 1, mu = 0, pm = 1)
```


## Arguments

| $\mathrm{x}, \mathrm{q}$ | numeric vector of quantiles. |
| :---: | :---: |
| p | numeric vector of probabilities. |
| n | number of observations. |
| alpha | shape parameter, a positive number. alpha can also be a vector of length four, containing alpha, beta, delta and mu (in that order). |
| beta | skewness parameter, abs(beta) is in the range (0, alpha). |
| delta | scale parameter, must be zero or positive. |
| mu | location parameter, by default 0 . |
| pm | integer number specifying the parameterisation, one of $1,2,3$, or 4 . The default is the first parameterization. |
| $\log$ | a logical value, if TRUE, probabilities $p$ are given as $\log (p)$. |
|  | arguments to be passed to the function integrate. |

## Details

dhyp gives the density, phyp gives the distribution function, qhyp gives the quantile function, and rhyp generates random deviates.
The meaning of the parameters given above corresponds to the first parameterization, $\mathrm{pm}=1$, which is the default.

In the second parameterization, $\mathrm{pm}=2$, alpha and beta take the meaning of the shape parameters (usually named) zeta and rho.
In the third parameterization, $\mathrm{pm}=3$, alpha and beta take the meaning of the shape parameters (usually named) xi and chi.
In the fourth parameterization, $\mathrm{pm}=4$, alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.
The generator rhyp is based on the HYP algorithm given by Atkinson (1982).

## Value

numeric vector

## Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.
Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.

Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
## hyp -
    set.seed(1953)
    r= rhyp(5000, alpha = 1, beta = 0.3, delta = 1)
    plot(r, type = "l", col = "steelblue",
        main = "hyp: alpha=1 beta=0.3 delta=1")
## hyp -
    # Plot empirical density and compare with true density:
    hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
    x = seq(-5, 5, 0.25)
    lines(x, dhyp(x, alpha = 1, beta = 0.3, delta = 1))
## hyp -
    # Plot df and compare with true df:
    plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
    lines(x, phyp(x, alpha = 1, beta = 0.3, delta = 1))
## hyp -
    # Compute Quantiles:
    qhyp(phyp(seq(-5, 5, 1), alpha = 1, beta = 0.3, delta = 1),
        alpha = 1, beta = 0.3, delta = 1)
```

hypFit Fit a Hyperbolic distribution

## Description

Estimates the parameters of a hyperbolic distribution.

## Usage

```
hypFit(x, alpha = 1, beta = 0, delta = 1, mu = 0,
    scale = TRUE, doplot = TRUE, span = "auto", trace = TRUE,
    title = NULL, description = NULL, ...)
```


## Arguments

x
alpha
beta skewness parameter, abs(beta) is in the range (0, alpha).
delta scale parameter, must be zero or positive.

| mu | location parameter, by default 0 . |
| :---: | :---: |
| scale | a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization? |
| doplot | a logical flag. Should a plot be displayed? |
| span | x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001 , and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq( $\min$, max, times $=n$ ), where, min and max are the left and right endpoints of the range, and $n$ gives the number of the intermediate points. |
| trace | a logical flag. Should the parameter estimation process be traced? |
| title | a character string which allows for a project title. |
| description | a character string which allows for a brief description. |
|  | parameters to be parsed. |

## Details

The meaning of the parameters given above corresponds to the first parameterization, see dhyp for details.
The function nlm is used to minimize the "negative" maximum log-likelihood function. nlm carries out a minimization using a Newton-type algorithm.

## Value

an object from class "fDISTFIT". Slot fit is a list with the following components:
estimate the point at which the maximum value of the log liklihood function is obtained.
minimum the value of the estimated maximum, i.e. the value of the $\log$ liklihood function.
code an integer indicating why the optimization process terminated.
1: relative gradient is close to zero, current iterate is probably solution;
2: successive iterates within tolerance, current iterate is probably solution;
3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small;
4: iteration limit exceeded;
5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient the gradient at the estimated maximum.
steps number of function calls.

## Examples

```
## rhyp -
    # Simulate Random Variates:
    set.seed(1953)
    s = rhyp(n = 1000, alpha = 1.5, beta = 0.3, delta = 0.5, mu = -1.0)
```

```
## hypFit -
    # Fit Parameters:
    hypFit(s, alpha = 1, beta = 0, delta = 1, mu = mean(s), doplot = TRUE)
```

hypMode Hyperbolic mode

## Description

Computes the mode of the hyperbolic distribution.

## Usage

hypMode(alpha $=1$, beta $=0$, delta $=1, \mathrm{mu}=0, \mathrm{pm}=1$ )

## Arguments

alpha shape parameter, a positive number. alpha can also be a vector of length four, containing alpha, beta, delta and mu (in that order).
beta skewness parameter, abs(beta) is in the range ( 0, alpha).
delta scale parameter, must be zero or positive.
$\mathrm{mu} \quad$ location parameter, by default 0 .
$\mathrm{pm} \quad$ an integer value between 1 and 4 for the selection of the parameterization. The default takes the first parameterization.

## Value

a numeric value, the mode in the appropriate parameterization for the hyperbolic distribution.

## Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.

Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.
Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
    ## hypMode -
    hypMode()
```

hypMoments

Hyperbolic distribution moments

## Description

Calculates moments of the hyperbolic distribution function.

## Usage

hypMean(alpha=1, beta=0, delta=1, mu=0)
hypVar(alpha=1, beta=0, delta=1, mu=0)
hypSkew(alpha=1, beta=0, delta=1, mu=0)
hypKurt(alpha=1, beta=0, delta=1, mu=0)
hypMoments(order, type = c("raw", "central", "mu"),
alpha=1, beta=0, delta=1, mu=0)

## Arguments

| alpha | numeric value, the first shape parameter. |
| :--- | :--- |
| beta | numeric value, the second shape parameter in the range ( 0, alpha). |
| delta | numeric value, the scale parameter, must be zero or positive. |
| mu | numeric value, the location parameter, by default 0. |
| order | an integer value, the order of the moment. |
| type | a character string, "raw" returns the moments about zero, "central" returns <br> the central moments about the mean, and "mu" returns the moments about the <br> location parameter mu. |

## Value

a named numerical value. The name is one of mean, var, skew, or kurt, obtained by dropping the hyp prefix from the name of the corresponding function and lowercasing it.
for hypMoments, the name is obtained by paste0 ("m", order, type).

## Author(s)

Diethelm Wuertz

## References

Scott, D. J., Wuertz, D. and Tran, T. T. (2008) Moments of the Generalized Hyperbolic Distribution. Preprint.

## Examples

```
## hypMean -
    hypMean(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)
## ghKurt -
    hypKurt(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)
## hypMoments -
    hypMoments(4, alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)
    hypMoments(4, "central", alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)
```

hypRobMoments Robust moments for the HYP

## Description

Computes the first four robust moments for the hyperbolic distribution.

## Usage

$\operatorname{hypMED}($ alpha $=1$, beta $=0$, delta $=1$, mu $=0)$
$\operatorname{hypIQR}(a l p h a=1$, beta $=0$, delta $=1$, mu = 0)
hypSKEW(alpha $=1$, beta $=0$, delta $=1$, mu = 0)
hypKURT(alpha $=1$, beta $=0$, delta $=1$, mu $=0$ )

## Arguments

alpha shape parameter, a positive number. alpha can also be a vector of length four, containing alpha, beta, delta and mu (in that order).
beta skewness parameter, abs (beta) is in the range ( 0 , alpha).
delta scale parameter, must be zero or positive.
$\mathrm{mu} \quad$ location parameter, by default 0.

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the hyp prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz

## Examples

```
## hypMED -
    # Median:
    hypMED(alpha = 1, beta = 0, delta = 1, mu = 0)
## hypIQR -
    # Inter-quartile Range:
    hypIQR(alpha = 1, beta = 0, delta = 1, mu = 0)
## hypSKEW -
    # Robust Skewness:
    hypSKEW(alpha = 1, beta = 0, delta = 1, mu = 0)
## hypKURT -
    # Robust Kurtosis:
    hypKURT(alpha = 1, beta = 0, delta = 1, mu = 0)
```

    hypSlider Hyperbolic distribution slider
    
## Description

Displays interactively the dependence of the hyperbolic distribution on its parameters.

## Usage

hypSlider()

## Value

a tcl/tk based graphical user interface.
This is a nice display for educational purposes to investigate the densities and probabilities of the hyperbolic distribution.

## Examples

```
## hypSlider -
```

    \#
    ```
    Ids Set and retrieve column/row names
```


## Description

Sets and retrieves column and row names. The functions are for compatibility with SPlus.

## Usage

```
collds(x, ...)
```

rowIds(x, ...)

## Arguments

x
a numeric matrix.
... passed on to colnames or rownames.

## Details

Usually in R the functions colnames and rownames are used to retrieve and set the names of matrices. The functions rowIds and colIds, are S-Plus like synonyms.

## Examples

```
## pascal -
    # Create Pascal Matrix:
    P = pascal(3)
    P
## rownames -
    rownames(P) <- letters[1:3]
    P
## colIds<- -
    colIds(P) <- as.character(1:3)
    P
```

    interactivePlot Interactive Plot Utility
    
## Description

Plots with emphasis on interactive plots.

## Usage

interactivePlot(x, choices = paste("Plot", 1:9), plotFUN = paste("plot.", 1:9, sep = ""), which = "all", ...)

## Arguments

plotFUN a vector of the same length as choices, containing functions and/or names

X
choices
which
which
an object to be plotted.
a character vector of length at most 9 , giving descriptive names of the plots for the menu presented to the user. of functions. plotFUN[[i]] is called to produce the plot corresponding to choice[i].
Which graph(s) should be displayed? One of the character strings "ask" (ask the user) or "all" (produce all plots), or a logical vector in which the positions of the TRUE values designating the plots to produce.
... additional arguments passed to the FUN or plot function. (2023-10-21 GNB: currently the " . . " arguments are not really passed on to the plotting functions.)

## Details

If "which" is the character string "ask", then the user is presented with a menu to interactively choose which plot(s) to show. Argument choices is used for the choices in the menu, so they should be informative.
If "which" is equal to "all" all plots are drawn. If "which" is a logical vector, the indicate plots are displayed.
Note that if more plots are to be shown in one window, the arrangement should be made in advance (and cleaned up afterwards), see the examples.

## Examples

```
## Test Plot Function:
    testPlot = function(x, which = "all", ...) {
        # Plot Function and Addons:
        plot.1 <<- function(x, ...) plot(x, ...)
        plot.2 <<- function(x, ...) acf(x, ...)
        plot.3 <<- function(x, ...) hist(x, ...)
        plot.4 <<- function(x, ...) qqnorm(x, ...)
        # Plot:
        interactivePlot(x,
            choices = c("Series Plot", "ACF", "Histogram", "QQ Plot"),
            plotFUN = c("plot.1", "plot.2", "plot.3", "plot.4"),
            which = which, ...)
        # Return Value:
        invisible()
    }
## Plot:
    # prepare the window and store its previous state
    op <- par(mfrow = c(2, 2), cex = 0.7)
    # produce the plot
    testPlot(rnorm(500))
    # restore the previous state
    par(op)
    # Try:
```

```
    # par(mfrow = c(1,1))
    # testPlot(rnorm(500), which = "ask")
    ## similar to above but using functions for plotFUN
    testPlot_2 = function(x, which = "all", ...) {
        interactivePlot(x,
            choices = c("Series Plot", "ACF", "Histogram", "QQ Plot"),
            plotFUN = c(plot.1 = function(x, ...) plot(x, ...),
                        plot.2 = function(x, ...) acf(x, ...),
                        plot. }3\mathrm{ = function(x, ...) hist(x, ...),
                        plot.4 = function(x, ...) qqnorm(x, ...) ),
        which = which, ...)
        # Return Value:
        invisible()
    }
    # produce the plot
    op <- par(mfrow = c(2, 2), cex = 0.7)
    testPlot_2(rnorm(500))
    par(op)
```


## Description

Computes the inverse of a matrix.

## Usage

```
    inv(x)
```


## Arguments

## x

a numeric matrix.

## Value

a matrix

## References

Golub, van Loan, (1996); Matrix Computations, 3rd edition. Johns Hopkins University Press.

## Examples

```
## Create Pascal Matrix:
    P = pascal(5)
    P
## Compute the Inverse Matrix:
    inv(P)
## Check:
    inv(P) %*% P
## Alternatives:
    chol2inv(chol(P))
    solve(P)
```

krigeInterp Bivariate Krige Interpolation

## Description

Bivariate Krige Interpolation.

## Usage

krigeInterp (x, y = NULL, z = NULL, gridPoints = 21, xo $=\operatorname{seq}(\min (x), \max (x)$, length $=$ gridPoints $)$, yo $=\operatorname{seq}(\min (y), \max (y)$, length $=$ gridPoints), extrap $=$ FALSE, polDegree $=6$ )

## Arguments

| $x, y, z$ | the arguments $x$ and $y$ are two numeric vectors of grid pounts, and $z$ is a numeric <br> matrix or any other rectangular object which can be transformed by the function <br> as.matrix into a matrix object. |
| :--- | :--- |
| gridPoints | an integer value specifying the number of grid points in $x$ and $y$ direction. |
| xo, yo | two numeric vectors of data points spanning the grid. |
| extrap | a logical, if TRUE then the data points are extrapolated. |
| polDegree | the polynomial krige degree, an integer ranging between 1 and 6. |

## Value

a list with at least three entries, $x, y$ and $z$. The returned values can be used directly in persp and contour 3D plotting methods.

## Note

krigeInterp() requires package spatial.

## See Also

akimaInterp, linearInterp.

## Examples

```
## The akima library is not auto-installed because of a different licence.
## krigeInterp - Kriging:
set.seed(1953)
x = runif(999) - 0.5
y = runif(999) - 0.5
z = cos(2*pi* (x^2+\mp@subsup{y}{}{\wedge}2))
ans = krigeInterp(x, y, z, extrap = FALSE)
persp(ans, theta = -40, phi = 30, col = "steelblue",
    xlab = "x", ylab = "y", zlab = "z")
    contour(ans)
```

    kron Kronecker product
    
## Description

Computes the Kronecker product of two matrices.

## Usage

kron(x, y)

## Arguments

$\mathrm{x}, \mathrm{y} \quad$ numeric matrices.

## Details

The Kronecker product can be computed using the operator \%x\% or alternatively using the function kron for SPlus compatibility.

## Note

kron is a synonym to $\% \mathrm{x} \%$.

## References

Golub, van Loan, (1996); Matrix Computations, 3rd edition. Johns Hopkins University Press.

## Examples

```
    ## Create Pascal Matrix:
        P = pascal(3)
    P
    ## Return the Kronecker Product
    kron(P, diag(3))
    P %x% diag(3)
```

ks2Test Two sample Kolmogorov-Smirnov test

## Description

Tests if two series are distributionally equivalent using two sample Kolmogorov-Smirnov test.

## Usage

ks2Test(x, y, title = NULL, description = NULL)

## Arguments

$\mathrm{x}, \mathrm{y} \quad$ numeric vectors of data values.
title an optional title string, if not specified the inputs data name is deparsed.
description optional description string, or a vector of character strings.

## Details

The test ks2Test performs a Kolmogorov-Smirnov two sample test that the two data samples, x and $y$, come from the same distribution, not necessarily a normal distribution. That means that it is not specified what that common distribution is.
ks2Test calls several times base R's ks. test p-values for all three alternatives (two-sided, less, and greater), as well as the exact p-value for the two-sided case.
Note that the p-values are computed under a hypothesis of i.i.d., which is rarely the case for time series. So, the results should be interpreted cautiosly if that is the case. The same applies when the data are residuals from fitted models.

## Value

an object from class fHTEST

## References

Conover, W. J. (1971); Practical nonparametric statistics, New York: John Wiley \& Sons.
Lehmann E.L. (1986); Testing Statistical Hypotheses, John Wiley and Sons, New York.

## Examples

```
    ## rnorm -
    # Generate Series:
    x = rnorm(50)
    y = rnorm(50)
## ks2Test -
    ks2Test(x, y)
```

    lcg
    Generator for Portable random innovations

## Description

Functions to generate portable random innovations. The functions run under R and S-Plus and generate the same sequence of random numbers. Supported are uniform, normal and Student-t distributed random numbers.

The functions are:

| set.lcgseed | Set initial random seed, |
| :--- | :--- |
| get.lcgseed | Get the current valus of the random seed, |
| runif.lcg | Uniform linear congruational generator, |
| rnorm.lcg | Normal linear congruational generator, |
| rt.lcg | Student-t linear congruential generator. |

## Usage

set.lcgseed(seed $=4711$ )
get.lcgseed()
runif.lcg(n, min $=0, \max =1$ )
rnorm.lcg(n, mean $=0, s d=1)$
rt.lcg(n, df)

## Arguments

seed an integer value, the random number seed.
$\mathrm{n} \quad$ an integer, the number of random innovations to be generated.
df degrees of freedom, a positive number, may be non-integer.
mean, sd mean and standard deviation of the normally distributed innovations.
$\min , \max \quad$ lower and upper limits of the uniformly distributed innovations.

## Details

A simple portable random number generator for use in R and SPlus. We recommend to use this generator only for comparisons of calculations in R and Splus.
The generator is a linear congruential generator with parameters LCG( $a=13445, c=0, m=2^{\wedge} 31-1$, $X=0$ ). It is a simple random number generator which passes the bitwise randomness test.

## Value

A vector of generated random innovations. The value of the current seed is stored in the variable lcg.seed.

## References

Altman, N.S. (1988); Bitwise Behavior of Random Number Generators, SIAM J. Sci. Stat. Comput., 9(5), September, 941-949.

## Examples

```
## set.lcgseed -
    set.lcgseed(seed = 65890)
## runif.lcg - rnorm.lcg - rt.lcg -
    cbind(runif.lcg(10), rnorm.lcg(10), rt.lcg(10, df = 4))
## get.lcgseed -
    get.lcgseed()
## Note, to overwrite rnorm, use
    # rnorm = rnorm.lcg
    # Going back to rnorm
    # rm(rnorm)
```

linearInterp Bivariate Linear Interpolation

## Description

Bivariate Linear Interpolation. Options are available for gridded and pointwise interpolation.

## Usage

```
linearInterp(x, y = NULL, z = NULL, gridPoints = 21,
    xo = seq(min(x), max(x), length = gridPoints),
    yo = seq(min(y), max(y), length = gridPoints))
linearInterpp(x, y = NULL, z = NULL, xo, yo)
```


## Arguments

$x, y, z \quad$ for linearInterp the arguments $x$ and $y$ are two numeric vectors of grid pounts, and $z$ is a numeric matrix or any other rectangular object which can be transformed by the function as .matrix into a matrix object. For linearInterpp we consider either three numeric vectors of equal length or if $y$ and $z$ are NULL, a list with entries $x, y, z$, or named data frame with $x$ in the first, $y$ in the second, and $z$ in the third column.
gridPoints an integer value specifying the number of grid points in $x$ and $y$ direction.
xo, yo for linearInterp two numeric vectors of data points spanning the grid, and for linearInterpp two numeric vectors of data points building pairs for pointwise interpolation.

## Value

for linearInterp, a list with at least three entries, $x, y$ and $z$. The returned values, can be used directly in persp and contour 3D plotting methods.
for linearInterpp, a data.frame with columns "x", "y", and "z".

## See Also

akimaInterp and krigeInterp

## Examples

```
## linearInterp -
    # Linear Interpolation:
    if (requireNamespace("interp")) {
        set.seed(1953)
        x = runif(999) - 0.5
        y = runif(999) - 0.5
        z = cos(2*pi*(x^2+y^2))
        ans = linearInterp(x, y, z, gridPoints = 41)
        persp(ans, theta = 40, phi = 30, col = "steelblue",
            xlab = "x", ylab = "y", zlab = "z")
        contour(ans)
    }
```

listFunctions List exported functions in a package

## Description

Utilities to list and count exported functions in a package, list the contents of the description file of a package, and
Prints the content of an index file for a package (a list of the objects exported by a package).

## Usage

listFunctions(package, character.only = FALSE)
countFunctions(package, character.only = FALSE)
listIndex(package, character.only = FALSE)

## Arguments

package a literal character string or a character string denoting the name of a package.
character. only a logical indicating whether 'package' can be assumed to be a character string.

## Value

for listFunctions, a character vector containing the names of the exported functions in a package, for countFunctions, a named numeric value giving the number of the exported functions in a package.
listIndex doesn't return a useful value. It is used for the side effect of printing the description or index.

## Note

Be aware that listFunctions and countFunctions attach the package to the search path.

## See Also

```
packageDescription
```


## Examples

```
## listFunctions -
    listFunctions("fBasics")
## countFunctions -
    countFunctions("fBasics")
```

locationTest Two sample location tests

## Description

Tests if two series differ in their distributional location parameter.

## Usage

locationTest(x, y, method = c("t", "kw2"), title = NULL, description $=$ NULL)

## Arguments

$x, y \quad$ numeric vectors of data values.
method a character string naming which test should be applied.
title an optional title string, if not specified the input's data name is deparsed.
description optional description string, or a vector of character strings.

## Details

The method = " $t$ " can be used to determine if the two sample means are equal for unpaired data sets. Two variants are used, assuming equal or unequal variances.

The method = "kw2" performs a Kruskal-Wallis rank sum test of the null hypothesis that the central tendencies or medians of two samples are the same. The alternative is that they differ. Note, that it is not assumed that the two samples are drawn from the same distribution. It is also worth to know that the test assumes that the variables under consideration have underlying continuous distributions.

## Value

an object from class fHTEST

## Note

Some of the test implementations are selected from R's ctest package.

## Author(s)

R-core team for hypothesis tests implemented from R's package ctest.

## References

Conover, W. J. (1971); Practical nonparametric statistics, New York: John Wiley \& Sons.
Lehmann E.L. (1986); Testing Statistical Hypotheses, John Wiley and Sons, New York.

## Examples

```
## rnorm -
    # Generate Series:
    x = rnorm(50)
    y = rnorm(50)
## locationTest -
    locationTest(x, y, "t")
    locationTest(x, y, "kw2")
```


## Description

A collection of functions which compute drawdown statistics. Included are density, distribution function, and random generation for the maximum drawdown distribution. In addition the expectation of drawdowns for Brownian motion can be computed.

## Usage

dmaxdd(x, sd $=1$, horizon $=100, \mathrm{~N}=1000)$
$\operatorname{pmaxdd}(\mathrm{q}, \mathrm{sd}=1$, horizon $=100, \mathrm{~N}=1000$ )
rmaxdd(n, mean $=0, s d=1$, horizon $=100$ )
maxddStats (mean $=0$, sd $=1$, horizon $=1000$ )

## Arguments

$x, q \quad a \quad$ numeric vector of quantiles.
$\mathrm{n} \quad$ an integer value, the number of observations.
mean, sd two numeric values, the mean and standard deviation.
horizon an integer value, the (run time) horizon of the investor.
$\mathrm{N} \quad$ an integer value, the precession index for summations. Before you change this value please inspect Magdon-Ismail et. al. (2003).

## Details

dmaxdd computes the density function of the maximum drawdown distribution. pmaxdd computes the distribution function. rmaxdd generates random numbers from that distribution. maxddStats computes the expectation of drawdowns.
dmaxdd returns for a trendless Brownian process mean=0 and standard deviation "sd" the density from the probability that the maximum drawdown " D " is larger or equal to " h " in the interval $[0, \mathrm{~T}]$, where " T " denotes the time horizon of the investor.
pmaxdd returns for a trendless Brownian process mean=0 and standard deviation "sd" the probability that the maximum drawdown " D " is larger or equal to " h " in the interval $[0, \mathrm{~T}]$, where " T " denotes the time horizon of the investor.
rmaxdd returns for a Brownian Motion process with mean mean and standard deviation sd random variates of maximum drawdowns.
maxddStats returns the expected value, $\mathrm{E}[\mathrm{D}]$, of maximum drawdowns of Brownian Motion for a given drift mean, variance sd, and runtime horizon of the Brownian Motion process.

## Note

Currrently, only the driftless case is implemented.

## References

Magdon-Ismail M., Atiya A.F., Pratap A., Abu-Mostafa Y.S. (2003); On the Maximum Drawdown of a Brownian Motion, Preprint, CalTech, Pasadena USA, p. 24.

## Examples

```
## rmaxdd -
    # Set a random seed
    set.seed(1953)
    # horizon of the investor, time T
    horizon = 1000
    # number of MC samples, N -> infinity
    samples = 1000
    # Range of expected Drawdons
    xlim = c(0, 5)*sqrt(horizon)
    # Plot Histogram of Simulated Max Drawdowns:
    r = rmaxdd(n = samples, mean = 0, sd = 1, horizon = horizon)
    hist(x = r, n = 40, probability = TRUE, xlim = xlim,
        col = "steelblue4", border = "white", main = "Max. Drawdown Density")
    points(r, rep(0, samples), pch = 20, col = "orange", cex = 0.7)
## dmaxdd -
    x = seq(0, xlim[2], length = 200)
    d = dmaxdd(x = x, sd = 1, horizon = horizon, N = 1000)
    lines(x, d, lwd = 2)
## pmaxdd -
    # Count Frequencies of Drawdowns Greater or Equal to "h":
    n = 50
    x = seq(0, xlim[2], length = n)
    g = rep(0, times = n)
    for (i in 1:n) g[i] = length (r[r> x[i]]) / samples
    plot(x, g, type ="h", lwd = 3,
        xlab = "q", main = "Max. Drawdown Probability")
    # Compare with True Probability "G_D(h)":
    x = seq(0, xlim[2], length = 5*n)
    p = pmaxdd(q = x, sd = 1, horizon = horizon, N = 5000)
    lines(x, p, lwd = 2, col="steelblue4")
## maxddStats -
    # Compute expectation Value E[D]:
    maxddStats(mean = -0.5, sd = 1, horizon = 10^(1:4))
    maxddStats(mean = 0.0, sd = 1, horizon = 10^(1:4))
    maxddStats(mean = 0.5, sd = 1, horizon = 10^(1:4))
```


## Description

Density, distribution function, quantile function and random generation for the normal inverse Gaussian distribution.

## Usage

$\operatorname{dnig}(x$, alpha $=1$, beta $=0$, delta $=1, m u=0, \log =$ FALSE $)$
pnig(q, alpha $=1$, beta $=0$, delta $=1$, mu = 0)
qnig ( $p$, alpha $=1$, beta $=0$, delta $=1$, mu = 0)
$\operatorname{rnig}(\mathrm{n}, \mathrm{alpha}=1$, beta $=0$, delta $=1$, mu = 0)

## Arguments

$x, q \quad a \quad$ numeric vector of quantiles.
$p \quad a \operatorname{numeric}$ vector of probabilities.
$n \quad$ number of observations.
alpha shape parameter.
beta skewness parameter beta, abs(beta) is in the range (0, alpha).
delta scale parameter, must be zero or positive.
mu location parameter, by default 0 .
log a logical flag by default FALSE. Should labels and a main title be drawn to the plot?

## Details

dnig gives the density. pnig gives the distribution function. qnig gives the quantile function, and rnig generates random deviates.
The parameters alpha, beta, delta, mu are in the first parameterization of the distribution.
The random deviates are calculated with the method described by Raible (2000).

## Value

numeric vector

## Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.
Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.

Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
## nig -
    set.seed(1953)
    r= rnig(5000, alpha = 1, beta = 0.3, delta = 1)
    plot(r, type = "l", col = "steelblue",
        main = "nig: alpha=1 beta=0.3 delta=1")
## nig -
    # Plot empirical density and compare with true density:
    hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
    x = seq(-5, 5, 0.25)
    lines(x, dnig(x, alpha = 1, beta = 0.3, delta = 1))
## nig -
    # Plot df and compare with true df:
    plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
    lines(x, pnig(x, alpha = 1, beta = 0.3, delta = 1))
## nig -
    # Compute Quantiles:
    qnig(pnig(seq(-5, 5, 1), alpha = 1, beta = 0.3, delta = 1),
        alpha = 1, beta = 0.3, delta = 1)
```

nigFit

Fit of a Normal Inverse Gaussian Distribution

## Description

Estimates the parameters of a normal inverse Gaussian distribution.

## Usage

```
nigFit(x, alpha \(=1\), beta \(=0\), delta \(=1\), mu = 0,
    method = c("mle", "gmm", "mps", "vmps"), scale = TRUE, doplot = TRUE,
    span = "auto", trace = TRUE, title = NULL, description = NULL, ...)
```


## Arguments

alpha, beta, delta, mu
The parameters are alpha, beta, delta, and mu:
shape parameter alpha; skewness parameter beta, abs(beta) is in the range ( 0 , alpha); scale parameter delta, delta must be zero or positive; location parameter mu, by default 0 . These is the meaning of the parameters in the first
parameterization $\mathrm{pm}=1$ which is the default parameterization selection. In the second parameterization, $\mathrm{pm}=2$ alpha and beta take the meaning of the shape parameters (usually named) zeta and rho. In the third parameterization, pm=3 alpha and beta take the meaning of the shape parameters (usually named) xi and chi. In the fourth parameterization, $\mathrm{pm}=4$ alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.
description a character string which allows for a brief description.
doplot a logical flag. Should a plot be displayed?
method a character string. Either "mle", Maximum Likelihood Estimation, the default, "gmm" Gemeralized Method of Moments Estimation, "mps" Maximum Product Spacings Estimation, or "vmps" Minimum Variance Product Spacings Estimation.
scale a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
span $\quad x$-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001 , and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times $=n$ ), where, min and max are the left and right endpoints of the range, and $n$ gives the number of the intermediate points.
title a character string which allows for a project title.
trace a logical flag. Should the parameter estimation process be traced?
$x \quad a \quad$ numeric vector.
... parameters to be parsed.

## Value

an object from class "fDISTFIT".
Slot fit is a list with the following components:
estimate the point at which the maximum value of the log liklihood function is obtained.
minimum the value of the estimated maximum, i.e. the value of the log liklihood function.
code an integer indicating why the optimization process terminated.
1: relative gradient is close to zero, current iterate is probably solution;
2: successive iterates within tolerance, current iterate is probably solution;
3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small;
4: iteration limit exceeded;
5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient the gradient at the estimated maximum.
steps number of function calls.

## Examples

```
## nigFit -
    # Simulate Random Variates:
    set.seed(1953)
    s = rnig(n = 1000, alpha = 1.5, beta = 0.3, delta = 0.5, mu = -1.0)
## nigFit -
    # Fit Parameters:
    nigFit(s, alpha = 1, beta = 0, delta = 1, mu = mean(s), doplot = TRUE)
```

nigMode Normal Inverse Gaussian Mode

## Description

Computes the mode of the norm inverse Gaussian distribution.

## Usage

nigMode(alpha $=1$, beta $=0$, delta $=1, m u=0)$

## Arguments

| alpha | shape parameter. |
| :--- | :--- |
| beta | skewness parameter beta, abs(beta) is in the range ( 0, alpha). |
| delta | scale parameter, must be zero or positive. |
| mu | location parameter, by default 0. |

## Value

a numeric value, the mode of the normal inverse Gaussian distribution

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.
Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.
Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
    ## nigMode -
    nigMode()
```

nigMoments

Moments for the Normal Inverse Gaussian

## Description

Computes the first four moments for the normal inverse Gaussian distribution.

## Usage

```
nigMean(alpha \(=1\), beta \(=0\), delta \(=1, m u=0)\)
nigVar(alpha \(=1\), beta \(=0\), delta \(=1\), mu = 0)
nigSkew(alpha \(=1\), beta \(=0\), delta \(=1\), mu = 0)
nigKurt(alpha \(=1\), beta \(=0\), delta \(=1\), mu = 0)
```


## Arguments

| alpha | shape parameter. |
| :--- | :--- |
| beta | skewness parameter beta, abs(beta) is in the range (0, alpha). |
| delta | scale parameter, must be zero or positive. |
| mu | location parameter, by default 0. |

## Value

a named numerical value. The name is one of mean, var, skew, or kurt, obtained by dropping the nig prefix from the name of the corresponding function and lowercasing it.

## Author(s)

Diethelm Wuertz.

## References

Scott, D. J., Wuertz, D. and Tran, T. T. (2008) Moments of the Generalized Hyperbolic Distribution. Preprint.

## Examples

```
## nigMean -
    # Median:
    nigMean(alpha = 1, beta = 0, delta = 1, mu = 0)
## nigVar -
    # Inter-quartile Range:
    nigVar(alpha = 1, beta = 0, delta = 1, mu = 0)
## nigSKEW -
    # Robust Skewness:
    nigSkew(alpha = 1, beta = 0, delta = 1, mu = 0)
## nigKurt -
    # Robust Kurtosis:
    nigKurt(alpha = 1, beta = 0, delta = 1, mu = 0)
```

nigRobMoments
Robust Moments for the NIG

## Description

Computes the first four robust moments for the Normal Inverse Gaussian Distribution.

## Usage

nigMED(alpha $=1$, beta $=0$, delta $=1$, mu $=0$ )
nigIQR(alpha $=1$, beta $=0$, delta $=1$, mu = 0)
nigSKEW(alpha $=1$, beta $=0$, delta $=1$, mu = 0)
nigKURT(alpha $=1$, beta $=0$, delta $=1$, mu $=0$ )

## Arguments

alpha shape parameter.
beta skewness parameter beta, abs(beta) is in the range (0, alpha).
delta scale parameter, must be zero or positive.
mu location parameter, by default 0 .

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the nig prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz.

## Examples

```
## nigMED -
    # Median:
    nigMED(alpha = 1, beta = 0, delta = 1, mu = 0)
## nigIQR -
    # Inter-quartile Range:
    nigIQR(alpha = 1, beta = 0, delta = 1, mu = 0)
## nigSKEW -
    # Robust Skewness:
    nigSKEW(alpha = 1, beta = 0, delta = 1, mu = 0)
## nigKURT -
    # Robust Kurtosis:
    nigKURT(alpha = 1, beta = 0, delta = 1, mu = 0)
```

nigShapeTriangle NIG Shape Triangle

## Description

Plots the normal inverse Gaussian Shape Triangle.

## Usage

nigShapeTriangle(object, add = FALSE, labels = TRUE, ...)

## Arguments

object an object of class "fDISTFIT" as returned by the function nigFit.
add a logical value. Should another point added to the NIG shape triangle? By default FALSE, a new plot will be created.
labels a logical flag by default TRUE. Should the logarithm of the density be returned?
... arguments to be passed to the function integrate.

## Value

displays the parameters of fitted distributions in the NIG shape triangle.

## Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

## References

Atkinson, A.C. (1982); The simulation of generalized inverse Gaussian and hyperbolic random variables, SIAM J. Sci. Stat. Comput. 3, 502-515.
Barndorff-Nielsen O. (1977); Exponentially decreasing distributions for the logarithm of particle size, Proc. Roy. Soc. Lond., A353, 401-419.

Barndorff-Nielsen O., Blaesild, P. (1983); Hyperbolic distributions. In Encyclopedia of Statistical Sciences, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700-707. New York: Wiley.

Raible S. (2000); Levy Processes in Finance: Theory, Numerics and Empirical Facts, PhD Thesis, University of Freiburg, Germany, 161 pages.

## Examples

```
## nigShapeTriangle -
    #
```

nigSlider nigerbolic Distribution Slider

## Description

Displays interactively the dependence of the nigerbolic distribution on its parameters.

## Usage

nigSlider()

## Value

a tcl/tk based graphical user interface.
This is a nice display for educational purposes to investigate the densities and probabilities of the invetrse Gaussian distribution.

## Examples

```
## nigSlider -
    # nigSlider()
```

norm Matrix norm

## Description

Computes the norm of a matrix.

## Usage

norm2(x, $\mathrm{p}=2)$

## Arguments

$x \quad$ a numeric matrix.
$\mathrm{p} \quad$ an integer value, 1,2 or Inf, see section 'Details'.

## Details

The function norm2 computes the norm of a matrix. Three choices are possible:
$\mathrm{p}=1$ The maximum absolute column sum norm which is defined as the maximum of the sum of the absolute valued elements of columns of the matrix.
$p=2$ The spectral norm is "the norm" of a matrix $X$. This value is computed as the square root of the maximum eigenvalue of $C X$, where $C$ is the conjugate transpose.
$\mathrm{p}=$ Inf The maximum absolute row sum norm is defined as the maximum of the sum of the absolute valued elements of rows of the matrix.

Value
the requested norm of the matrix, a non-negative number

Note
Since base : : norm() has become available in the R base environment, the function fBasics: : norm() has become obsolete. To avoid conflicts with norm() we have renamed the fBasics' one to norm2.

## References

Golub, van Loan, (1996); Matrix Computations, 3rd edition. Johns Hopkins University Press.

## Examples

```
## Create Pascal Matrix:
    P <- pascal(5)
    P
## Return the Norm of the Matrix:
    norm2(P)
```

```
NormalityTests Tests for normality
```


## Description

A collection of functions of one sample tests for testing normality of financial return series.

The functions for testing normality are:

| ksnormTest | Kolmogorov-Smirnov normality test, |
| :--- | :--- |
| shapiroTest | Shapiro-Wilk’s test for normality, |
| jarqueberaTest | Jarque-Bera test for normality, |
| dagoTest | D'Agostino normality test. |

Functions for high precision Jarque Bera LM and ALM tests:
jbTest Performs finite sample adjusted JB, LM and ALM test.

Additional functions for testing normality from the 'nortest' package:

$$
\begin{array}{ll}
\text { adTest } & \text { Anderson-Darling normality test, } \\
\text { cvmTest } & \text { Cramer-von Mises normality test, } \\
\text { lillieTest } & \text { Lilliefors (Kolmogorov-Smirnov) normality test, } \\
\text { pchiTest } & \text { Pearson chi-square normality test, } \\
\text { sfTest } & \text { Shapiro-Francia normality test. }
\end{array}
$$

For SPlus/Finmetrics Compatibility:
normalTest test suite for some normality tests.

## Usage

```
ksnormTest(x, title = NULL, description = NULL)
jbTest(x, title = NULL, description = NULL)
shapiroTest(x, title = NULL, description = NULL)
    normalTest(x, method = c("sw", "jb"), na.rm = FALSE)
    jarqueberaTest(x, title = NULL, description = NULL)
    dagoTest(x, title = NULL, description = NULL)
    adTest(x, title = NULL, description = NULL)
    cvmTest(x, title = NULL, description = NULL)
    lillieTest(x, title = NULL, description = NULL)
    pchiTest(x, title = NULL, description = NULL)
```

```
sfTest(x, title \(=\) NULL, description = NULL)
```


## Arguments

$\times$ title an optional character string, if not specified the inputs data name is deparsed.
description
method for normalTest only, indicates one of four different methods for the normality test, one of "ks" (Kolmogorov-Smirnov one-sample test, the the default), "sw" (Shapiro-Wilk test), "jb" (Jarque-Bera Test), and "da" (D'Agostino Test).
na.rm for normalTest only, a logical value. Should missing values removed before computing the tests? The default value is FALSE.

## Details

The hypothesis tests may be of interest for many financial and economic applications, especially for the investigation of univariate time series returns.
Several tests for testing if the records from a data set are normally distributed are available. The input to all these functions may be just a vector $x$ or a univariate time series object $x$ of class timeSeries.
First, there exists a wrapper function which allows to call one from two normal tests either the Shapiro-Wilks test or the Jarque-Bera test. This wrapper was introduced for compatibility with S-Plus' FinMetrics package.
Also available are the Kolmogorov-Smirnov one sample test and the D'Agostino normality test.
The remaining five normal tests are the Anderson-Darling test, the Cramer-von Mises test, the Lilliefors (Kolmogorov-Smirnov) test, the Pearson chi-square test, and the Shapiro-Francia test. They are calling functions from R's contributed package nortest. The difference to the original test functions implemented in R and from contributed R packages is that the Rmetrics functions accept time series objects as input and give a more detailed output report.
The Anderson-Darling test is used to test if a sample of data came from a population with a specific distribution, here the normal distribution. The adTest goodness-of-fit test can be considered as a modification of the Kolmogorov-Smirnov test which gives more weight to the tails than does the ksnormTest.
Note that jarqueBeraTest computes the asymptotic statistic and p-value, while jbTesT gives final sample approximations.

## Value

an object from class fHTEST
Slot test is a list containing the following (optionally empty) elements (in addition to those described in fHTEST):
ksnormTest the 'D' statistic and p-values for the three alternatives 'two-sided, 'less' and 'greater'.
shapiroTest the 'W' statistic and the p-value.
jarqueberaTest no additional elements.
jbTest the 'Chi-squared' statistic with 2 degrees of freedom and the asymptotic p-value. jbTest is the finite sample version of the Jarque Bera Lagrange multiplier, LM, and adjusted Lagrange multiplier test, ALM.
dagoTest the 'Chi-squared', the 'Z3' (Skewness) and 'Z4' (Kurtosis) statistic together with the corresponding p values.
adTest the ' A ' statistic and the p -value.
cvmTest the 'W' statistic and the p-value.
lillieTest the 'D' statistic and the p -value.
pchiTest the value for the ' P ' statistic and the p -values for the adjusted and not adjusted test cases. In addition the number of classes is printed, taking the default value due to Moore (1986) computed from the expression $n$.classes $=\operatorname{ceiling}\left(2 *\left(n^{\wedge}(2 / 5)\right)\right)$, where $n$ is the number of observations.
sfTest the 'W' statistic and the p-value.

## Note

Some of the test implementations are selected from R's ctest and nortest packages.

## Author(s)

R-core team for the tests from R's ctest package,
Adrian Trapletti for the runs test from R's tseries package,
Juergen Gross for the normal tests from R's nortest package,
James Filliben for the Fortran program producing the runs report,
Diethelm Wuertz and Helmut Katzgraber for the finite sample JB tests,
Diethelm Wuertz for the Rmetrics R-port.
Earlier versions of theses functions were based on Fortran code of Paul Johnson.

## References

Anderson T.W., Darling D.A. (1954); A Test of Goodness of Fit, JASA 49:765-69.
Conover, W. J. (1971); Practical nonparametric statistics, New York: John Wiley \& Sons.
D’Agostino R.B., Pearson E.S. (1973); Tests for Departure from Normality, Biometrika 60, 613-22.
D'Agostino R.B., Rosman B. (1974); The Power of Geary's Test of Normality, Biometrika 61, 181-84.
Durbin J. (1961); Some Methods of Constructing Exact Tests, Biometrika 48, 41-55.
Durbin,J. (1973); Distribution Theory Based on the Sample Distribution Function, SIAM, Philadelphia.
Geary R.C. (1947); Testing for Normality; Biometrika 36, 68-97.
Lehmann E.L. (1986); Testing Statistical Hypotheses, John Wiley and Sons, New York.
Linnet K. (1988); Testing Normality of Transformed Data, Applied Statistics 32, 180-186.
Moore, D.S. (1986); Tests of the chi-squared type, In: D'Agostino, R.B. and Stephens, M.A., eds., Goodness-of-Fit Techniques, Marcel Dekker, New York.

Shapiro S.S., Francia R.S. (1972); An Approximate Analysis of Variance Test for Normality, JASA 67, 215-216.
Shapiro S.S., Wilk M.B., Chen V. (1968); A Comparative Study of Various Tests for Normality, JASA 63, 1343-72.

Thode H.C. (2002); Testing for Normality, Marcel Dekker, New York.
Weiss M.S. (1978); Modification of the Kolmogorov-Smirnov Statistic for Use with Correlated Data, JASA 73, 872-75.
Wuertz D., Katzgraber H.G. (2005); Precise finite-sample quantiles of the Jarque-Bera adjusted Lagrange multiplier test, ETHZ Preprint.

## Examples

```
## Series:
    x = rnorm(100)
## ksnormTests -
    # Kolmogorov - Smirnov One-Sampel Test
    ksnormTest(x)
## shapiroTest - Shapiro-Wilk Test
    shapiroTest(x)
## jarqueberaTest -
    # Jarque - Bera Test
    # jarqueberaTest(x)
    # jbTest(x)
```

    normRobMoments Robust moments for the Normal distribution
    
## Description

Computes the first four robust moments for the Normal distribution.

## Usage

normMED(mean $=0$, sd = 1)
normIQR(mean $=0, \quad s d=1$ )
normSKEW (mean $=0$, sd $=1$ )
normKURT (mean $=0$, sd $=1$ )

## Arguments

| mean | locaiton parameter. |
| :--- | :--- |
| sd | scale parameter. |

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the gh prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz

## Examples

```
## normMED -
    # Median:
    normMED(mean = 0, sd = 1)
## normIQR -
    # Inter-quartile Range:
    normIQR(mean = 0, sd = 1)
## normSKEW -
    # Robust Skewness:
    normSKEW(mean = 0, sd = 1)
## normKURT -
    # Robust Kurtosis:
    normKURT(mean = 0, sd = 1)
```


## pascal Pascal matrix

## Description

Creates a Pascal matrix.

## Usage

pascal(n)

## Arguments

$n \quad$ an integer value, the dimension of the square matrix.

## Details

The function pascal generates a Pascal matrix of order $n$ which is a symmetric positive definite matrix with integer entries made up from Pascal's triangle. The determinant of a Pascal matrix is 1. The inverse of a Pascal matrix has integer entries. If lambda is an eigenvalue of a Pascal matrix, then $1 /$ lambda is also an eigenvalue of the matrix. Pascal matrices are ill-conditioned.

## References

Call G.S., Velleman D.J., (1993); Pascal's matrices, American Mathematical Monthly 100, 372376.

Edelman A., Strang G., (2004); Pascal Matrices, American Mathematical Monthly 111, 361-385.

## Examples

```
## Create Pascal Matrix:
        P = pascal(5)
        P
    ## Determinant
        det(pascal(5))
        det(pascal(10))
        det(pascal(15))
        det(pascal(20))
```

    pdl Polynomial distributed lags
    
## Description

Creates a regressor matrix for polynomial distributed lags.

## Usage

$\operatorname{pdl}(x, d=2, q=3, \operatorname{trim}=F A L S E)$

## Arguments

x
d an integer specifying the order of the polynomial.
q
trim a logical flag; if TRUE, the missing values at the beginning of the returned matrix will be trimmed.

## See Also

tslag

## Examples

\#\# pdl -
\#

```
    positiveDefinite Positive definite matrices
```


## Description

Checks if a matrix is positive definite and/or forces a matrix to be positive definite.

## Usage

isPositiveDefinite(x)
makePositiveDefinite(x)

## Arguments

$x \quad$ a square numeric matrix.

## Details

The function isPositiveDefinite checks if a square matrix is positive definite.
The function makePositiveDefinite forces a matrix to be positive definite.

## Author(s)

Korbinian Strimmer.

## Examples

\#\# isPositiveDefinite \# the $3 \times 3$ Pascal Matrix is positive define isPositiveDefinite(pascal(3))

```
print Print control
```


## Description

Unlists and prints a control object.

## Usage

\#\# S3 method for class 'control'
print(x, ...)

## Arguments

x the object to be printed.
... arguments to be passed.

## Value

prints control

## Examples

```
## print -
    control = list( n = 211, seed = 54, name = "generator")
    print(control)
    class(control) = "control"
    print(control)
```

```
QuantileQuantilePlots Quantile-Quantile plots
```


## Description

Returns quantile-quantile plots for the normal, the normal inverse Gaussian, the generalized hyperbolic Student-t and the generalized lambda distribution.

## Usage

```
qqnormPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
qqnigPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
qqghtPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
qqgldPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
```


## Arguments

x
labels a logical flag, should the plot be returned with default labels and decorated in an automated way? By default TRUE.
col the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat. colors(ncol(x)).

| pch | an integer value, by default 19. Which plot character should be used in the plot? |
| :--- | :--- |
| title |  |
| mtext | a logical flag, by default TRUE. Should a default title added to the plot? <br> a logical flag, by default TRUE. Should a marginal text be printed on the third site <br> of the graph? |
| grid | a logical flag, should a grid be added to the plot? By default TRUE. To plot a <br> horizontal lines only use grid=" $h "$ and for vertical lines use grid="h", respec- <br> tively. |
| rug | a logical flag, by default TRUE . Should a rug representation of the data added to <br> the plot? <br> a logical flag, by default TRUE. Should the time series be scaled for the investi- <br> gation? |
| $\ldots$ | optional arguments to be passed. |

## Details

List of Functions:

> qqnormPlot Produces a tailored Normal quantile-quantile plot, qqnigPlot Produces a tailored NIG quantile-quantile plot, qqghtPlot Produces a tailored GHT quantile-quantile plot, qqgldPlot Produces a tailored GLD quantile-quantile plot.

## Value

displays a quantile-quantile plot.

## Author(s)

Diethelm Wuertz for the Rmetrics R-port.

## Examples

```
## data -
    data(LPP2005REC, package = "timeSeries")
    SPI <- LPP2005REC[, "SPI"]
    plot(SPI, type = "l", col = "steelblue", main = "SP500")
    abline(h = 0, col = "grey")
## qqPlot -
    qqnormPlot(SPI)
```


## Description

A graphical user interface to display finanical time series plots. returnSeriesGUI opens a GUI for return series plots.

## Usage

returnSeriesGUI(x)

## Arguments

x
an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other than timeSeries objects, is more or less untested.

## Value

For returnSeriesGUI function, besides the graphical user interface no values are returned.

## Author(s)

Diethelm Wuertz for the Rmetrics R-port.
rk The rank of a matrix

## Description

Computes the rank of a matrix.

## Usage

rk(x, method = c("qr", "chol"))

## Arguments

x
a numeric matrix.
method a character string. For method = "qr" the rank is computed as $\operatorname{qr}(x) \backslash \$ r a n k$, or alternatively for method $=$ "chol" the rank is computed as attr (chol ( $x$, pivot = TRUE), "rank").

## Details

The function rk computes the rank of a matrix which is the dimension of the range of the matrix corresponding to the number of linearly independent rows or columns of the matrix, or to the number of nonzero singular values.
The rank of a matrix is also named linear map.

## References

Golub, van Loan, (1996); Matrix Computations, 3rd edition. Johns Hopkins University Press.

## Examples

```
## Create Pascal Matrix:
    P = pascal(5)
    P
## Compute the Rank:
    rk(P)
    rk(P, "chol")
```

    rowStats Row statistics
    
## Description

Functions to compute row statistical properties of financial and economic time series data.

The functions are:

| rowStats | calculates row statistics, |
| :--- | :--- |
| rowSds | calculates row standard deviations, |
| rowVars | calculates row variances, |
| rowSkewness | calculates row skewness, |
| rowKurtosis | calculates row kurtosis, |
| rowMaxs | calculates maximum values in each row, |
| rowMins | calculates minimum values in each row, |
| rowProds | computes product of all values in each row, |
| rowQuantiles | computes quantiles of each row. |

## Usage

```
rowStats(x, FUN, ...)
```

rowSds(x, ...)
rowVars(x, ...)
rowSkewness(x, ...)
rowKurtosis(x, ...)
rowMaxs(x, ...)
rowMins(x, ...)
rowProds ( $x, \ldots$.
rowQuantiles(x, prob = 0.05, ...)

```
rowStdevs(x, ...)
rowAvgs(x, ...)
```


## Arguments

FUN a function name, the statistical function to be applied.
prob a numeric value, the probability with value in $[0,1]$.
$x \quad$ a rectangular object which can be transformed into a matrix by the function as.matrix.
... arguments to be passed.

## Value

each function returns a numeric vector of the statistics

## See Also

colStats

## Examples

```
## Simulated Return Data in Matrix Form:
    x = matrix(rnorm(10*10), nrow = 10)
## rowStats -
    rowStats(x, FUN = mean)
## rowMaxs -
    rowMaxs(x)
```

sampleLMoments Sample L-moments

## Description

Computes L-moments from an empirical sample data set.

## Usage

sampleLmoments(x, rmax = 4)

## Arguments

x
rmax
numeric vector, the sample values.
an integer value, the number of L-moments to be returned.

## Value

a named numeric vector of length rmax with names c("L1", "L2", ..., "L<rmax>")

## Author(s)

Diethelm Wuertz

## Examples

```
## Sample:
    x = rt(100, 4)
## sampleLmoments -
    sampleLmoments(x)
```

sampleRobMoments

Robust moments for the GLD

## Description

Computes the first four robust moments for the Normal Inverse Gaussian Distribution.

## Usage

sampleMED ( $x$ )
sampleIQR(x)
sampleSKEW( $x$ )
sampleKURT( $x$ )

## Arguments

X
numeric vector, the sample values.

## Value

a named numerical value. The name is one of MED, IQR, SKEW, or KURT, obtained by dropping the sample prefix from the name of the corresponding function.

## Author(s)

Diethelm Wuertz

## Examples

```
## Sample:
    x = rt(100, 4)
## sampleMED -
    # Median:
    sampleMED(x)
## sampleIQR -
    # Inter-quartile Range:
    sampleIQR(x)
## sampleSKEW -
    # Robust Skewness:
    sampleSKEW(x)
## sampleKURT -
    # Robust Kurtosis:
    sampleKURT(x)
```

scaleTest Two sample scale tests

## Description

Tests if two series differ in their distributional scale parameter.

## Usage

scaleTest(x, y, method = c("ansari", "mood"), title $=$ NULL, description $=$ NULL)

## Arguments

$x, y \quad$ numeric vectors of data values.
method a character string naming which test should be applied.
title an optional title string, if not specified the inputs data name is deparsed.
description optional description string, or a vector of character strings.

## Details

The method="ansari" performs the Ansari-Bradley two-sample test for a difference in scale parameters. The test returns for any sizes of the series $x$ and $y$ the exact $p$ value together with its asymptotic limit.
The method="mood", is another test which performs a two-sample test for a difference in scale parameters. The underlying model is that the two samples are drawn from $f(x-l)$ and $f((x-l) / s) / s$, respectively, where $l$ is a common location parameter and $s$ is a scale parameter. The null hypothesis is $s=1$.

## Value

an object from class fHTEST

## Note

Some of the test implementations are selected from R's ctest package.

## Author(s)

R-core team for hypothesis tests implemented from R's package ctest.

## References

Conover, W. J. (1971); Practical nonparametric statistics, New York: John Wiley \& Sons.
Lehmann E.L. (1986); Testing Statistical Hypotheses, John Wiley and Sons, New York.
Moore, D.S. (1986); Tests of the chi-squared type, In: D'Agostino, R.B. and Stephens, M.A., eds., Goodness-of-Fit Techniques, Marcel Dekker, New York.

## Examples

```
## rnorm -
    # Generate Series:
    x = rnorm(50)
    y = rnorm(50)
## scaleTest -
    scaleTest(x, y, "ansari")
    scaleTest(x, y, "mood")
```


## Description

Evaluates the scaling exponent of a financial return series and plots the scaling law.

## Usage

scalinglawPlot(x, span = ceiling(log(length(x)/252)/log(2)), doplot = TRUE, labels $=$ TRUE, trace $=$ TRUE,...$)$

## Arguments

X
an uni- or multivariate return series of class "timeSeries" or any other object which can be transformed by the function as.timeSeries() into an object of class "timeSeries".
span an integer value, determines for the qqgaussPlot the plot range, by default 5, and for the scalingPlot a reasonable number of points for the scaling range, by default daily data with 252 business days per year are assumed.
doplot a logical value. Should a plot be displayed?
labels a logical value. Whether or not $x$ - and $y$-axes should be automatically labeled and a default main title should be added to the plot. By default TRUE.
trace a logical value. Should the computation be traced?
arguments to be passed.

## Details

## Scaling Behavior:

The function scalingPlot plots the scaling law of financial time series under aggregation and returns an estimate for the scaling exponent. The scaling behavior is a very striking effect of the foreign exchange market and also other markets expressing a regular structure for the volatility. Considering the average absolute return over individual data periods one finds a scaling power law which relates the mean volatility over given time intervals to the size of these intervals. The power law is in many cases valid over several orders of magnitude in time. Its exponent usually deviates significantly from a Gaussian random walk model which implies 1/2.

## Value

a list with the following components:
Intercept intercept,
Exponent the scaling exponent,
InverseExponent
the inverse of the scaling component.

## Author(s)

Diethelm Wuertz for the Rmetrics R-port.

## References

Taylor S.J. (1986); Modeling Financial Time Series, John Wiley and Sons, Chichester.

## Examples

```
## data -
    data(LPP2005REC, package = "timeSeries")
    SPI <- LPP2005REC[, "SPI"]
```

```
    plot(SPI, type = "l", col = "steelblue", main = "SP500")
    abline(h = 0, col = "grey")
    ## teffectPlot -
    # Scaling Law Effect:
    scalinglawPlot(SPI)
```

sgh
Standardized Generalized Hyperbolic Distribution

## Description

Density, distribution function, quantile function and random generation for the standardized generalized hyperbolic distribution.

## Usage

dsgh(x, zeta $=1$, rho $=0$, lambda $=1$, log $=$ FALSE $)$
psgh(q, zeta $=1$, rho $=0$, lambda = 1)
qsgh(p, zeta $=1$, rho $=0$, lambda = 1)
$\operatorname{rsgh}(\mathrm{n}$, zeta $=1$, rho $=0$, lambda = 1)

## Arguments

| $\mathrm{x}, \mathrm{q}$ | a numeric vector of quantiles. |
| :--- | :--- |
| p | a numeric vector of probabilities. |
| n | number of observations. |
| zeta | shape parameter, a positive number. |
| rho | skewness parameter, a number in the range $(-1,1)$. |
| lambda | $? ?$ |
| log | a logical flag by default FALSE. If TRUE, log values are returned. |

## Details

dsgh gives the density, psgh gives the distribution function, qsgh gives the quantile function, and rsgh generates random deviates.

The generator rsgh is based on the GH algorithm given by Scott (2004).

## Value

numeric vector

## Author(s)

Diethelm Wuertz

## Examples

```
    ## rsgh -
    set.seed(1953)
    r = rsgh(5000, zeta = 1, rho = 0.5, lambda = 1)
    plot(r, type = "l", col = "steelblue",
        main = "gh: zeta=1 rho=0.5 lambda=1")
## dsgh -
    # Plot empirical density and compare with true density:
    hist(r, n = 50, probability = TRUE, border = "white", col = "steelblue",
        ylim = c(0, 0.6))
    x = seq(-5, 5, length = 501)
    lines(x, dsgh(x, zeta = 1, rho = 0.5, lambda = 1))
## psgh -
    # Plot df and compare with true df:
    plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
    lines(x, psgh(x, zeta = 1, rho = 0.5, lambda = 1))
## qsgh -
    # Compute Quantiles:
    round(qsgh(psgh(seq(-5, 5, 1), zeta = 1, rho = 0.5), zeta = 1, rho = 0.5), 4)
```

sghFit Standardized GH distribution fit

## Description

Estimates the distributional parameters for a standardized generalized hyperbolic distribution.

## Usage

$\operatorname{sghFit}(x$, zeta $=1$, rho $=0$, lambda $=1$, include.lambda $=$ TRUE, scale $=$ TRUE, doplot $=$ TRUE, span = "auto", trace $=$ TRUE, title $=$ NULL, description $=$ NULL, ...)

## Arguments

$x \quad$ a numeric vector.
zeta, rho, lambda
shape parameter zeta is positive, skewness parameter rho is in the range $(-1$, 1). and index parameter lambda, by default 1 .
include. lambda a logical flag, by default TRUE. Should the index parameter lambda included in the parameter estimate?
scale a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
doplot a logical flag. Should a plot be displayed?

| span | x-coordinates for the plot, by default 100 values automatically selected and rang- <br> ing between the 0.001, and 0.999 quantiles. Alternatively, you can specify the <br> range by an expression like span=seq(min, max, times $=n$ ), where, min and <br> max are the left and right endpoints of the range, and $n$ gives the number of the <br> intermediate points. |
| :--- | :--- |
| trace | a logical flag. Should the parameter estimation process be traced? |
| title | a character string which allows for a project title. |
| description | a character string which allows for a brief description. |
| $\ldots$ | parameters to be parsed. |

## Value

an object from class "fDISTFIT".
Slot fit is a list with the following components:

| estimate | the point at which the maximum value of the log liklihood function is obtained. |
| :--- | :--- |
| minimum | the value of the estimated maximum, i.e. the value of the log likelihood function. |
| code | an integer indicating why the optimization process terminated. |
| 1: relative gradient is close to zero, current iterate is probably solution; |  |
| 2: successive iterates within tolerance, current iterate is probably solution; |  |
| 3: last global step failed to locate a point lower than estimate. Either estimate |  |
| is an approximate local minimum of the function or steptol is too small; |  |
| 4: iteration limit exceeded; |  |
| 5: maximum step size stepmax exceeded five consecutive times. Either the |  |
| function is unbounded below, becomes asymptotic to a finite value from above |  |
| in some direction or stepmax is too small. |  |
| gradient | the gradient at the estimated maximum. |
| steps | number of function calls. |

## Examples

```
## sghFit -
    # Simulate Random Variates:
    set.seed(1953)
    s = rsgh(n = 2000, zeta = 0.7, rho = 0.5, lambda = 0)
## sghFit -
    # Fit Parameters:
    sghFit(s, zeta = 1, rho = 0, lambda = 1, include.lambda = TRUE,
        doplot = TRUE)
```


## Description

Density, distribution function, quantile function and random generation for the standardized generalized hyperbolic Student-t distribution.

## Usage

dsght (x, beta $=0.1$, delta $=1, m u=0, n u=10, \log =$ FALSE)
psght(q, beta $=0.1$, delta $=1$, mu = 0, nu = 10)
qsght ( $p$, beta $=0.1$, delta $=1$, mu $=0$, nu $=10$ )
$\operatorname{rsght}(\mathrm{n}$, beta $=0.1$, delta $=1, \mathrm{mu}=0, \mathrm{nu}=10)$

## Arguments

$x, q \quad a \quad$ numeric vector of quantiles.
$p \quad a \quad$ numeric vector of probabilities.
$n \quad$ number of observations.
beta numeric value, beta is the skewness parameter in the range ( 0 , alpha).
delta numeric value, the scale parameter, must be zero or positive.
mu numeric value, the location parameter, by default 0 .
nu a numeric value, the number of degrees of freedom. Note, alpha takes the limit of abs(beta), and lambda=-nu/2.
$\log \quad a \operatorname{logical}$, if TRUE, probabilities $p$ are given as $\log (p)$.

## Details

dsght gives the density, psght gives the distribution function, qsght gives the quantile function, and rsght generates random deviates.
These are the parameters in the first parameterization.

## Value

numeric vector

## Author(s)

Diethelm Wuertz

## Examples

```
## rsght -
    set.seed(1953)
    r = rsght(5000, beta = 0.1, delta = 1, mu = 0, nu = 10)
    plot(r, type = "l", col = "steelblue",
        main = "gh: zeta=1 rho=0.5 lambda=1")
## dsght -
    # Plot empirical density and compare with true density:
    hist(r, n = 50, probability = TRUE, border = "white", col = "steelblue")
    x = seq(-5, 5, length = 501)
    lines(x, dsght(x, beta = 0.1, delta = 1, mu = 0, nu = 10))
## psght -
    # Plot df and compare with true df:
    plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
    lines(x, psght(x, beta = 0.1, delta = 1, mu = 0, nu = 10))
## qsght -
    # Compute Quantiles:
    round(qsght(psght(seq(-5, 5, 1), beta = 0.1, delta = 1, mu = 0, nu =10),
                beta = 0.1, delta = 1, mu = 0, nu = 10), 4)
```

snig

Standardized Normal Inverse Gaussian Distribution

## Description

Density, distribution function, quantile function and random generation for the standardized normal inverse Gaussian distribution.

## Usage

dsnig(x, zeta $=1$, rho $=0, \log =$ FALSE $)$
psnig (q, zeta $=1$, rho $=0$ )
qsnig(p, zeta $=1$, rho $=0$ )
$\operatorname{rsnig}(n$, zeta $=1$, rho $=0)$

## Arguments

$x, q$
a numeric vector of quantiles.
p
a numeric vector of probabilities.
n number of observations.
zeta shape parameter zeta is positive.
rho skewness parameter, a number in the range $(-1,1)$.
$\log \quad a \operatorname{logical}$ flag by default FALSE. If TRUE, log values are returned.

## Details

dsnig gives the density, psnig gives the distribution function, qsnig gives the quantile function, and rsnig generates random deviates.
The random deviates are calculated with the method described by Raible (2000).

## Value

numeric vector

## Author(s)

Diethelm Wuertz

## Examples

```
## snig -
    set.seed(1953)
    r = rsnig(5000, zeta = 1, rho = 0.5)
    plot(r, type = "l", col = "steelblue",
        main = "snig: zeta=1 rho=0.5")
## snig -
    # Plot empirical density and compare with true density:
    hist(r, n = 50, probability = TRUE, border = "white", col = "steelblue")
    x = seq(-5, 5, length = 501)
    lines(x, dsnig(x, zeta = 1, rho = 0.5))
## snig -
    # Plot df and compare with true df:
    plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
    lines(x, psnig(x, zeta = 1, rho = 0.5))
## snig -
    # Compute Quantiles:
    qsnig(psnig(seq(-5, 5, 1), zeta = 1, rho = 0.5), zeta = 1, rho = 0.5)
```

snigFit

Fit of a Standardized NIG Distribution

## Description

Estimates the parameters of a standardized normal inverse Gaussian distribution.

## Usage

```
snigFit(x, zeta = 1, rho = 0, scale = TRUE, doplot = TRUE,
    span = "auto", trace = TRUE, title = NULL, description = NULL, ...)
```


## Arguments

| zeta, rho <br> description <br> doplot | shape parameter zeta is positive, skewness parameter rho is in the range $(-1,1)$. <br> a character string which allows for a brief description. |
| :--- | :--- |
| scale | a logical flag. Should a plot be displayed? <br> a logical flag, by default TRUE. Should the time series be scaled by its standard <br> deviation to achieve a more stable optimization? |
| span | x-coordinates for the plot, by default 100 values automatically selected and rang- <br> ing between the 0.001, and 0.999 quantiles. Alternatively, you can specify the <br> range by an expression like span=seq (min, max, times $=n)$, where, min and <br> max are the left and right endpoints of the range, and $n$ gives the number of the <br> intermediate points. |
| title | a character string which allows for a project title. |
| trace | a logical flag. Should the parameter estimation process be traced? |
| x | a numeric vector. |
| parameters to be parsed. |  |

## Value

an object from class "fDISTFIT".
Slot fit is a list with the following components:

| estimate | the point at which the maximum value of the log liklihood function is obtained. |
| :--- | :--- |
| minimum | the value of the estimated maximum, i.e. the value of the log liklihood function. |
| code | an integer indicating why the optimization process terminated. |
| 1: relative gradient is close to zero, current iterate is probably solution; |  |
| 2: successive iterates within tolerance, current iterate is probably solution; |  |
| 3: last global step failed to locate a point lower than estimate. Either estimate |  |
| is an approximate local minimum of the function or steptol is too small; |  |
| 4: iteration limit exceeded; |  |
| 5: maximum step size stepmax exceeded five consecutive times. Either the |  |
| function is unbounded below, becomes asymptotic to a finite value from above |  |
| in some direction or stepmax is too small. |  |
| gradient | the gradient at the estimated maximum. |
| steps | number of function calls. |

## Examples

```
## snigFit -
    # Simulate Random Variates:
    set.seed(1953)
    s = rsnig(n = 2000, zeta = 0.7, rho = 0.5)
## snigFit -
    # Fit Parameters:
    snigFit(s, zeta = 1, rho = 0, doplot = TRUE)
```

```
ssd Spline Smoothed Distribution
```


## Description

Density, distribution function, quantile function and random generation from smoothing spline estimates.

## Usage

```
    dssd(x, param, log = FALSE)
    pssd(q, param)
    qssd(p, param)
    rssd(n, param)
```


## Arguments

$x, q \quad a \quad$ numeric vector of quantiles.
$p \quad a \quad$ numeric vector of probabilities.
n number of observations.
param an object as returned by the function ssdFit.
$\log \quad$ a logical flag by default FALSE. Should labels and a main title drawn to the plot?

## Details

dssd gives the density, pssd gives the distribution function, qssd gives the quantile function, and rssd generates random deviates.

## Value

numeric vector

## Author(s)

Diethelm Wuertz, Chong Gu for the underlying gss package.

## References

Gu, C. (2002), Smoothing Spline ANOVA Models, New York Springer-Verlag.
Gu, C. and Wang, J. (2003), Penalized likelihood density estimation: Direct cross-validation and scalable approximation, Statistica Sinica, 13, 811-826.

## Examples

```
    ## ssdFit -
    set.seed(1953)
    r = rnorm(500)
    hist(r, breaks = "FD", probability = TRUE,
        col = "steelblue", border = "white")
## ssdFit -
    param = ssdFit(r)
## dssd -
    u = seq(min(r), max(r), len = 301)
    v = dssd(u, param)
    lines(u, v, col = "orange", lwd = 2)
```

    ssdFit Fit density using smoothing splines
    
## Description

Estimates the parameters of a density function using smoothing splines.

## Usage

ssdFit(x)

## Arguments

x a numeric vector.

## Value

for ssdFit, an object of class ssden. The returned object can be used to evaluate density, probabilities and quantiles.

## Author(s)

Diethelm Wuertz, Chong Gu for the underlying gss package.

## References

Gu, C. (2002), Smoothing Spline ANOVA Models, New York Springer-Verlag.
Gu, C. and Wang, J. (2003), Penalized likelihood density estimation: Direct cross-validation and scalable approximation, Statistica Sinica, 13, 811-826.

## Examples

```
    ## ssdFit -
    set.seed(1953)
    r = rnorm(500)
    hist(r, breaks = "FD", probability = TRUE,
        col = "steelblue", border = "white")
## ssdFit -
    param = ssdFit(r)
## dssd -
    u = seq(min(r), max(r), len = 301)
    v = dssd(u, param)
    lines(u, v, col = "orange", lwd = 2)
```

StableSlider Slider GUI for Stable Distribution

## Description

The stableSlider() function provides interactive displays of density and probabilities of stable distributions.

## Usage

stableSlider(col= "steelblue", col.med = "gray30")

## Arguments

col colour for the density and distributions functions.
col.med colour for the median.

## Value

The stableSlider() function displays densities and probabilities of the skew stable distribution, for educational purposes.

## Author(s)

Diethelm Wuertz for the Rmetrics R-port.

## References

see those in dstable, in package stabledist.

## Examples

if(dev.interactive()) stableSlider()
symbolTable Table of symbols

## Description

Displays a table of plot characters and symbols.

## Usage

symbolTable(font $=\operatorname{par}($ 'font'), cex $=0.7$ )

## Arguments

cex a numeric value, determines the character size, the default size is 0.7 .
font an integer value, the number of the font, by default font number 1.

## Value

displays a table with the plot characters and symbols numbered from 0 to 255 and returns invisibly the name of the font.

## Note

Symbols with codes on the range 128-255 are not legitimate in some locales, most notably UTF-8. Moreover, what happens with non-ASCII characters in plots is system dependent and depends on the graphics device, as well. Use of such characters is not recommended for portable code.

From version 4031.95 of package fBasics, the characters are always defined as Latin1. In particular, in UTF8 locales the system converts them internally to UTF8. Still some symbols are not usable and non-ASCII symbols are not recommended, as pointed out above. For details, see the help page of points(), in particular the discussion of its argument pch.

## See Also

characterTable, colorTable
pdf for discussion of encodings for the pdf device

## Examples

\# symbolTable()

## Description

Produces an index/price, a cumulated return, a return, or a drawdown plot.

## Usage

```
seriesPlot(x, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
cumulatedPlot(x, index = 100, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
returnPlot(x, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
drawdownPlot(x, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
```


## Arguments

box a logical flag, should a box be added to the plot? By default TRUE.
col the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat. colors (ncol (x)).
grid a logical flag, should a grid be added to the plot? By default TRUE.
index a numeric value, by default 100. The function cumulates column by colum the returns and multiplies the result with the index value: index*exp(colCumsums (x)).
labels a logical flag, should the plot be returned with default labels and decorated in an automated way? By default TRUE.
rug a logical flag, by default TRUE. Should a rug representation of the data added to the plot?
title a logical flag, by default TRUE. Should a default title added to the plot?
type what type of plot should be drawn? By default we use a line plot, type="l". An alternative plot style which produces nice figures is for example type="h".
x
an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other then timeSeries objects, is more or less untested.
... optional arguments to be passed.

## Details

List of Functions:

$$
\begin{array}{ll}
\text { seriesPlot } & \text { Returns a tailored return series plot, } \\
\text { cumulatedPlot } & \text { Displays a cumulated series given the returns, } \\
\text { returnPlot } & \text { Displays returns given the cumulated series, } \\
\text { drawdownPlot } & \text { Displays drawdowns given the return series. }
\end{array}
$$

The plot functions can be used to plot univariate and multivariate time series of class timeSeries.
The graphical parameters type and col can be set by the values specified through the argument list. In the case of multivariate time series col can be specified by the values returned by a color palette.
Automated titles including main title, $x$ - and $y$-lables, grid lines, box style and rug represenatations cann be selected by setting these arguments to TRUE which is the default. If the title flag is unset, then the main title, $x$-, and y-labels are empty strings. This allows to set user defined labels with the function title after the plot is drawn.

Beside type, col, main, xlab and ylab, all other par arguments can be passed to the plot function.
If the labels flag is unset to FALSE, then no decorations will be added tothe plot, and the plot can be fully decorated by the user.

## Value

displays a time series plot

## Examples

```
## seriesPlot -
    data(LPP2005REC, package = "timeSeries")
    tS <- as.timeSeries(LPP2005REC)
    seriesPlot(tS)
```

    tr
    
## Description

Computes the trace of a matrix.

## Usage

$\operatorname{tr}(\mathrm{x})$

## Arguments

x
a numeric matrix.

## Details

tr computes the trace of a square matrix, i.e., the sum of its diagonal elements.
If the matrix is not square, tr returns NA.

## References

Golub, van Loan, (1996); Matrix Computations, 3rd edition. Johns Hopkins University Press.

## Examples

```
## Create Pascal Matrix:
    P = pascal(3)
    P
## Trace:
    tr(P)
```

triang Upper and lower triangular matrices

## Description

Extracs the upper or lower triangular part from a matrix.

## Usage

triang (x)
Triang(x)

## Arguments

X a numeric matrix.

## Details

triang and Triang transform a square matrix to a lower or upper triangular form. The functions just replace the remaining values with zeroes and work with non-square matrices, as well.
A triangular matrix is either an upper triangular matrix or lower triangular matrix. For the first case all matrix elements $a[i, j]$ of matrix $A$ are zero for $i>j$, whereas in the second case we have just the opposite situation. A lower triangular matrix is sometimes also called left triangular.
In fact, triangular matrices are so useful that much of computational linear algebra begins with factoring or decomposing a general matrix or matrices into triangular form. Some matrix factorization methods are the Cholesky factorization and the LU-factorization. Even including the factorization step, enough later operations are typically avoided to yield an overall time savings.
Triangular matrices have the following properties: the inverse of a triangular matrix is a triangular matrix, the product of two triangular matrices is a triangular matrix, the determinant of a triangular matrix is the product of the diagonal elements, the eigenvalues of a triangular matrix are the diagonal elements.

## Value

a matrix of the same dimensions as $x$ with the elements above or below the main diagonal set to zeroes

## References

Higham, N.J., (2002); Accuracy and Stability of Numerical Algorithms, 2nd ed., SIAM.
Golub, van Loan, (1996); Matrix Computations, 3rd edition. Johns Hopkins University Press.

## Examples

```
## Create Pascal Matrix:
    P = pascal(3)
    P
## Create lower triangle matrix
    L = triang(P)
    L
```

tsHessian Two sided approximated Hessian

## Description

Computes two sided (TS) approximated Hessian.

## Usage

tsHessian( $x$, fun, ...)

## Arguments

| $x$ | argument to be passed to fun. |
| :--- | :--- |
| fun | function. |
| $\ldots$ | additional parameters to be passed to fun. |

## Author(s)

A function borrowed from Kevin Sheppard's Matlab garch toolbox as implemented by Alexios Ghalanos in his rgarch package.
tslag Lagged or leading vector/matrix

## Description

Creates a lagged or leading vector/matrix of selected order(s).

## Usage <br> $\operatorname{tslag}(\mathrm{x}, \mathrm{k}=1, \operatorname{trim}=\mathrm{FALSE})$

## Arguments

k an integer value, the number of positions the new series is to lag or to lead the input series.
$x \quad$ a numeric vector or matrix, missing values are allowed.
trim a logical flag, if TRUE, the missing values at the beginning ans/or end of the returned series will be trimmed. The default value is FALSE.

## See Also

pdl

## Examples

```
    ## tslag -
```

varianceTest

Two sample variance tests

## Description

Tests if two series differ in their distributional variance parameter.

## Usage

```
varianceTest(x, y, method = c("varf", "bartlett", "fligner"),
    title = NULL, description = NULL)
```


## Arguments

$x, y \quad$ numeric vectors of data values.
method a character string naming which test should be applied.
title an optional title string, if not specified the inputs data name is deparsed.
description optional description string, or a vector of character strings.

## Details

The method="varf" can be used to compare variances of two normal samples performing an F test. The null hypothesis is that the ratio of the variances of the populations from which they were drawn is equal to one.

The method="bartlett" performs the Bartlett test of the null hypothesis that the variances in each of the samples are the same. This fact of equal variances across samples is also called homogeneity of variances. Note, that Bartlett's test is sensitive to departures from normality. That is, if the samples come from non-normal distributions, then Bartlett's test may simply be testing for nonnormality. The Levene test (not yet implemented) is an alternative to the Bartlett test that is less sensitive to departures from normality.
The method="fligner" performs the Fligner-Killeen test of the null that the variances in each of the two samples are the same.

## Value

an object from class fHTEST

## Note

Some of the test implementations are selected from R's ctest package.

## Author(s)

R-core team for hypothesis tests implemented from R's package ctest.

## References

Conover, W. J. (1971); Practical nonparametric statistics, New York: John Wiley \& Sons.
Lehmann E.L. (1986); Testing Statistical Hypotheses, John Wiley and Sons, New York.

## Examples

```
## rnorm -
    # Generate Series:
    x = rnorm(50)
    y = rnorm(50)
## varianceTest -
    varianceTest(x, y, "varf")
    varianceTest(x, y, "bartlett")
    varianceTest(x, y, "fligner")
```

```
vec Stacking vectors and matrices
```


## Description

Stacks either a lower triangle matrix or a matrix.

## Usage

$\operatorname{vec}(x)$
$\operatorname{vech}(x)$

## Arguments

X
a numeric matrix.

## Details

The function vec implements the operator that stacks a matrix as a column vector, to be more precise in a matrix with one column. $\operatorname{vec}(X)=\left(X_{11}, X_{21}, \ldots, X_{N 1}, X_{12}, X_{22}, \ldots, X_{N N}\right)$.
The function vech implements the operator that stacks the lower triangle of a NxN matrix as an $\mathrm{N}(\mathrm{N}+1) / 2 \mathrm{x} 1$ vector: $\operatorname{vech}(X)=\left(X_{11}, X_{21}, X_{22}, X_{31}, \ldots, X_{N N}\right)$, to be more precise in a matrix with one row.

## Examples

```
    ## Create Pascal Matrix:
        P = pascal(3)
    ## Stack a matrix
    vec(P)
    ## Stack the lower triangle
    vech(P)
```

volatility Compute volatility

## Description

Generic function for volatility computations.

## Usage

```
volatility(object, ...)
\#\# Default S3 method:
volatility(object, ...)
```

volatility

## Arguments

object
. . .
an object from which to extract or compute the volatility.
arguments for methods. Ignored by the default method.

## Details

volatility is a generic function, whose default method centers and squares the values in object. Other packages can (and do) define methods for it.

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