

Package ‘jti’

July 5, 2021

Title Junction Tree Inference

Version 0.8.0

Date 2021-07-05

Description Minimal and memory efficient implementation of the junction tree algorithm using the Lauritzen-Spiegelhalter scheme;
S. L. Lauritzen and D. J. Spiegelhalter (1988)
<<https://www.jstor.org/stable/2345762?seq=1>>.

Depends R (>= 3.5.0)

URL <https://github.com/mlindsk/jti>

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Encoding UTF-8

LazyData true

Imports Rcpp, igraph, sparta

LinkingTo Rcpp, RcppArmadillo

RoxygenNote 7.1.1

SystemRequirements C++11

Suggests tinytest

NeedsCompilation yes

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Repository CRAN

Date/Publication 2021-07-05 14:40:02 UTC

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jti-package	<i>jti: Junction Tree Inference</i>
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Description

Minimal and memory efficient implementation of the junction tree algorithm using the Lauritzen-Spiegelhalter scheme. S. L. Lauritzen and D. J. Spiegelhalter (1988).

Author(s)

Maintainer: Mads Lindskou <mads@math.aau.dk>

See Also

Useful links:

- <https://github.com/mlindsk/jti>

asia

Asia

Description

Small synthetic data set from Lauritzen and Spiegelhalter (1988) about lung diseases (tuberculosis, lung cancer or bronchitis) and visits to Asia. This copy of the data was taken from the R package "bnlearn" where all values "yes" have been converted to "y" and all values "no" have been converted to "n".

Usage

```
asia
```

Format

An object of class `tbl_df` (inherits from `tbl`, `data.frame`) with 5000 rows and 8 columns.

Details

D (**dyspnea**)

T (**tuberculosis**)

L (**lung cancer**)

B (**bronchitis**)

A (**visit to Asia**)

S (**smoking**)

X (**chest C-ray**)

E (**tuberculosis vs cancer/bronchitis**)

References

[bnlearn-asia](#)

asia2

Asia2

Description

See the `asia` data for information. This version, has class `bn_fit`.

Usage

```
asia2
```

Format

An object of class `list` of length 8.

References

[bnlearn-asia](#)

<code>bnfit_to_cpts</code>	<i>bnfit to cpts</i>
----------------------------	----------------------

Description

Convert a `bn.fit` object (a list of `cpts` from the `bnlearn` package) into a list of ordinary array-like `cpts`

Usage

```
bnfit_to_cpts(x)
```

Arguments

<code>x</code>	A <code>bn.fit</code> object
----------------	------------------------------

<code>compile</code>	<i>Compile information</i>
----------------------	----------------------------

Description

Compiled objects are used as building blocks for junction tree inference

Usage

```
compile(
  x,
  evidence = NULL,
  root_node = "",
  joint_vars = NULL,
  tri = "min_fill",
  pmf_evidence = NULL,
  alpha = NULL
)

## S3 method for class 'cpt_list'
compile(
  x,
```

```

    evidence = NULL,
    root_node = "",
    joint_vars = NULL,
    tri = "min_fill",
    pmf_evidence = NULL,
    alpha = NULL
)

## S3 method for class 'pot_list'
compile(
  x,
  evidence = NULL,
  root_node = "",
  joint_vars = NULL,
  tri = "min_fill",
  pmf_evidence = NULL,
  alpha = NULL
)

```

Arguments

<code>x</code>	An object returned from <code>cpt_list</code> (baeysian network) or <code>pot_list</code> (decomposable markov random field)
<code>evidence</code>	A named vector. The names are the variabes and the elements are the evidence.
<code>root_node</code>	A node for which we require it to live in the root clique (the first clique).
<code>joint_vars</code>	A vector of variables for which we require them to be in the same clique. Edges between all these variables are added to the moralized graph.
<code>tri</code>	The optimization strategy used for triangulation if <code>x</code> originates from a Baeysian network. One of <ul style="list-style-type: none"> • 'min_fill' • 'min_rfill' • 'min_efill' • 'min_sfill' • 'min_sp' • 'min_esp' • 'min_nei' • 'minimal' • 'alpha'
<code>pmf_evidence</code>	A named vector of frequencies. The names should correspond to the evidence that is expected to see over time. Relevant in connection to <code>min_efill</code> and <code>min_esp</code> triangulations.
<code>alpha</code>	Character vector. A permutation of the nodes in the graph. It specifies a user-supplied elimination ordering for triangulation of the moral graph.

Details

The Junction Tree Algorithm performs both a forward and inward message pass (collect and distribute). However, when the forward phase is finished, the root clique potential is guaranteed to be the joint pmf over the variables involved in the root clique. Thus, if it is known in advance that a specific variable is of interest, the algorithm can be terminated after the forward phase. Use the `root_node` to specify such a variable and specify `propagate = "collect"` in the junction tree algorithm function `jt`.

Moreover, if interest is in some joint pmf for variables that end up being in different cliques these variables must be specified in advance using the `joint_vars` argument. The compilation step then adds edges between all of these variables to ensure that at least one clique contains all of them.

Evidence can be entered either at compile stage or after compilation. Hence, one can also combine evidence from before compilation with evidence after compilation. `Before` refers to entering evidence in the `'compile'` function and `after` refers to entering evidence in the `'jt'` function.

Finally, one can either use a Bayesian network or a decomposable Markov random field (use the `ess` package to fit these). Bayesian networks must be constructed with `cpt_list` and decomposable MRFs should be constructed with `pot_list`, but can also be constructed using `cpt_list`.

Examples

```
cpt1 <- cpt_list(asia2)
cp1 <- compile(cpt1, evidence = c(bronc = "yes"), joint_vars = c("bronc", "tub"))
print(cp1)
names(cp1)
dim_names(cp1)
plot(get_graph(cp1))
```

`cpt_list`

Conditional probability list

Description

A check and conversion of cpts to be used in the junction tree algorithm

Usage

```
cpt_list(x, g = NULL)

## S3 method for class 'list'
cpt_list(x, g = NULL)

## S3 method for class 'data.frame'
cpt_list(x, g)
```

Arguments

- `x` Either a named list with cpts in form of array-like object(s) where names must be the child node or a `data.frame`
- `g` Either a directed acyclic graph (DAG) as an `igraph` object or a decomposable graph as an `igraph` object. If `x` is a list, `g` must be `NULL`. The procedure then deduce the graph from the conditional probability tables.

Examples

```
library(igraph)
e1 <- matrix(c(
  "A", "T",
  "T", "E",
  "S", "L",
  "S", "B",
  "L", "E",
  "E", "X",
  "E", "D",
  "B", "D"),
  nc = 2,
  byrow = TRUE
)

g <- igraph::graph_from_edgelist(e1)
cl <- cpt_list(asia, g)

print(cl)
dim_names(cl)
names(cl)
plot(get_graph(cl))
```

dim_names

Various getters

Description

Getter methods for `cpt_list`, `pot_list`, `charge` and `jt` objects

Usage

```
dim_names(x)

has_inconsistencies(x)

## S3 method for class 'cpt_list'
dim_names(x)
```

```
## S3 method for class 'cpt_list'  
names(x)  
  
## S3 method for class 'pot_list'  
dim_names(x)  
  
## S3 method for class 'pot_list'  
names(x)  
  
## S3 method for class 'charge'  
dim_names(x)  
  
## S3 method for class 'charge'  
names(x)  
  
## S3 method for class 'charge'  
has_inconsistencies(x)  
  
## S3 method for class 'jt'  
dim_names(x)  
  
## S3 method for class 'jt'  
names(x)  
  
## S3 method for class 'jt'  
has_inconsistencies(x)
```

Arguments

x cpt_list, pot_list, charge or jt

get_cliques *Return the cliques of a junction tree*

Description

Return the cliques of a junction tree

Usage

```
get_cliques(x)  
  
## S3 method for class 'jt'  
get_cliques(x)  
  
## S3 method for class 'charge'  
get_cliques(x)
```



```
## S3 method for class 'pot_list'  
get_cliques(x)  
  
get_clique_root_idx(x)  
  
## S3 method for class 'jt'  
get_clique_root_idx(x)  
  
get_clique_root(x)  
  
## S3 method for class 'jt'  
get_clique_root(x)
```

Arguments

x A junction tree object, jt.

See Also

[jt](#)

Examples

```
# See Example 5 and 6 of the 'jt' function
```

get_graph

Get graph

Description

Retrieve the graph from

Usage

```
get_graph(x)  
  
## S3 method for class 'charge'  
get_graph(x)  
  
## S3 method for class 'cpt_list'  
get_graph(x)  
  
## S3 method for class 'pot_list'  
get_graph(x)
```

Arguments

x cpt_list or a compiled object

Value

A graph as an igraph object

jt *Junction Tree*

Description

Construction of a junction tree and message passing

Usage

```
jt(x, evidence = NULL, flow = "sum", propagate = "full")
```

```
## S3 method for class 'charge'
```

```
jt(x, evidence = NULL, flow = "sum", propagate = "full")
```

Arguments

x An object return from compile

evidence A named vector. The names are the variabes and the elements are the evidence

flow Either "sum" or "max"

propagate Either "no", "collect" or "full".

Details

Evidence can be entered either at compile stage or after compilation. Hence, one can also combine evidence from before compilation with evidence after compilation. Before refers to entering evidence in the 'compile' function and after refers to entering evidence in the 'jt' function.

Value

A jt object

See Also

[query_belief](#), [mpe](#), [get_cliques](#), [get_clique_root](#), [propagate](#)

Examples

```

# Setting up the network
# -----

library(igraph)
e1 <- matrix(c(
  "A", "T",
  "T", "E",
  "S", "L",
  "S", "B",
  "L", "E",
  "E", "X",
  "E", "D",
  "B", "D"),
  nc = 2,
  byrow = TRUE
)

g <- igraph::graph_from_edgelist(e1)
plot(g)
# -----

# Data
# ----
# We use the asia data; see the man page (?asia)

# Compilation
# -----
cl <- cpt_list(asia, g) # Checking and conversion
cp <- compile(cl)

# After the network has been compiled, the graph has been triangulated and
# moralized. Furthermore, all conditional probability tables (CPTs) has been
# designated one of the cliques (in the triangulated and moralized graph).

# Example 1: sum-flow without evidence
# -----
jt1 <- jt(cp)
plot(jt1)
print(jt1)
query_belief(jt1, c("E", "L", "T"))
query_belief(jt1, c("B", "D", "E"), type = "joint")

# Notice, that jt1 is equivalent to:
# jt1 <- jt(cp, propagate = "no")
# jt1 <- propagate(jt1, prop = "full")

# That is; it is possible to postpone the actual propagation
# In this setup, the junction tree is saved in the jt1 object,
# and one can repeatedly enter evidence for new observations

```

```

# using the set_evidence function on jt1 and then query
# several probabilities without repeatedly calculating the
# the junction tree over and over again. One just needs
# to use the propagate function on jt1.

# Example 2: sum-flow with evidence
# -----

e2 <- c(A = "y", X = "n")
jt2 <- jt(cp, e2)
query_belief(jt2, c("B", "D", "E"), type = "joint")

# Notice that, the configuration (D,E,B) = (y,y,n) has changed
# dramatically as a consequence of the evidence

# We can get the probability of the evidence:
query_evidence(jt2)

# Example 3: max-flow without evidence
# -----

jt3 <- jt(cp, flow = "max")
mpe(jt3)

# Example 4: max-flow with evidence
# -----

e4 <- c(T = "y", X = "y", D = "y")
jt4 <- jt(cp, e4, flow = "max")
mpe(jt4)

# Notice, that T, E, S, B, X and D has changed from "n" to "y"
# as a consequence of the new evidence e4

# Example 5: specifying a root node and only collect to save run time
# -----

cp5 <- compile(cpt_list(asia, g), root_node = "X")
jt5 <- jt(cp5, propagate = "collect")
query_belief(jt5, get_clique_root(jt5), "joint")

# We can only query from the variables in the root clique now
# but we have ensured that the node of interest, "X", does indeed live in
# this clique. The variables are found using 'get_clique_root'

# Example 6: Compiling from a list of conditional probabilities
# -----

# * We need a list with CPTs which we extract from the asia2 object
#   - the list must be named with child nodes
#   - The elements need to be array-like objects

```

```

c1 <- cpt_list(asia2)
cp6 <- compile(c1)

# Inspection; see if the graph correspond to the cpts
# g <- get_graph(cp6)
# plot(g)

# This time we specify that no propagation should be performed
jt6 <- jt(cp6, propagate = "no")

# We can now inspect the collecting junction tree and see which cliques
# are leaves and parents
plot(jt6)
get_cliques(jt6)
get_clique_root(jt6)

leaves(jt6)
unlist(parents(jt6))

# That is;
# - clique 2 is parent of clique 1
# - clique 3 is parent of clique 4 etc.

# Next, we send the messages from the leaves to the parents
jt6 <- send_messages(jt6)

# Inspect again
plot(jt6)

# Send the last message to the root and inspect
jt6 <- send_messages(jt6)
plot(jt6)

# The arrows are now reversed and the outwards (distribute) phase begins
leaves(jt6)
parents(jt6)

# Clique 2 (the root) is now a leave and it has 1, 3 and 6 as parents.

# Finishing the message passing
jt6 <- send_messages(jt6)
jt6 <- send_messages(jt6)

# Queries can now be performed as normal
query_belief(jt6, c("either", "tub"), "joint")

```

Description

Number of binary operations needed to propagate in a junction tree given evidence, using the Lauritzen-Spiegelhalter scheme

Usage

```
jt_nbinary_ops(x, evidence = character(0), root = NULL)

## S3 method for class 'jt'
jt_nbinary_ops(x, evidence = character(0), root = NULL)

## S3 method for class 'triangulation'
jt_nbinary_ops(x, evidence = character(0), root = NULL)
```

Arguments

x	A junction tree object or an object returned from the triangulation function
evidence	Character vector of evidence nodes
root	Integer specifying the root node in the junction tree

leaves

Query Parents or Leaves in a Junction Tree

Description

Return the clique indices of current parents or leaves in a junction tree

Usage

```
leaves(jt)

## S3 method for class 'jt'
leaves(jt)

parents(jt)

## S3 method for class 'jt'
parents(jt)
```

Arguments

jt	A junction tree object, jt.
----	-----------------------------

See Also

[jt, get_cliques](#)

Examples

```
# See example 6 in the help page for the jt function
```

```
mpd Maximal Prime Decomposition
```

Description

Find the maximal prime decomposition and its associated junction tree

Usage

```
mpd(x, save_graph = TRUE)

## S3 method for class 'matrix'
mpd(x, save_graph = TRUE)

## S3 method for class 'cpt_list'
mpd(x, save_graph = TRUE)
```

Arguments

x	Either a neighbor matrix or a <code>cpt_list</code> object
save_graph	Logical indicating if the moralized graph should be kept. Useful when x is a <code>cpt_list</code> object.

Value

- `prime_ints`: a list with the prime components, - `flawed`: indicating which prime components that are triangulated - `jt_collect`: the MPD junction tree prepared for collecting

Examples

```
library(igraph)
e1 <- matrix(c(
  "A", "T",
  "T", "E",
  "S", "L",
  "S", "B",
  "L", "E",
  "E", "X",
  "E", "D",
  "B", "D"),
  nc = 2,
  byrow = TRUE
)
```

```
g <- igraph::graph_from_edgelist(e1, directed = FALSE)
A <- igraph::as_adjacency_matrix(g, sparse = FALSE)
mpd(A)
```

mpe *Most Probable Explanation*

Description

Returns the most probable explanation given the evidence entered in the junction tree

Usage

```
mpe(x)

## S3 method for class 'jt'
mpe(x)
```

Arguments

x A junction tree object, jt, with max-flow.

See Also

[jt](#)

Examples

```
# See the 'jt' function
```

plot.jt *A plot method for junction trees*

Description

A plot method for junction trees

Usage

```
## S3 method for class 'jt'
plot(x, ...)
```

Arguments

x A junction tree object, jt.
 ... For S3 compatability. Not used.

See Also[jt](#)

pot_list	<i>A check and extraction of clique potentials from a Markov random field to be used in the junction tree algorithm</i>
----------	---

Description

A check and extraction of clique potentials from a Markov random field to be used in the junction tree algorithm

Usage

```
pot_list(x, g)

## S3 method for class 'data.frame'
pot_list(x, g)
```

Arguments

x	Character data.frame
g	A decomposable Markov random field as an igraph object.

Examples

```
# Typically one would use the ess package:
# library(ess)
# g <- ess::fit_graph(derma)
# pl <- pot_list(derma, ess::as_igraph(g))
# pl

# Another example
g <- igraph::sample_gnm(ncol(asia), 12)
while(!igraph::is.chordal(g)$chordal) g <- igraph::sample_gnm(ncol(asia), 12, FALSE)
igraph::V(g)$name <- colnames(asia)
plot(g)
pot_list(asia, g)
```

print.charge	<i>A print method for compiled objects</i>
--------------	--

Description

A print method for compiled objects

Usage

```
## S3 method for class 'charge'  
print(x, ...)
```

Arguments

x	A compiled object
...	For S3 compatibility. Not used.

See Also

[jt](#)

print.cpt_list	<i>A print method for cpt lists</i>
----------------	-------------------------------------

Description

A print method for cpt lists

Usage

```
## S3 method for class 'cpt_list'  
print(x, ...)
```

Arguments

x	A cpt_list object
...	For S3 compatibility. Not used.

See Also

[compile](#)

print.jt	<i>A print method for junction trees</i>
----------	--

Description

A print method for junction trees

Usage

```
## S3 method for class 'jt'  
print(x, ...)
```

Arguments

x	A junction tree object, jt.
...	For S3 compatability. Not used.

See Also

[jt](#)

print.pot_list	<i>A print method for pot lists</i>
----------------	-------------------------------------

Description

A print method for pot lists

Usage

```
## S3 method for class 'pot_list'  
print(x, ...)
```

Arguments

x	A pot_list object
...	For S3 compatability. Not used.

See Also

[compile](#)

propagate	<i>Propagation of junction trees</i>
-----------	--------------------------------------

Description

Given a junction tree object, propagation is conducted

Usage

```
propagate(x, prop = "full")

## S3 method for class 'jt'
propagate(x, prop = "full")
```

Arguments

x	A junction tree object jt
prop	Either "collect" or "full".

See Also

[jt](#)

Examples

```
# See Example 1 in the 'jt' function
```

query_belief	<i>Query probabilities</i>
--------------	----------------------------

Description

Get probabilities from a junction tree object

Usage

```
query_belief(x, nodes, type = "marginal")

## S3 method for class 'jt'
query_belief(x, nodes, type = "marginal")
```

Arguments

x	A junction tree object, jt.
nodes	The nodes for which the probability is desired
type	Either 'marginal' or 'joint'

See Also[jt](#), [mpe](#)**Examples**

```
# See the 'jt' function
```

query_evidence	<i>Query Evidence</i>
----------------	-----------------------

Description

Get the probability of the evidence entered in the junction tree object

Usage

```
query_evidence(x)

## S3 method for class 'jt'
query_evidence(x)
```

Arguments

x A junction tree object, jt.

See Also[jt](#), [mpe](#)

send_messages	<i>Send Messages in a Junction Tree</i>
---------------	---

Description

Send messages from the current leaves to the current parents in a junction tree

Usage

```
send_messages(jt)
```

Arguments

jt A jt object return from the jt function

See Also[jt](#), [get_cliques](#), [leaves](#), [parents](#)

Examples

```
# See example 6 in the help page for the jt function
```

```
set_evidence      Enter Evidence
```

Description

Enter evidence into a the junction tree object that has not been propagated

Usage

```
set_evidence(x, evidence)

## S3 method for class 'jt'
set_evidence(x, evidence)
```

Arguments

x A junction tree object, jt.
evidence A named vector. The names are the variabes and the elements are the evidence.

See Also

[jt](#), [mpe](#)

Examples

```
# See the 'jt' function
```

```
sim_data_from_bn      Simulate data from a Bayesian network
```

Description

Simulate data from a Bayesian network

Usage

```
sim_data_from_bn(
  net,
  lvls,
  nsims = 1000,
  increasing_prob = FALSE,
  p1 = 0.8,
  p2 = 1
)
```

Arguments

net	A Bayesian network as an igraph object
lvls	Named integer vector where each element is the size of the statespace of the corresponding variable
nsims	Number of simulations distributions from which the simulatios are drawn.
increasing_prob	Logical. If true, probabilities in the underlying CPTs increases with as the number of levels increses.
p1	Probability
p2	Probability

Examples

```
net <- igraph::graph(as.character(c(1,2,1,3,3,4,3,5,5,4,2,6,6,7,5,7)), directed = TRUE)
nodes_net <- igraph::V(net)$name
lvls_net <- structure(sample(3:9, length(nodes_net)), names = nodes_net)
lvls_net <- structure(rep(3, length(nodes_net)), names = nodes_net)
sim_data_from_bn(net, lvls_net, 10)
```

sim_data_from_dmr *Simulate data from a decomposable discrete markov random field*

Description

Simulate data from a decomposable discrete markov random field

Usage

```
sim_data_from_dmr(
  graph,
  lvls,
  nsims = 1000,
  increasing_prob = FALSE,
  p1 = 0.8,
  p2 = 1
)
```

Arguments

graph	A decomposable discrete markov random field as an igraph object
lvls	Named integer vector where each element is the size of the statespace of the corresponding variable
nsims	Number of simulations distributions from which the simulatios are drawn.
increasing_prob	Logical. If true, probabilities in the underlying CPTs increases with as the number of levels increses.

p1	Probability
p2	Probability

triangulate	<i>Triangulate a Bayesian network</i>
-------------	---------------------------------------

Description

Given a list of CPTs, this function finds a triangulation

Usage

```

triangulate(
  x,
  root_node = "",
  joint_vars = NULL,
  tri = "min_fill",
  pmf_evidence = NULL,
  alpha = NULL,
  perm = NULL
)

## S3 method for class 'cpt_list'
triangulate(
  x,
  root_node = "",
  joint_vars = NULL,
  tri = "min_fill",
  pmf_evidence = NULL,
  alpha = NULL,
  perm = NULL
)

```

Arguments

x	An object returned from <code>cpt_list</code> (baeysian network) or <code>pot_list</code> (decomposable markov random field)
root_node	A node for which we require it to live in the root clique (the first clique).
joint_vars	A vector of variables for which we require them to be in the same clique. Edges between all these variables are added to the moralized graph.
tri	The optimization strategy used for triangulation if x originates from a Baeysian network. One of <ul style="list-style-type: none"> • 'min_fill' • 'min_rfill' • 'min_efill'

- 'min_sfill'
- 'min_sp'
- 'min_esp'
- 'min_nei'
- 'minimal'
- 'alpha'

pmf_evidence	A named vector of frequencies. The names should correspond to the evidence that is expected to see over time. Relevant in connection to min_efill and min_esp triangulations.
alpha	Character vector. A permutation of the nodes in the graph. It specifies a user-supplied elimination ordering for triangulation of the moral graph.
perm	Experimental

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